

# Turbulent Mixing in Galactic Disks

*Chao-Chin Yang*  
Lund Observatory

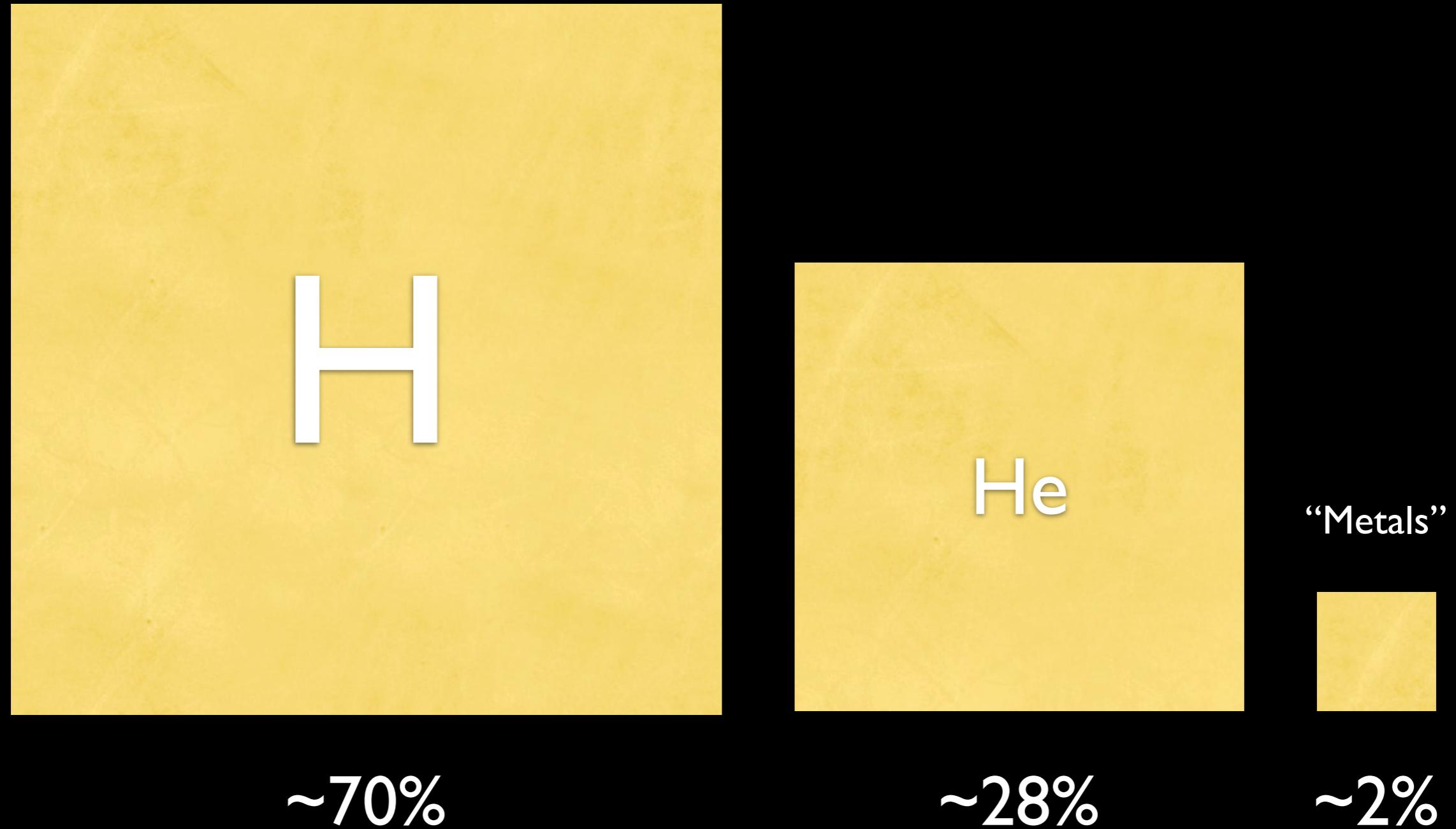
# Periodic Table of Elements

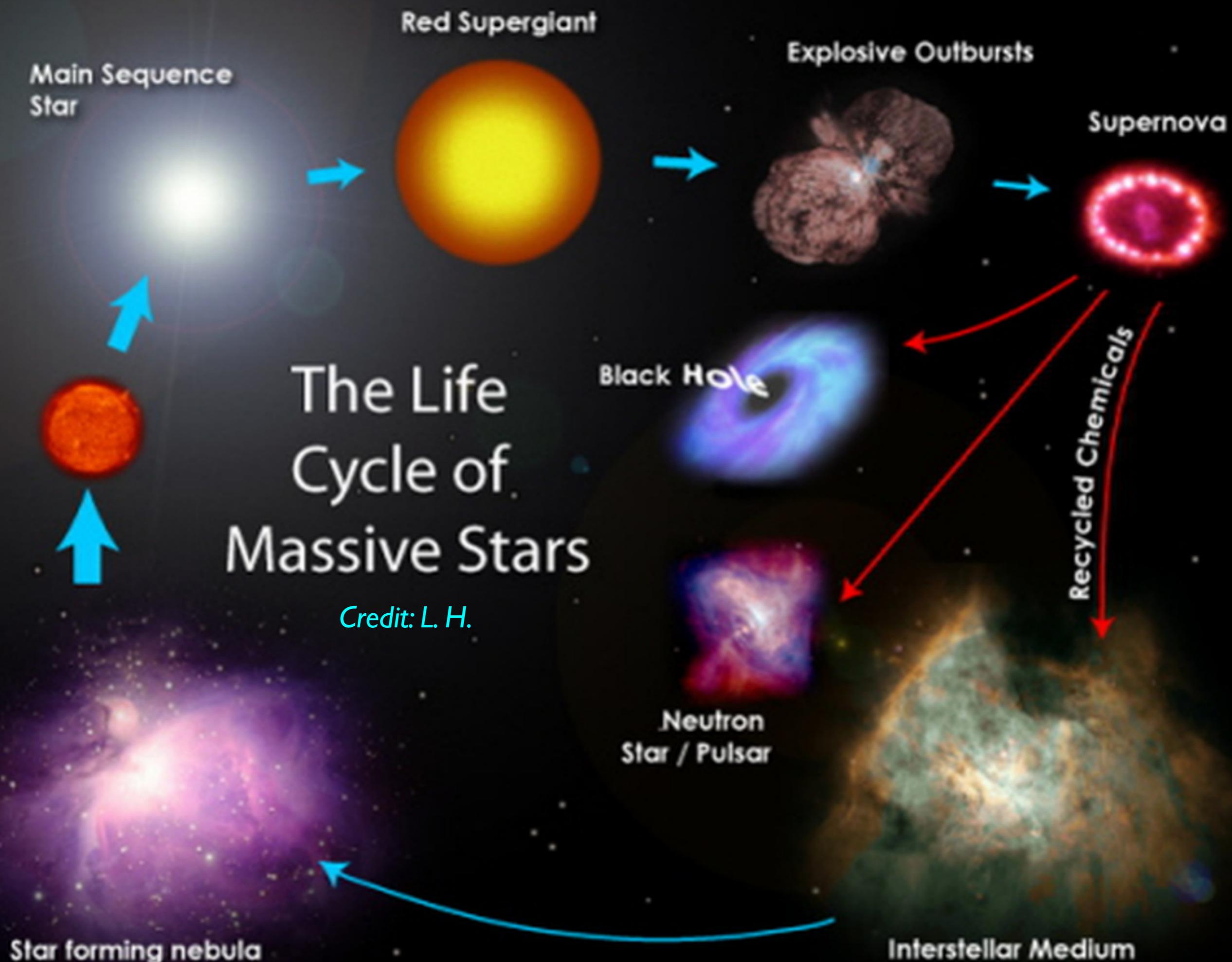
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18															
1 <b>H</b> Hydrogen 1.00794	2 <b>He</b> Helium 4.002602	3 <b>Li</b> Lithium 6.941	4 <b>Be</b> Beryllium 9.012182	5 <b>Sc</b> Scandium 44.955912	6 <b>Ti</b> Titanium 47.987	7 <b>V</b> Vanadium 50.9415	8 <b>Cr</b> Chromium 51.9961	9 <b>Mn</b> Manganese 54.938045	10 <b>Fe</b> Iron 55.845	11 <b>Co</b> Cobalt 58.933195	12 <b>Ni</b> Nickel 58.6934	13 <b>Cu</b> Copper 63.545	14 <b>Zn</b> Zinc 65.38	15 <b>Ga</b> Gallium 69.723	16 <b>Ge</b> Germanium 72.64	17 <b>As</b> Arsenic 74.92160	18 <b>Se</b> Selenium 78.96	19 <b>Kr</b> Krypton 83.798														
1 <b>Na</b> Sodium 22.98976928	2 <b>Ne</b> Neon 20.1797	3 <b>Mg</b> Magnesium 24.3060	4 <b>Rf</b> Unknown	5 <b>Al</b> Aluminum 26.9815386	6 <b>Si</b> Silicon 28.0855	7 <b>P</b> Phosphorus 30.973762	8 <b>S</b> Sulfur 32.066	9 <b>Cl</b> Chlorine 35.453	10 <b>Ar</b> Argon 39.948	11 <b>Rb</b> Rubidium 85.4878	12 <b>Sr</b> Strontium 87.62	13 <b>Y</b> Yttrium 88.90585	14 <b>Zr</b> Zirconium 91.224	15 <b>Nb</b> Niobium 92.90838	16 <b>Mo</b> Molybdenum 95.96	17 <b>Tc</b> Technetium (97.9072)	18 <b>Ru</b> Ruthenium 101.07	19 <b>Rh</b> Rhodium 102.90550	20 <b>Pd</b> Palladium 106.42	21 <b>Ag</b> Silver 107.8682	22 <b>Cd</b> Cadmium 112.411	23 <b>In</b> Indium 114.816	24 <b>Sn</b> Tin 118.710	25 <b>Sb</b> Antimony 121.760	26 <b>Te</b> Tellurium 127.60	27 <b>I</b> Iodine 131.293	28 <b>Xe</b> Xenon 131.320					
1 <b>Cs</b> Caesium 132.9054519	2 <b>Ba</b> Barium 137.327	3 <b>Hf</b> Hafnium 178.49	4 <b>Ta</b> Tantalum 180.94788	5 <b>W</b> Tungsten 183.84	6 <b>Re</b> Rhenium 186.207	7 <b>Os</b> Osmium 190.23	8 <b>Ir</b> Iridium 192.217	9 <b>Pt</b> Platinum 195.064	10 <b>Au</b> Gold 196.966569	11 <b>Hg</b> Mercury 200.59	12 <b>Tl</b> Thallium 204.3833	13 <b>Pb</b> Lead 207.2	14 <b>Bi</b> Bismuth 208.98040	15 <b>Po</b> Polonium (208.9824)	16 <b>At</b> Astatine (209.9871)	17 <b>Rn</b> Radon (222.0176)	18 <b>Fr</b> Francium (223)	19 <b>Ra</b> Radium (226)	20 <b>Rf</b> Rutherfordium (261)	21 <b>Db</b> Dubnium (262)	22 <b>Sg</b> Seaborgium (266)	23 <b>Bh</b> Bohrium (264)	24 <b>Hs</b> Hassium (277)	25 <b>Mt</b> Meitnerium (277)	26 <b>Ds</b> Darmstadtium (271)	27 <b>Rg</b> Roentgenium (272)	28 <b>Uub</b> Ununbium (285)	29 <b>Uut</b> Ununtrium (289)	30 <b>Uup</b> Ununquadium (289)	31 <b>Uuh</b> Ununhexium (292)	32 <b>Uus</b> Ununseptium (294)	33 <b>Uuo</b> Ununoctium (294)
For elements with no stable isotopes, the mass number of the isotope with the longest half-life is in parentheses.																																

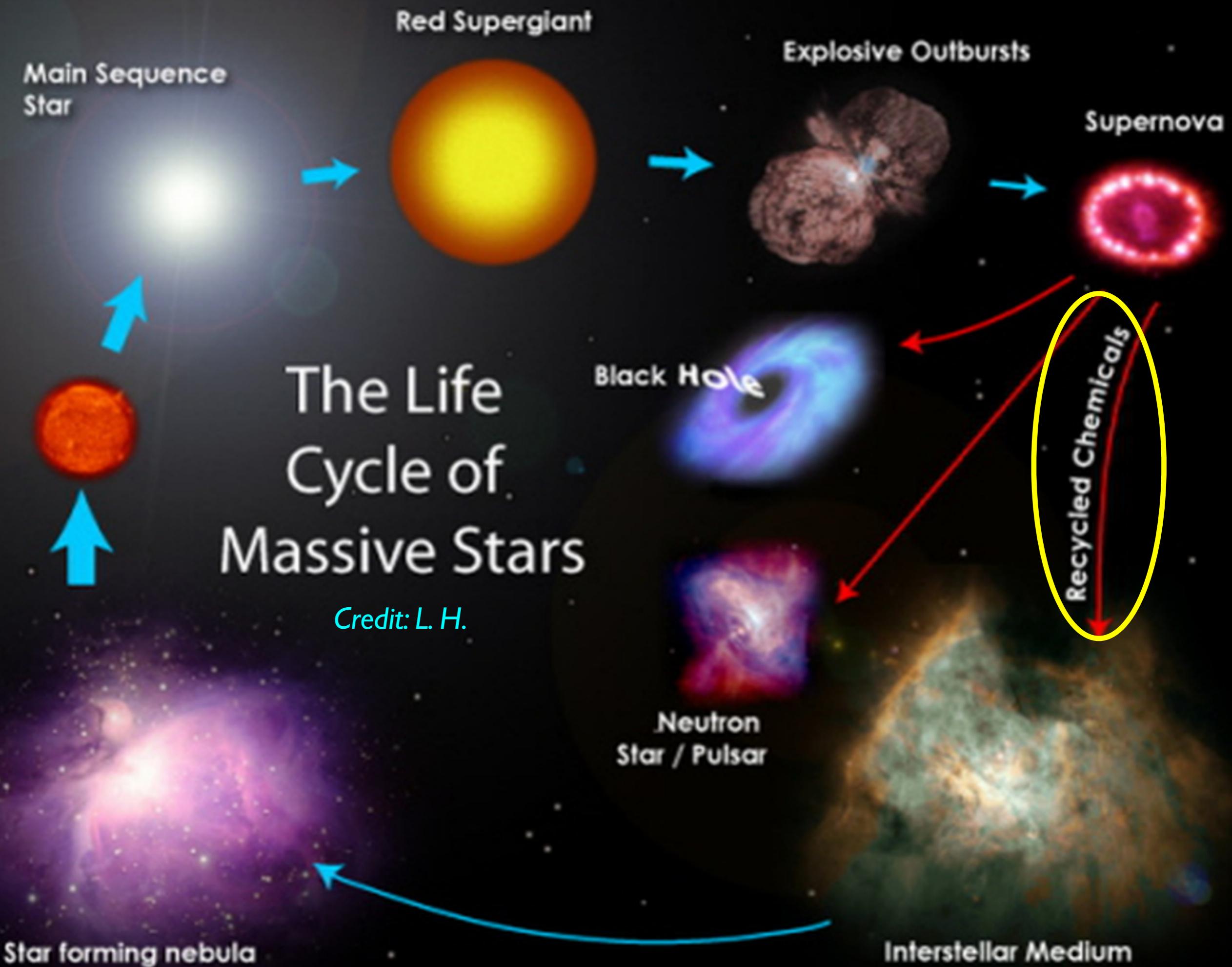
Design and Interface Copyright © 1997 Michael Dayah (michael@dayah.com). <http://www.ptable.com/>

57 <b>La</b> Lanthanum 138.90547	58 <b>Ce</b> Cerium 140.116	59 <b>Pr</b> Praseodymium 140.90765	60 <b>Nd</b> Neodymium 144.242	61 <b>Pm</b> Promethium (145)	62 <b>Sm</b> Samarium 150.36	63 <b>Eu</b> Europium 151.964	64 <b>Gd</b> Gadolinium 157.25	65 <b>Tb</b> Terbium 168.92535	66 <b>Dy</b> Dysprosium 162.500	67 <b>Ho</b> Holmium 164.93032	68 <b>Er</b> Erbium 167.259	69 <b>Tm</b> Thulium 168.93421	70 <b>Yb</b> Ytterbium 173.054	71 <b>Lu</b> Lutetium 174.90668	72 <b>Lu</b> Lutetium 174.90668	73 <b>Lu</b> Lutetium 174.90668	74 <b>Lu</b> Lutetium 174.90668	75 <b>Lu</b> Lutetium 174.90668	76 <b>Lu</b> Lutetium 174.90668	77 <b>Lu</b> Lutetium 174.90668	
89 <b>Ac</b> Actinium (227)	90 <b>Th</b> Thorium 232.03808	91 <b>Pa</b> Protactinium 231.03588	92 <b>U</b> Uranium 238.02891	93 <b>Np</b> Neptunium (237)	94 <b>Pu</b> Plutonium (244)	95 <b>Am</b> Americium (243)	96 <b>Cm</b> Curium (247)	97 <b>Bk</b> Berkelium (247)	98 <b>Cf</b> Californium (251)	99 <b>Es</b> Einsteinium (252)	100 <b>Fm</b> Fermium (257)	101 <b>Md</b> Mendelevium (258)	102 <b>No</b> Nobelium (259)	103 <b>Lr</b> Lawrencium (262)	104 <b>Lu</b> Lutetium 174.90668	105 <b>Lu</b> Lutetium 174.90668	106 <b>Lu</b> Lutetium 174.90668	107 <b>Lu</b> Lutetium 174.90668	108 <b>Lu</b> Lutetium 174.90668	109 <b>Lu</b> Lutetium 174.90668	110 <b>Lu</b> Lutetium 174.90668

# Periodic Table for Astronomers

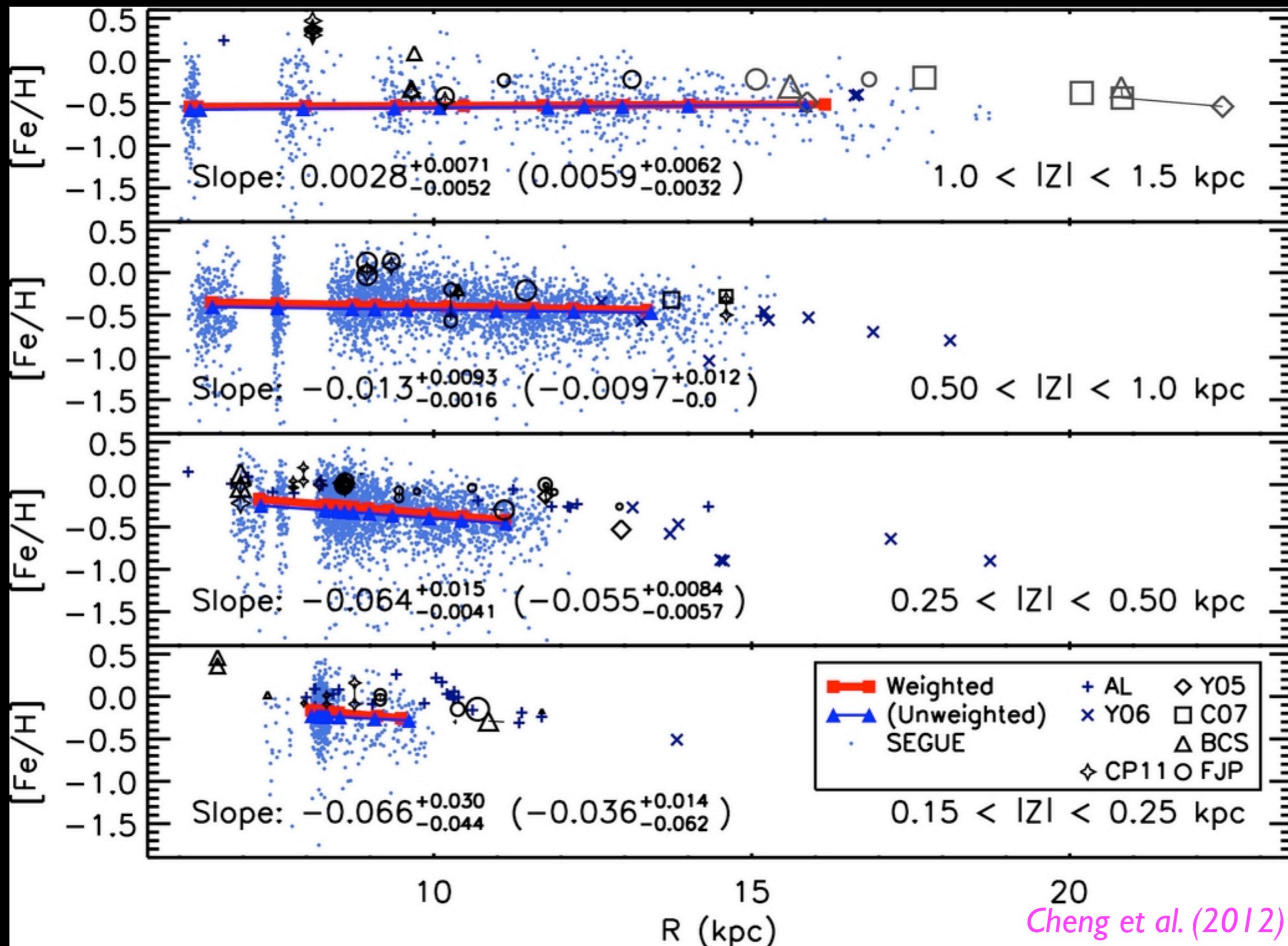




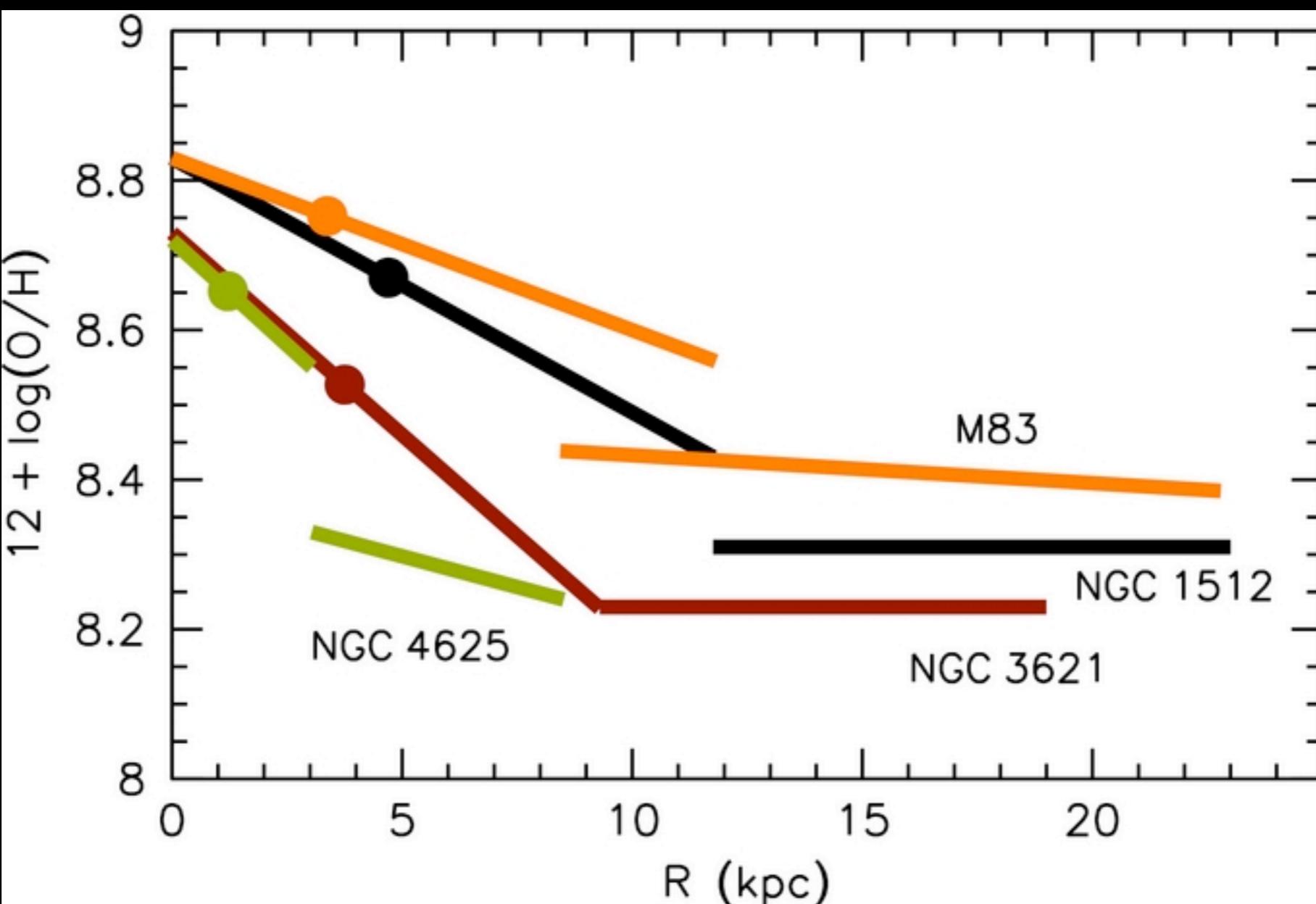


# Radial Metallicity Gradient

## The Milky Way



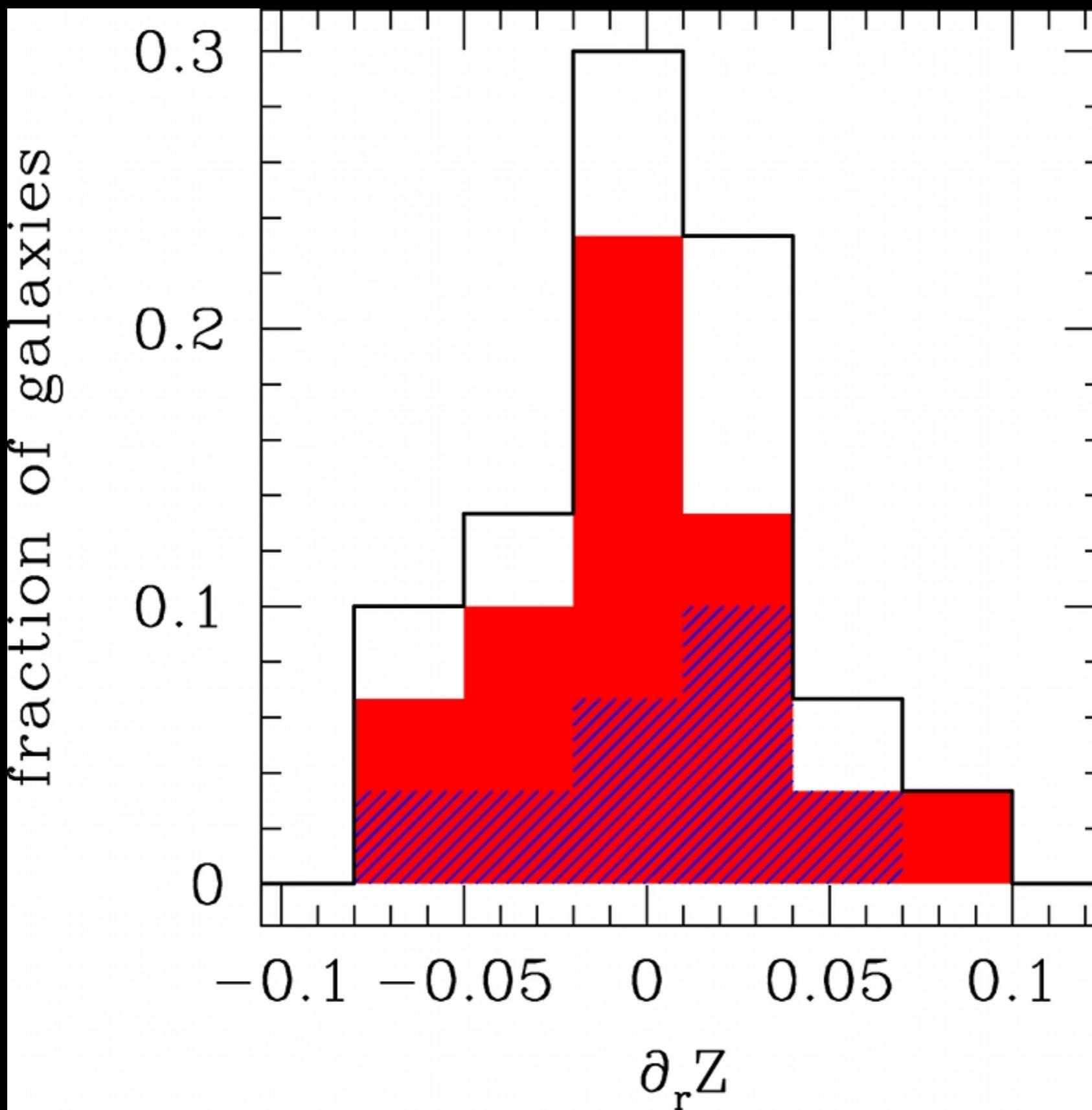
# Radial Metallicity Gradient Nearby Disk Galaxies



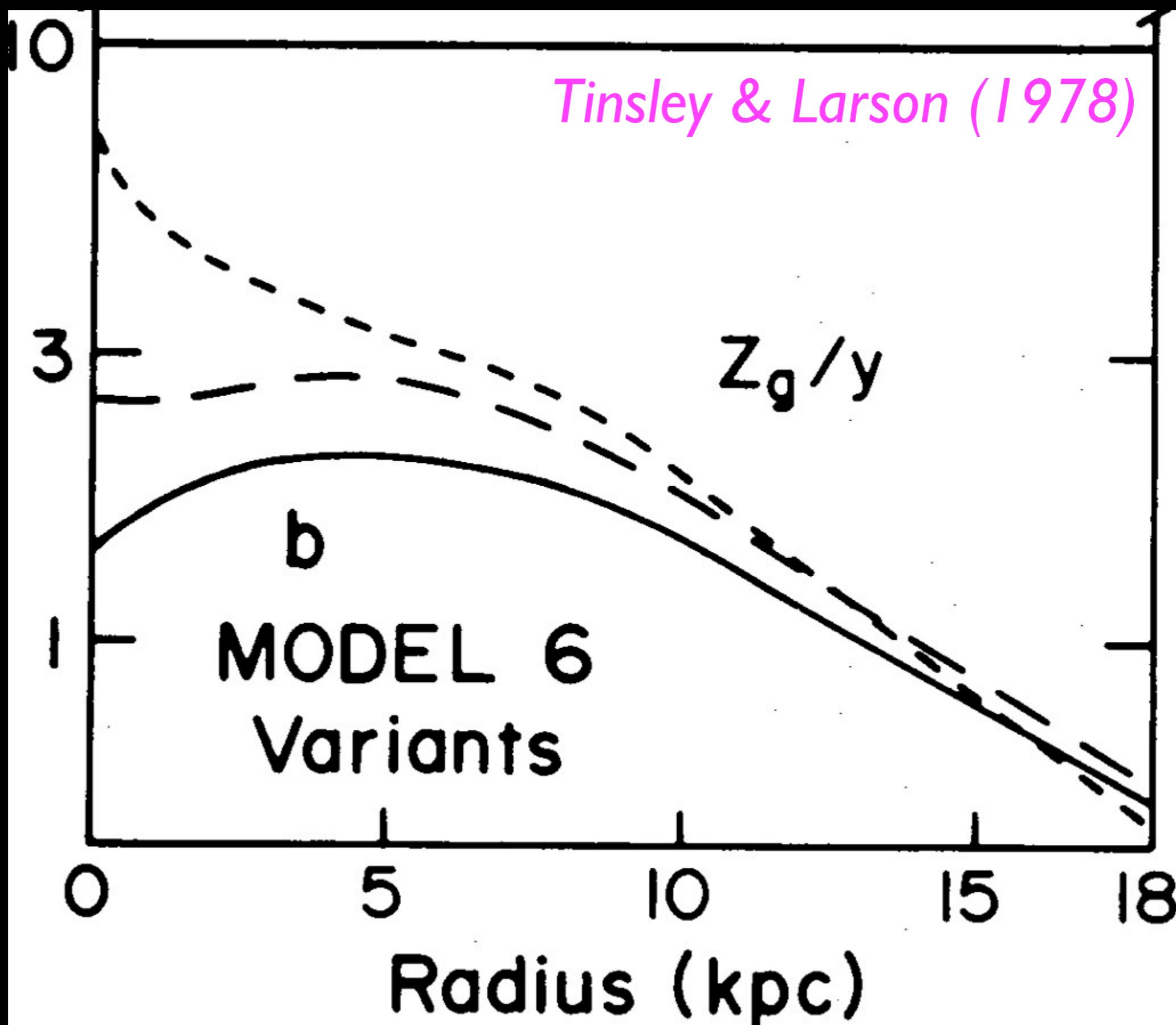
*Bresolin, Kennicutt, & Ryan-Weber (2012)*

# Radial Metallicity Gradient

## 26 MASSIV Galaxies at $z \sim 1.2$



# Failure of Closed-system Models



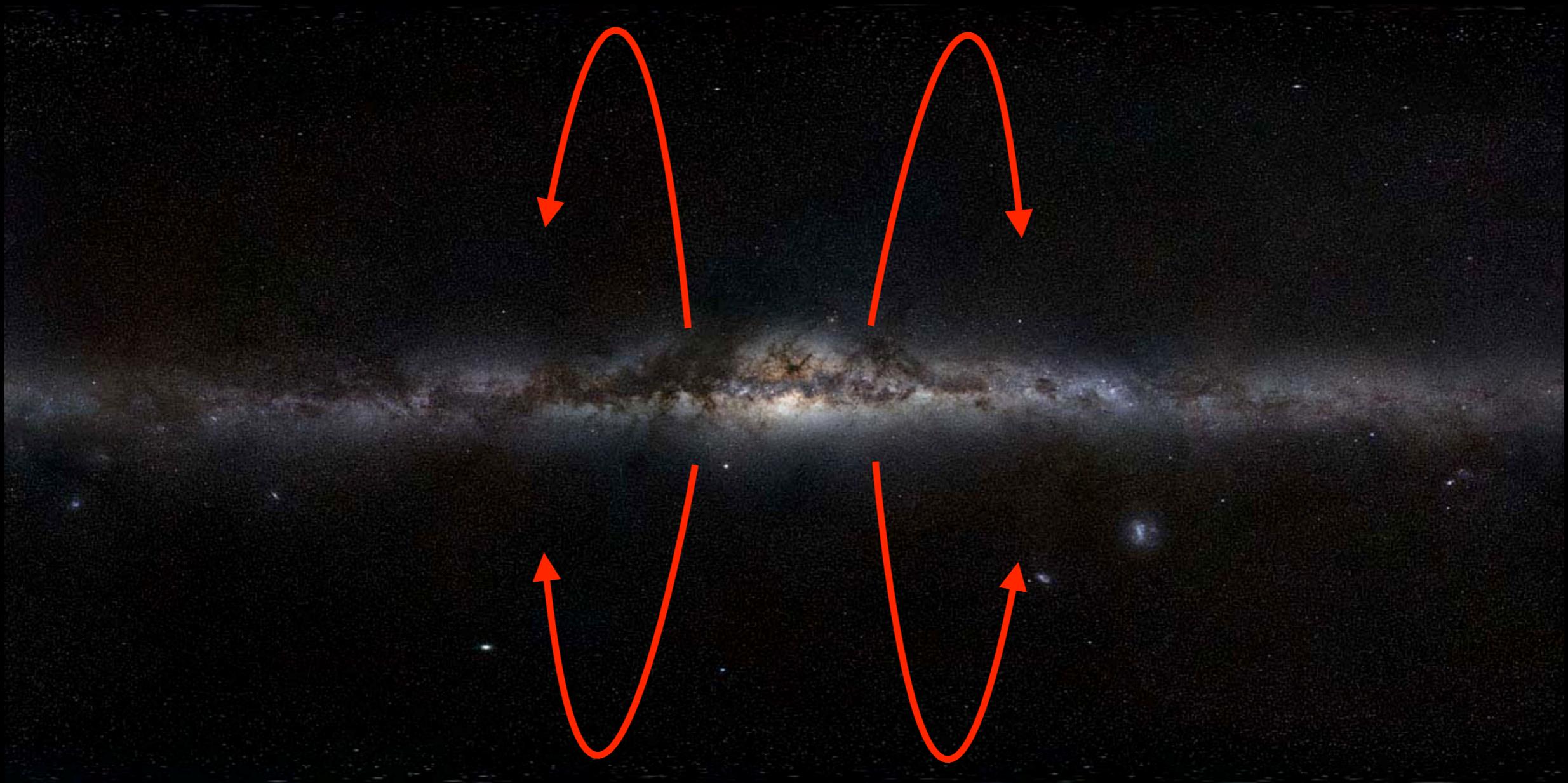
# What flattens metallicity gradients?



*Credit: S. Brunier*

# What flattens metallicity gradients?

Supernova-driven galactic fountains

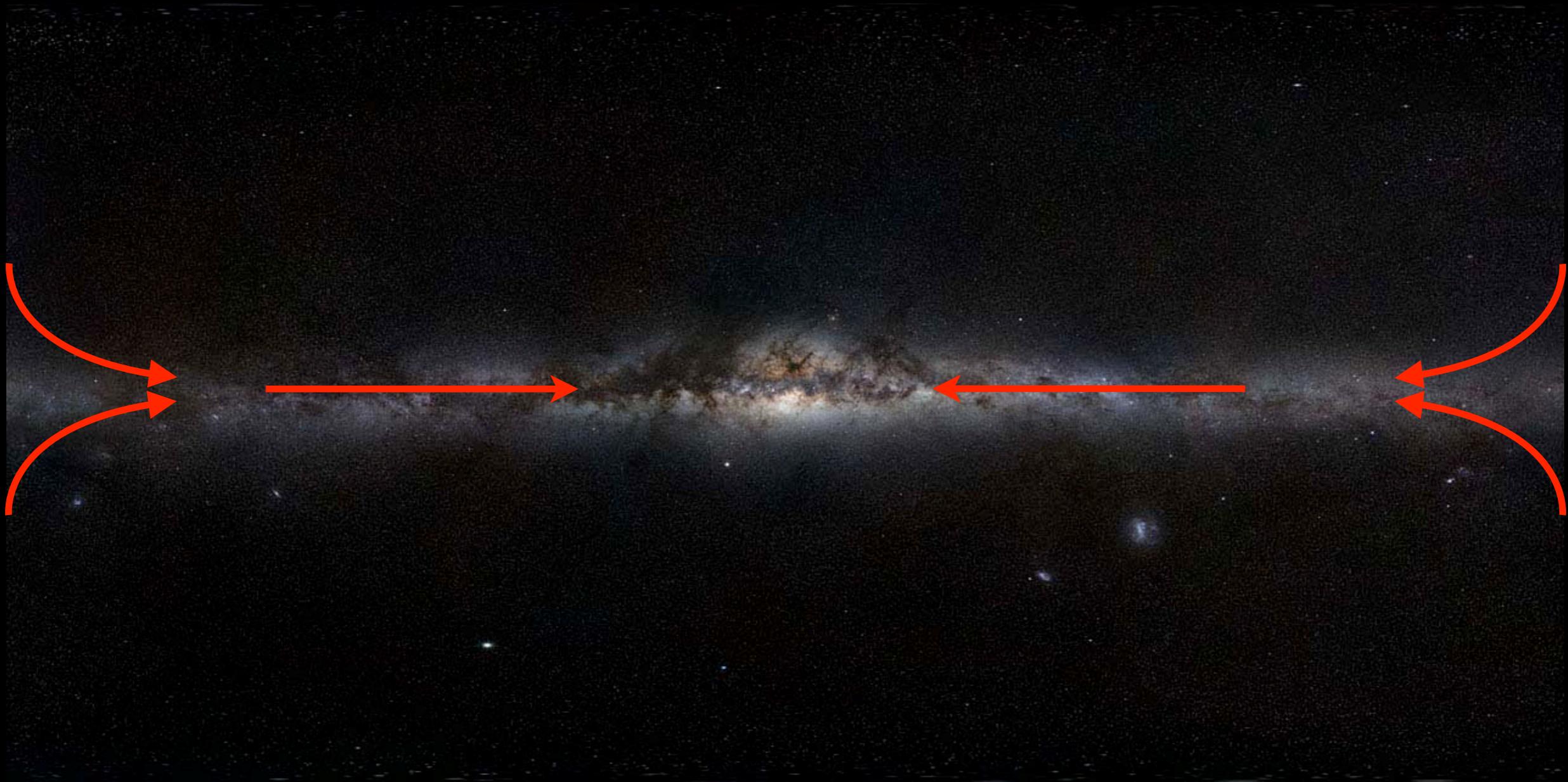


Credit: S. Brunier

e.g., Spitoni, Recchi, & Matteucci (2008); Spitoni et al. (2009)

# What flattens metallicity gradients?

Radial inflows within the disk

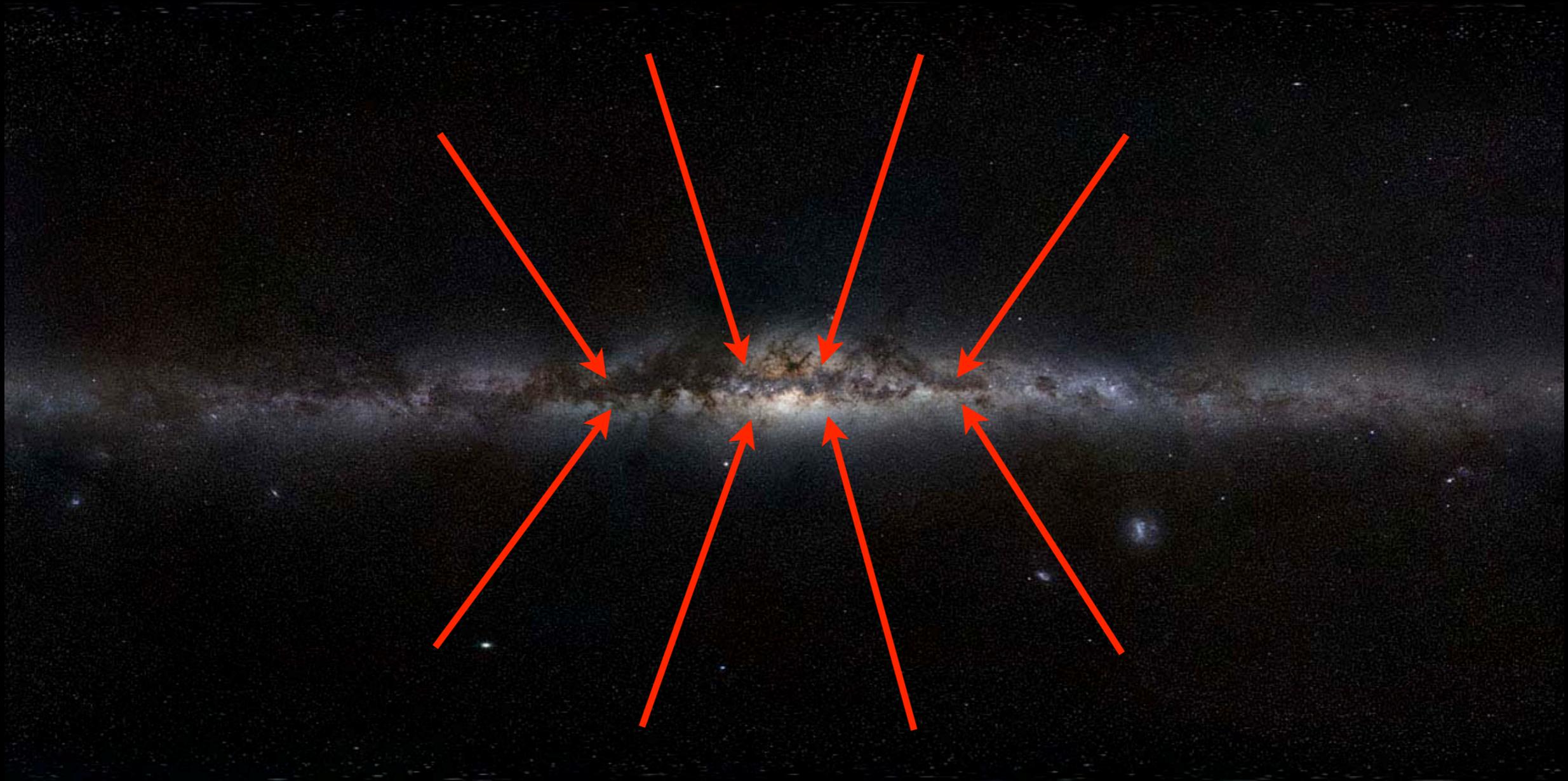


Credit: S. Brunier

Mayor & Vigroux (1981); Lacey & Fall (1985); Pitts & Tayler (1989)  
Götz & Köppen (1992); Portinari & Chiosi (2000)  
Spitoni & Matteucci (2011); Bilitewski & Schönrich (2012)

# What flattens metallicity gradients?

Accretion/infall from halo/circumgalactic medium

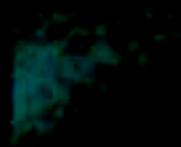


Credit: S. Brunier

Tinsley & Larson (1978); Chiosi (1980); Matteucci & François (1989)  
Chiappini et al. (1997, 2001); Prantzos & Boissier (2000)

# What flattens metallicity gradients?

Merger/interaction history



Credit: J. E. Barnes

Perez et al. (2006, 2011); Kewley et al. (2010); Rupke, Kewley, & Barnes (2010);  
Rupke, Kewley, & Chien (2010); Torrey et al., in prep.

# What flattens metallicity gradients?

Stellar radial migration

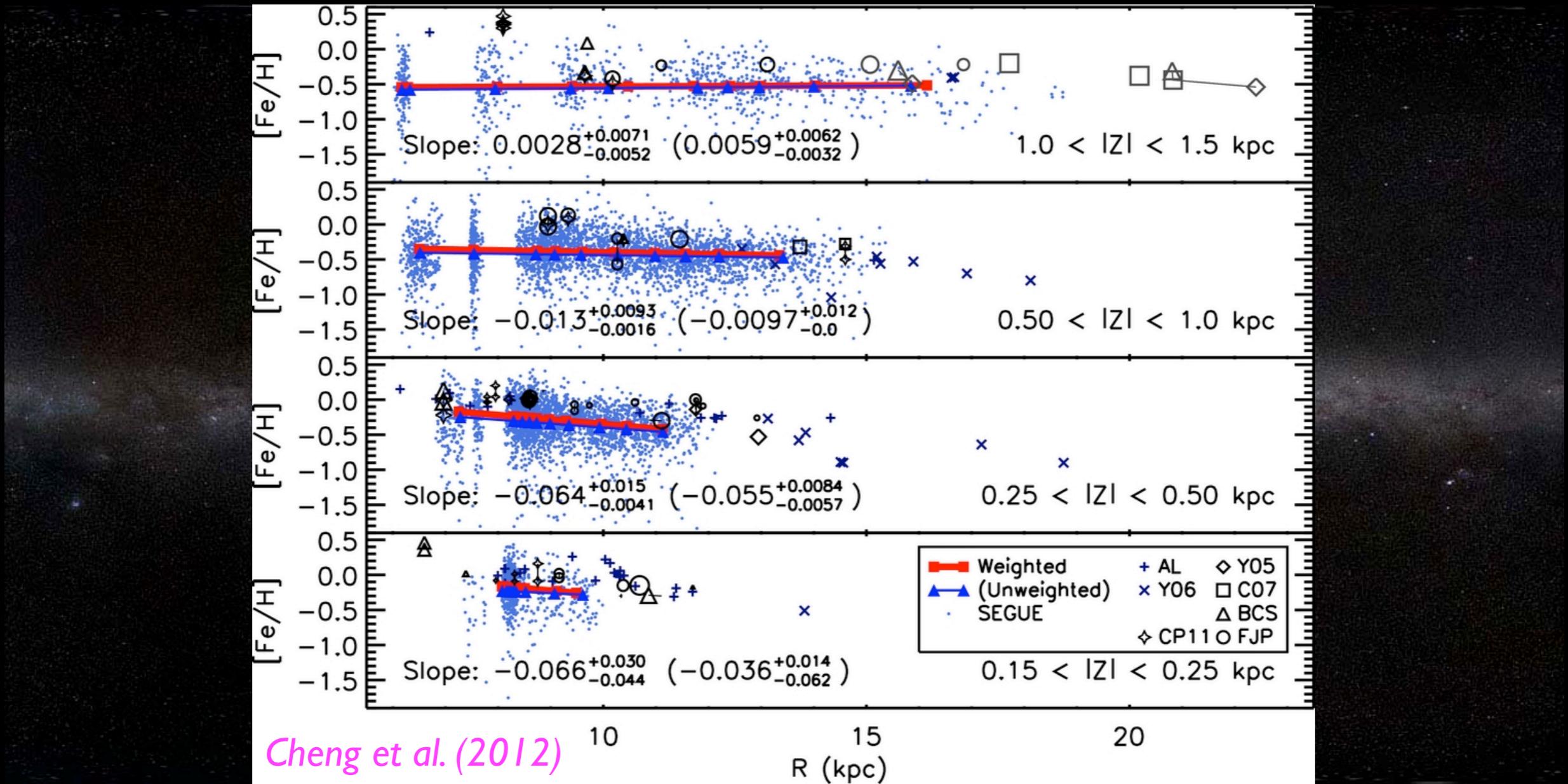


Credit: S. Brunier

Roškar et al. (2008a,b); Schönrich & Binney (2009)

# What flattens metallicity gradients?

## Stellar radial migration



Roškar et al. (2008a,b); Schönrich & Binney (2009)

# Turbulent Diffusion (?)

- Shakura & Sunyaev (1973)  $\alpha$ -prescription
  - Kinematic viscosity:  $\nu = \alpha c_s H$ ,  $0 < \alpha < 1$
  - Diffusion timescale:  $\tau \sim L^2 / \nu$
  - Typical galactic disks:  $c_s \sim 7$  km/s,  $H \sim 200$  pc
    - $\tau \sim (10 \text{ Gyr}) (\alpha / 10^{-2})^{-1}$  for  $L \sim 10$  kpc

# Turbulent Diffusion (?)

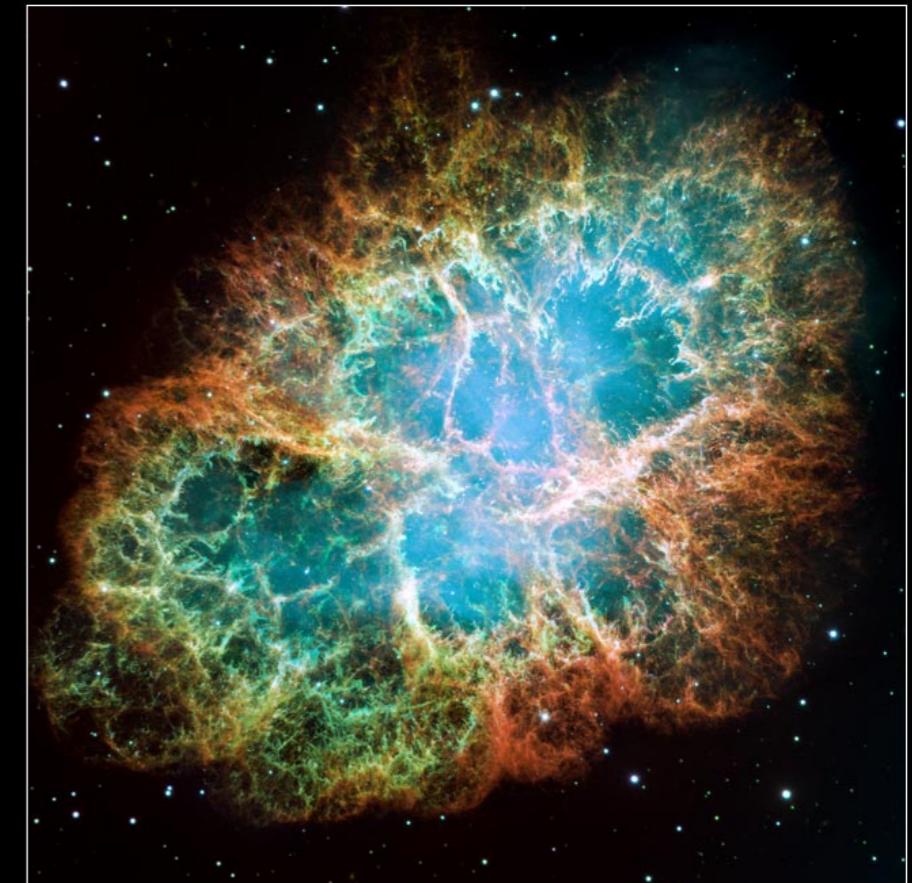
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    - $\tau \sim (10 \text{ Gyr}) (\alpha / 10^{-2})^{-1}$  for  $L \sim 10$  kpc
- *Is that so?*

# Driving Turbulence in the Interstellar Medium

- Supernova explosions
  - Rayleigh-Taylor instability
- Gravitational instability
- Magneto-rotational instability
- *Thermal instability*

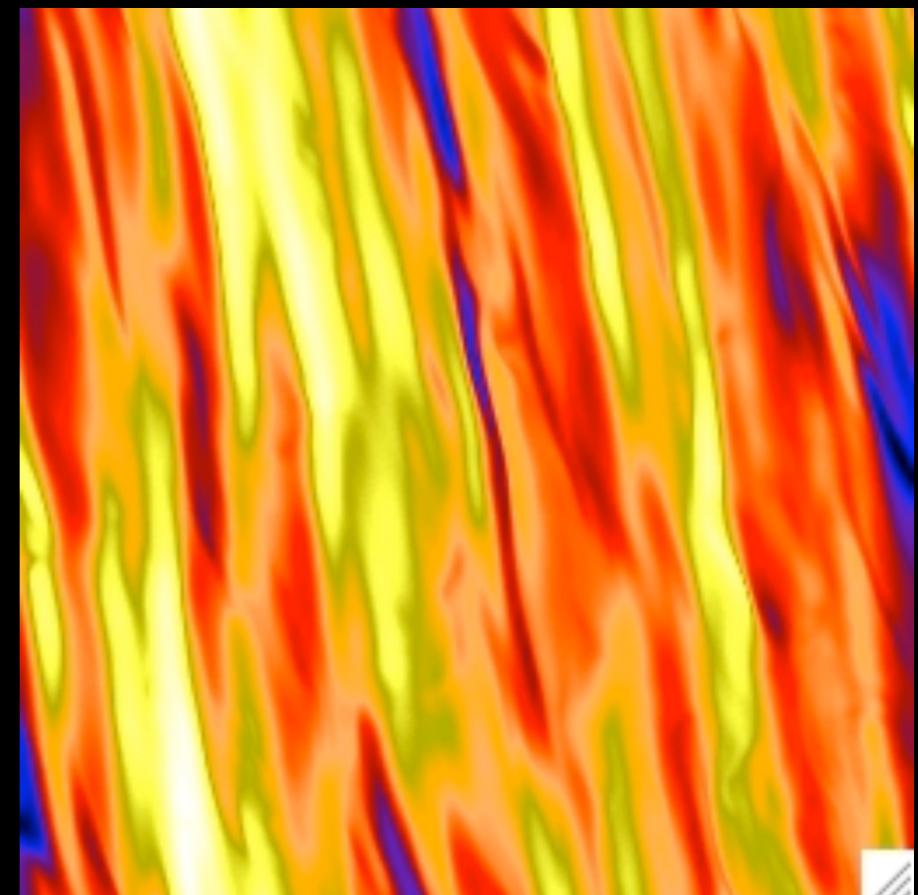
Crab Nebula • M1

HST • WFPC2

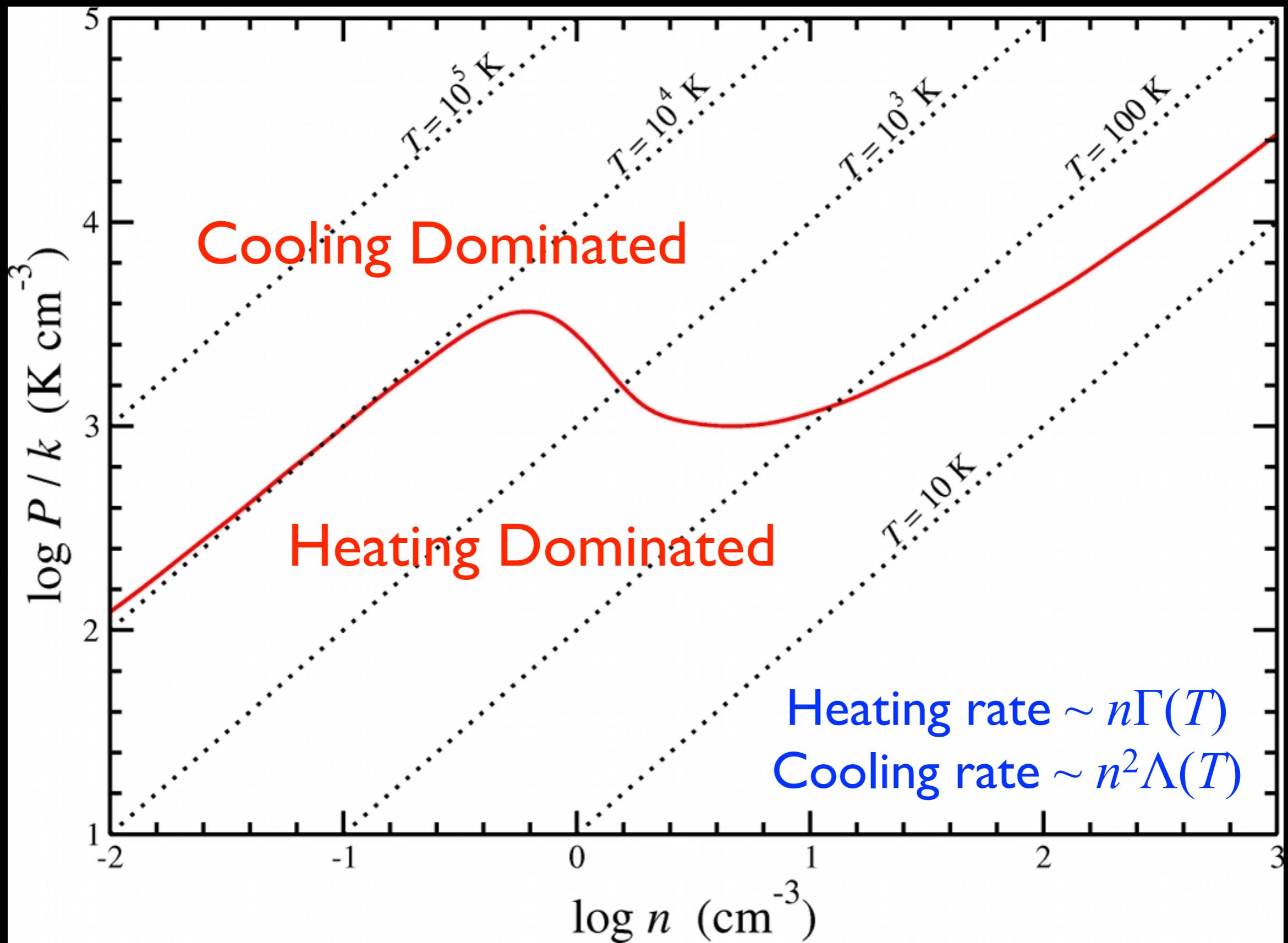


NASA, ESA, and J. Hester (Arizona State University)

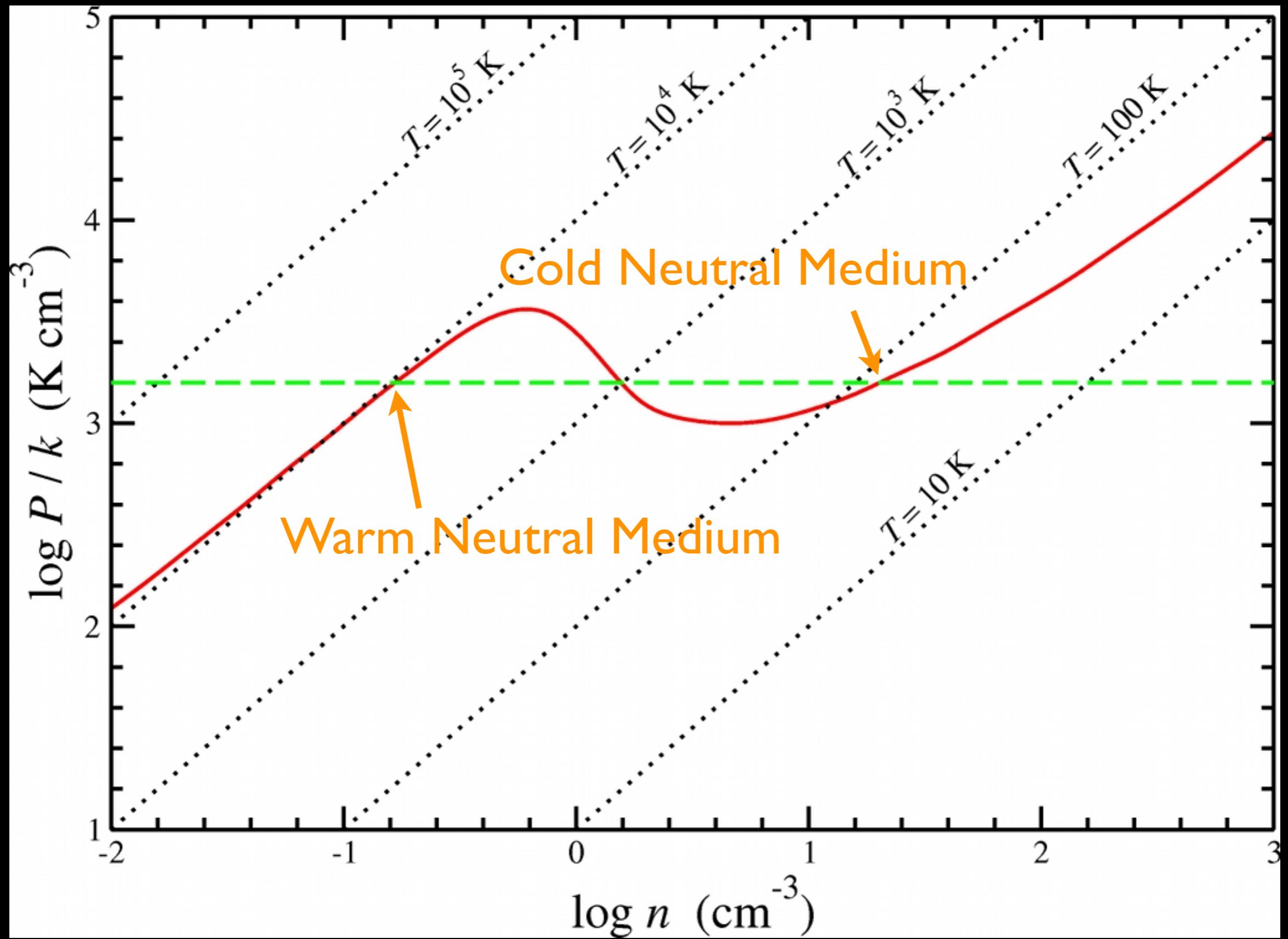
STScI-PRC05-37



# Two-phase Model for the ISM



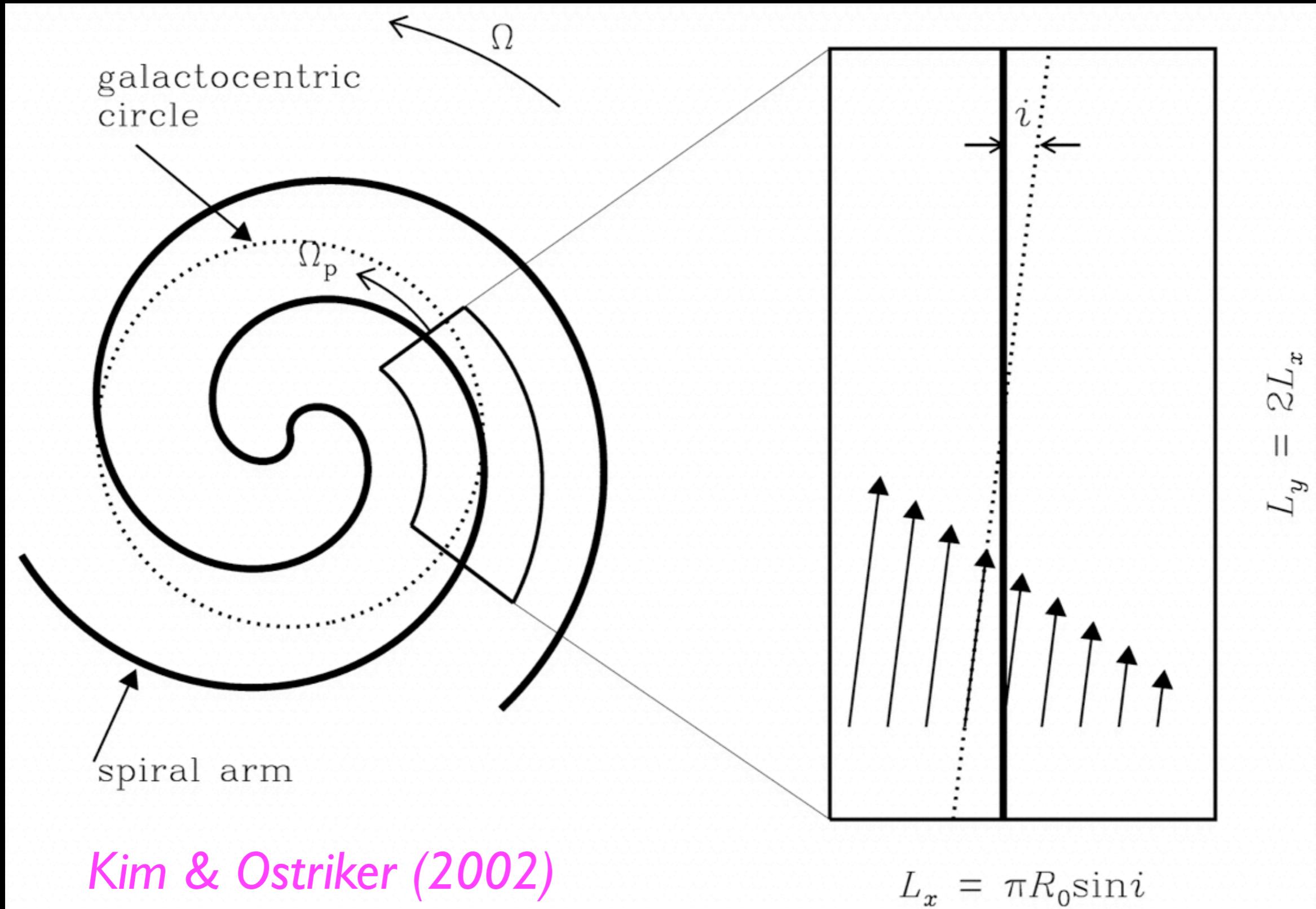
# Two-phase Model for the ISM



M51

[HTTP://CHANDRA.HARVARD.EDU](http://chandra.harvard.edu)

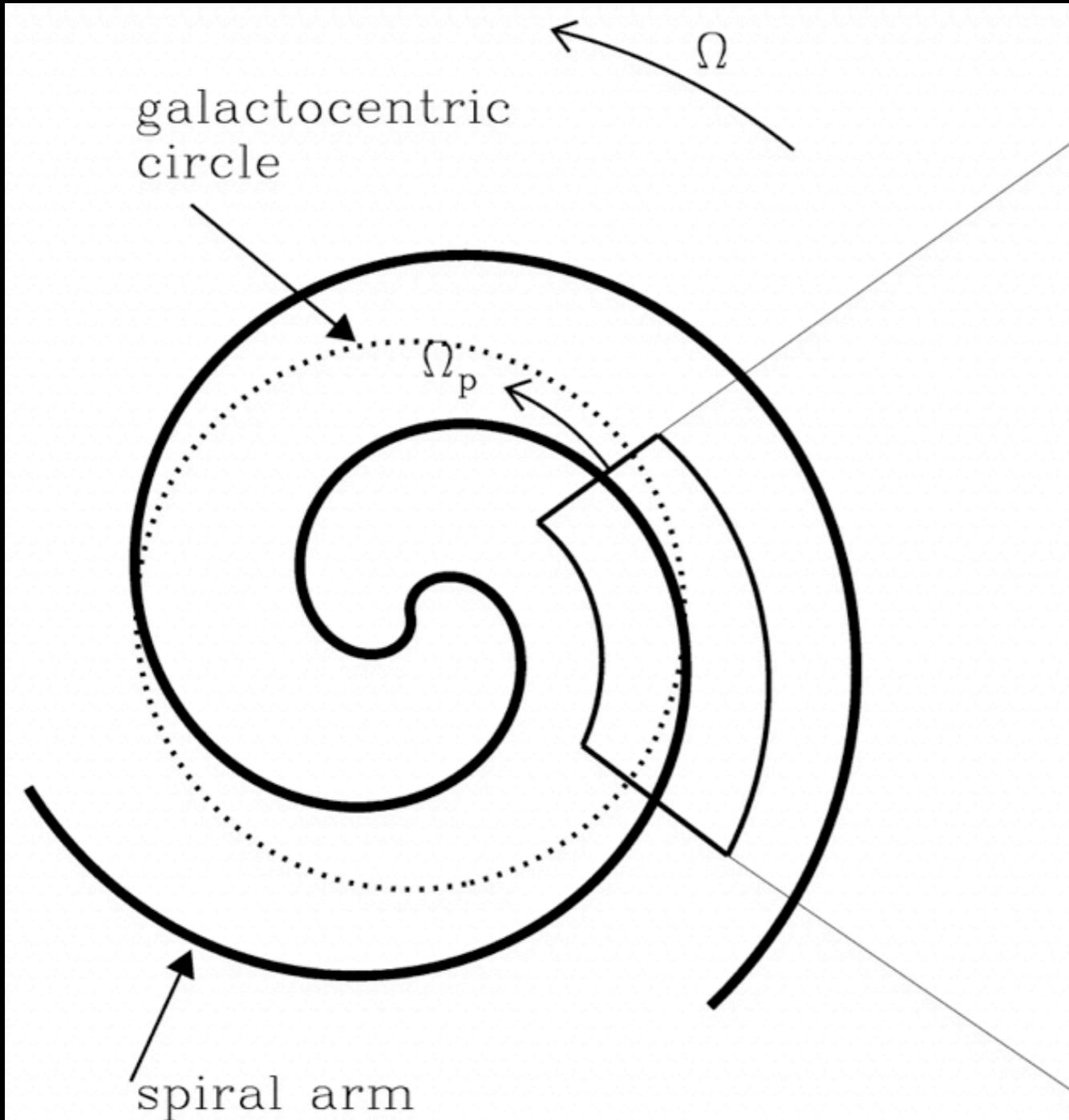
# Local Shearing Sheet for a Thin Gas Disk



Kim & Ostriker (2002)

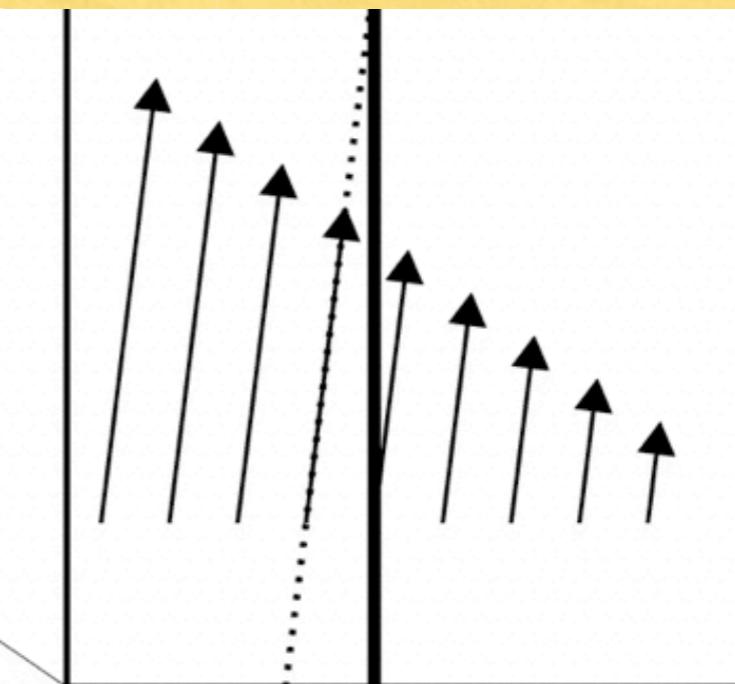
$$L_x = \pi R_0 \sin i$$

# Local Shearing Sheet for a Thin Gas Disk



Three physical effects to consider:

1. Thermal instability;
2. Spiral forcing;
3. Magnetic fields.



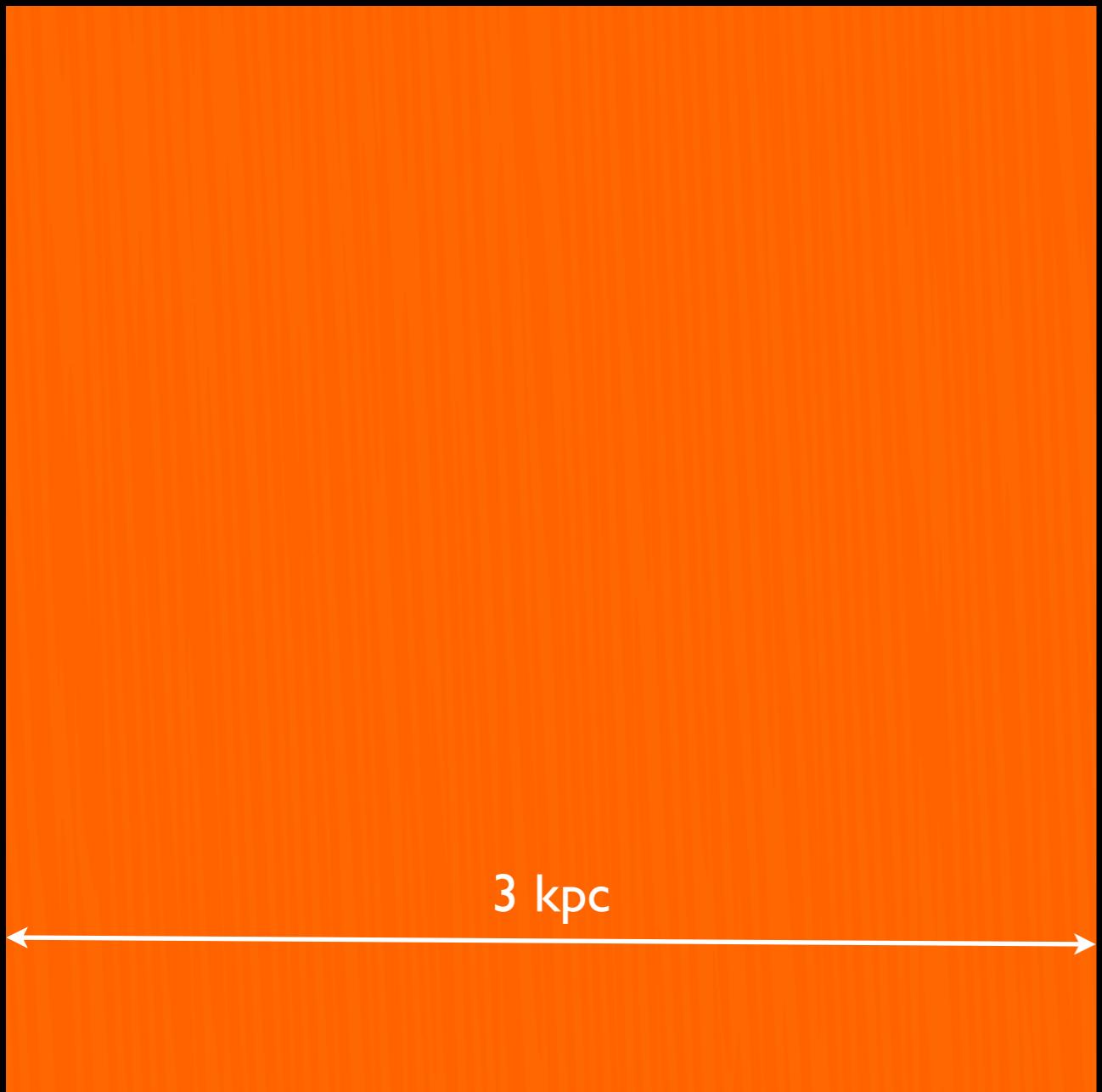
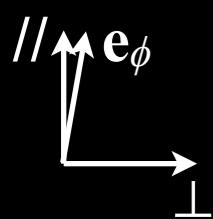
$$L_y = 2L_x$$

# Turbulent Steady State

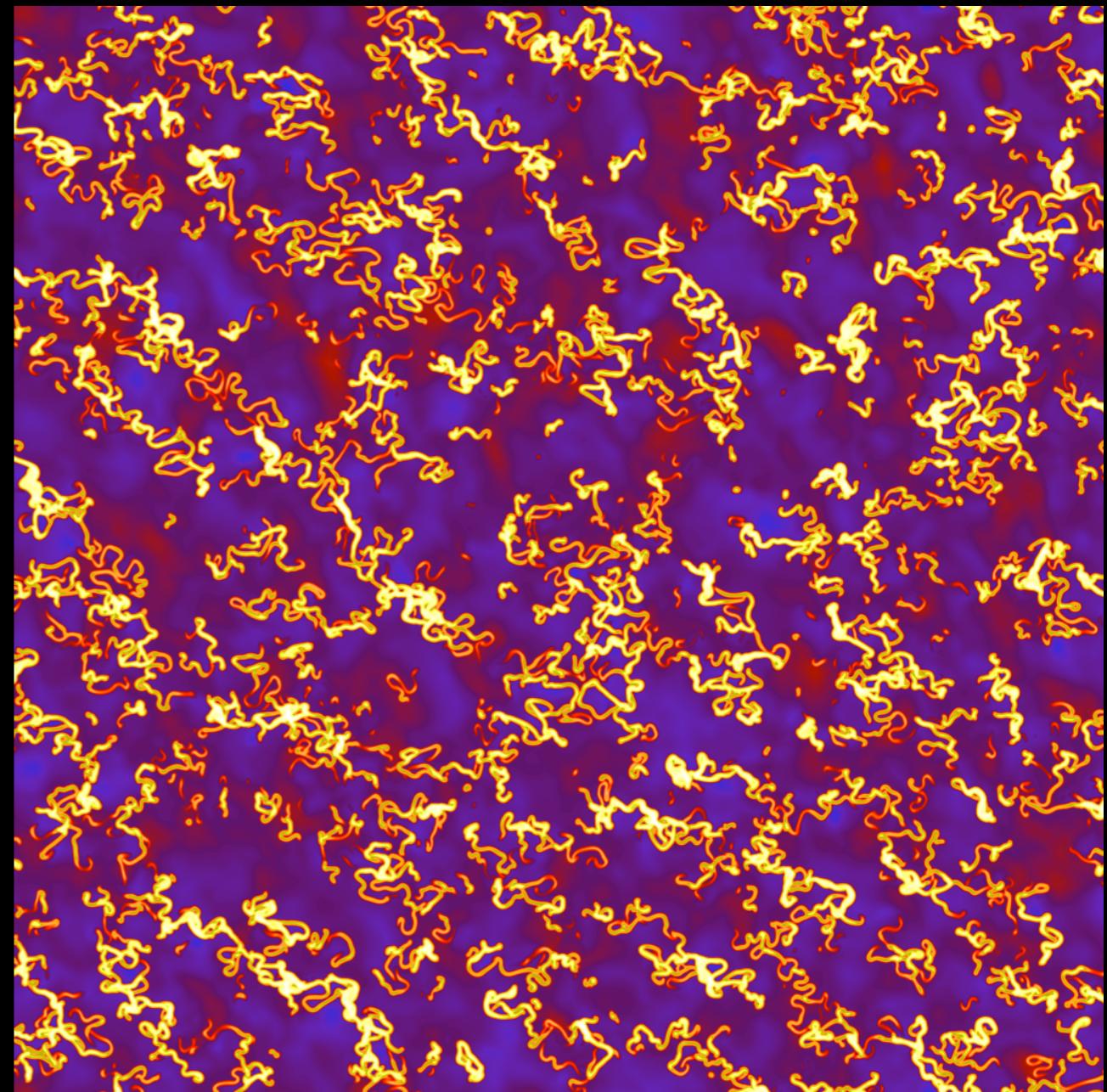
Spiral Forcing

Magnetic Fields

Surface Density



Isothermal



Thermally Unstable

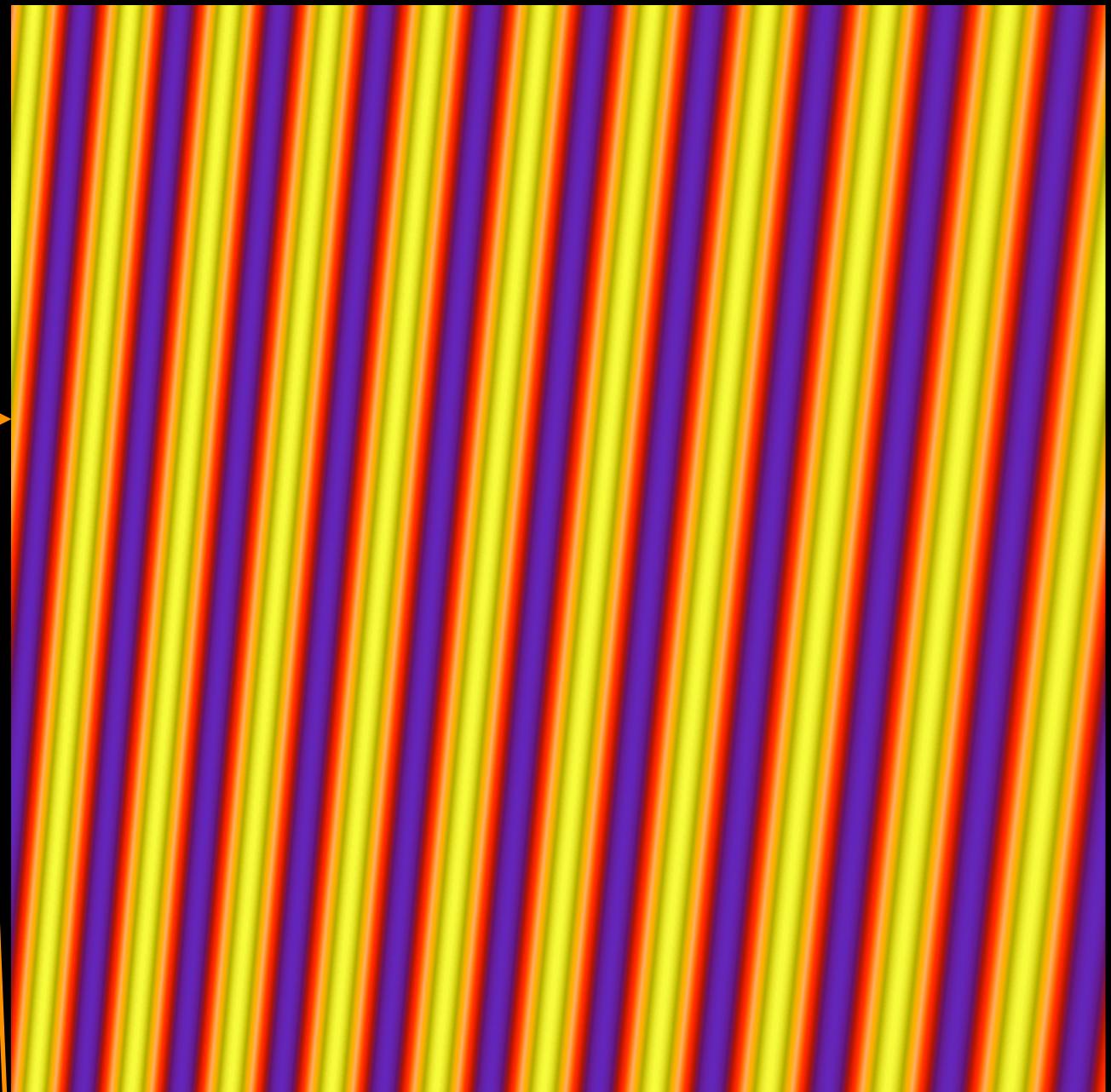
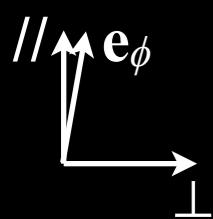
Yang & Krumholz (2012)

# Turbulent Steady State

Spiral Forcing

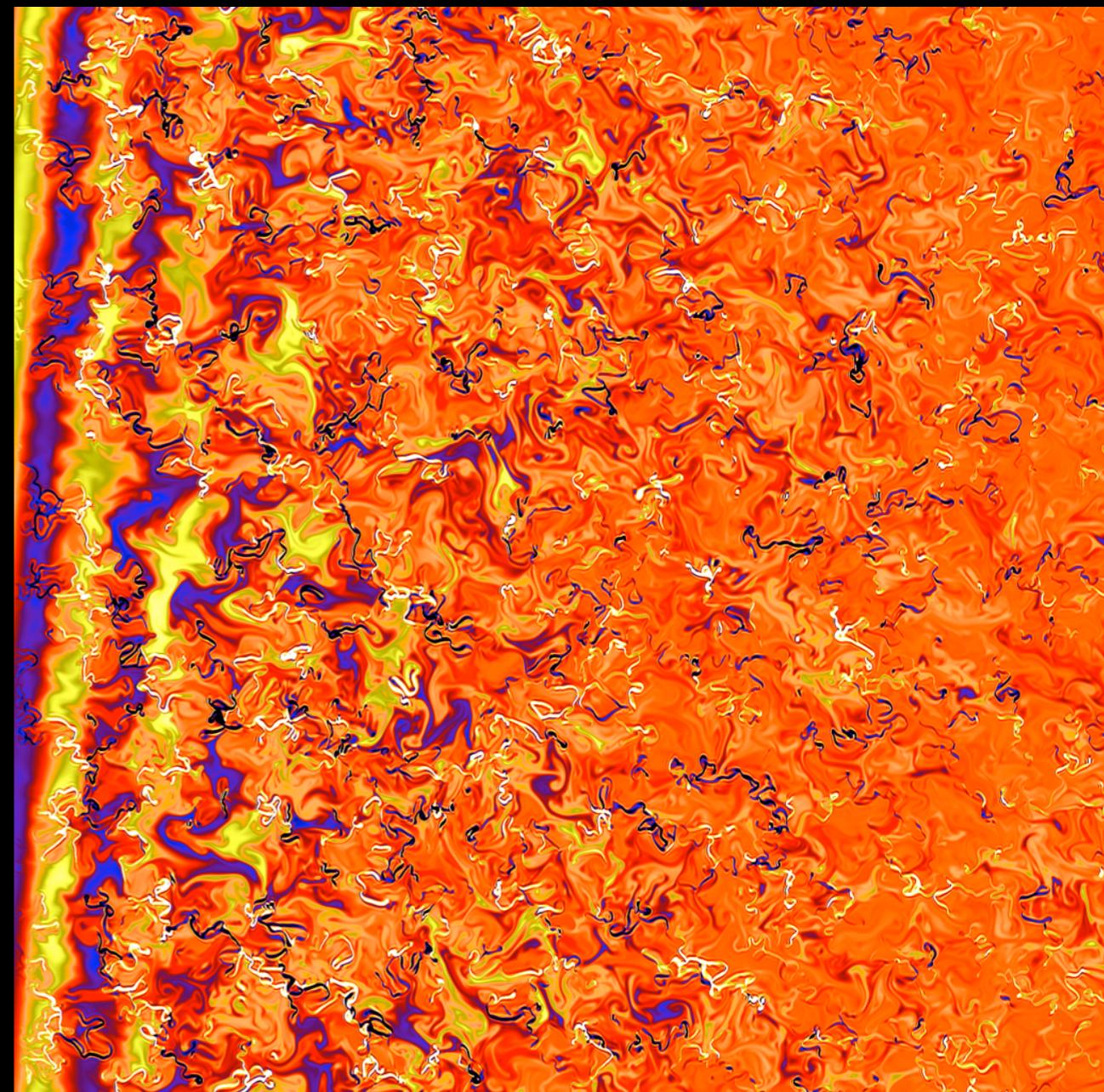
Magnetic Fields

Metal Tracer Field



Isothermal

Metal Injection Layer



Thermally Unstable

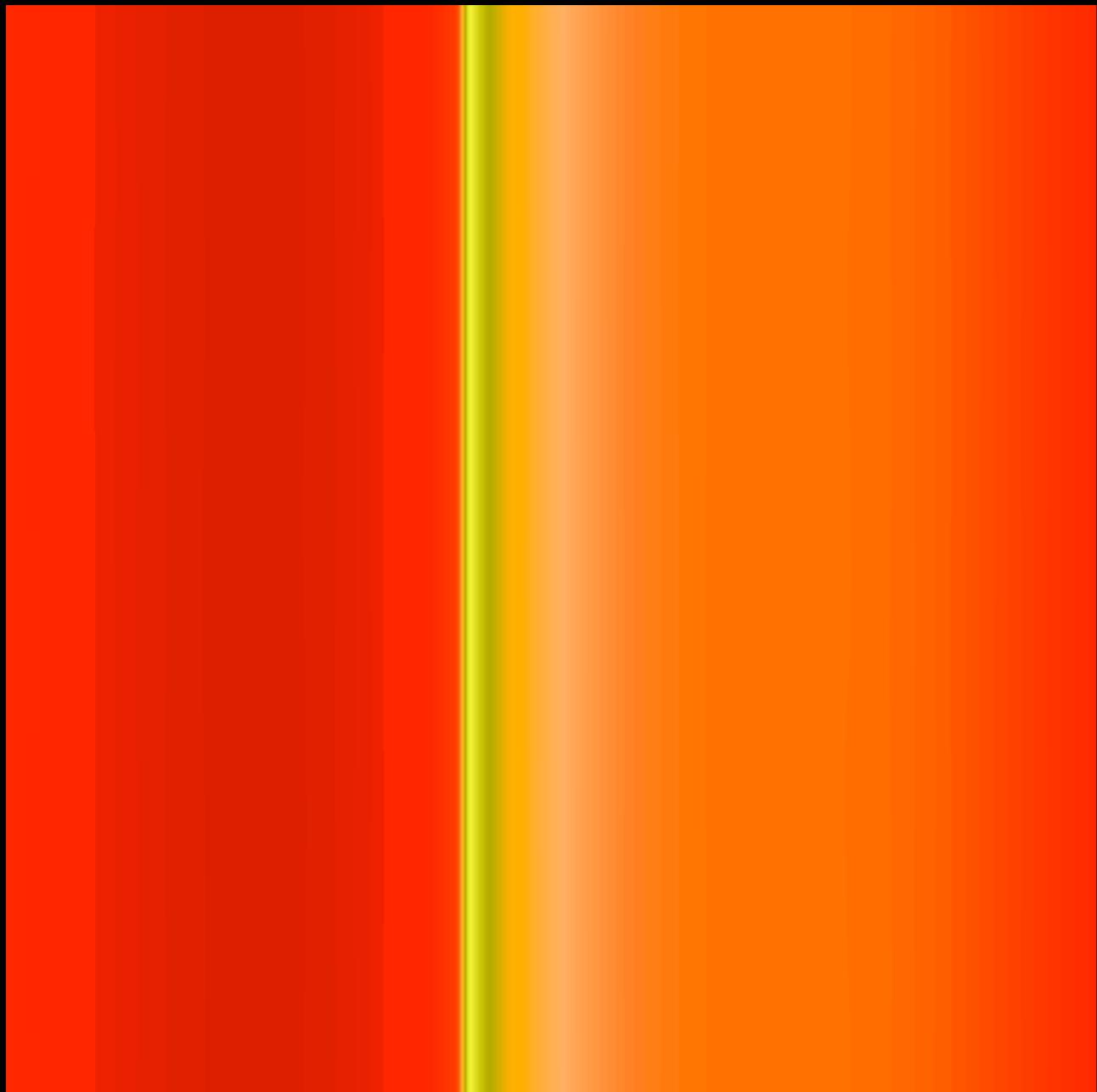
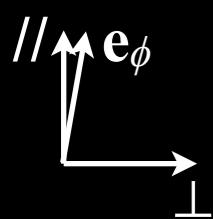
Yang & Krumholz (2012)

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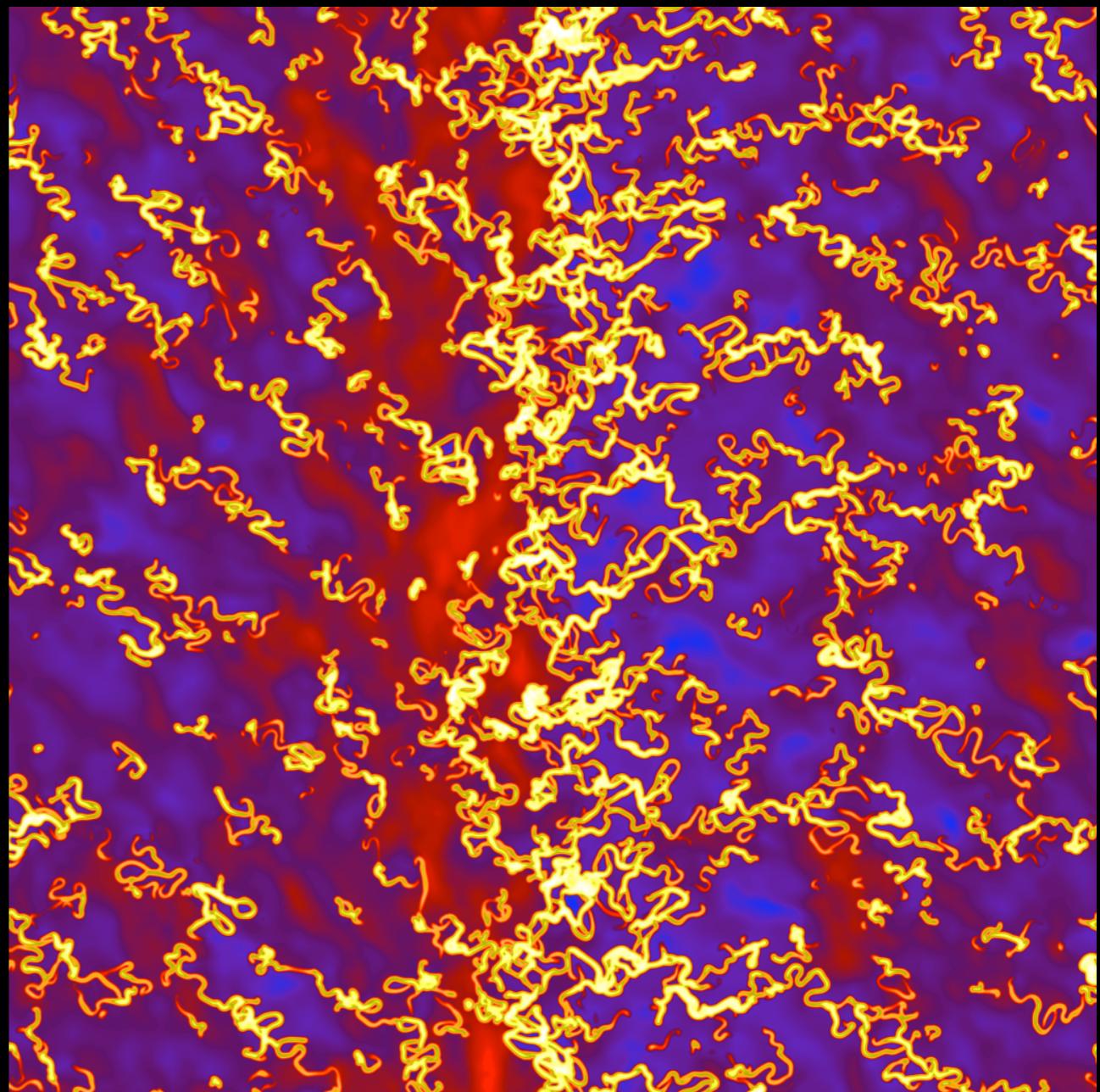
Spiral Forcing

Magnetic Fields

Surface Density



Isothermal



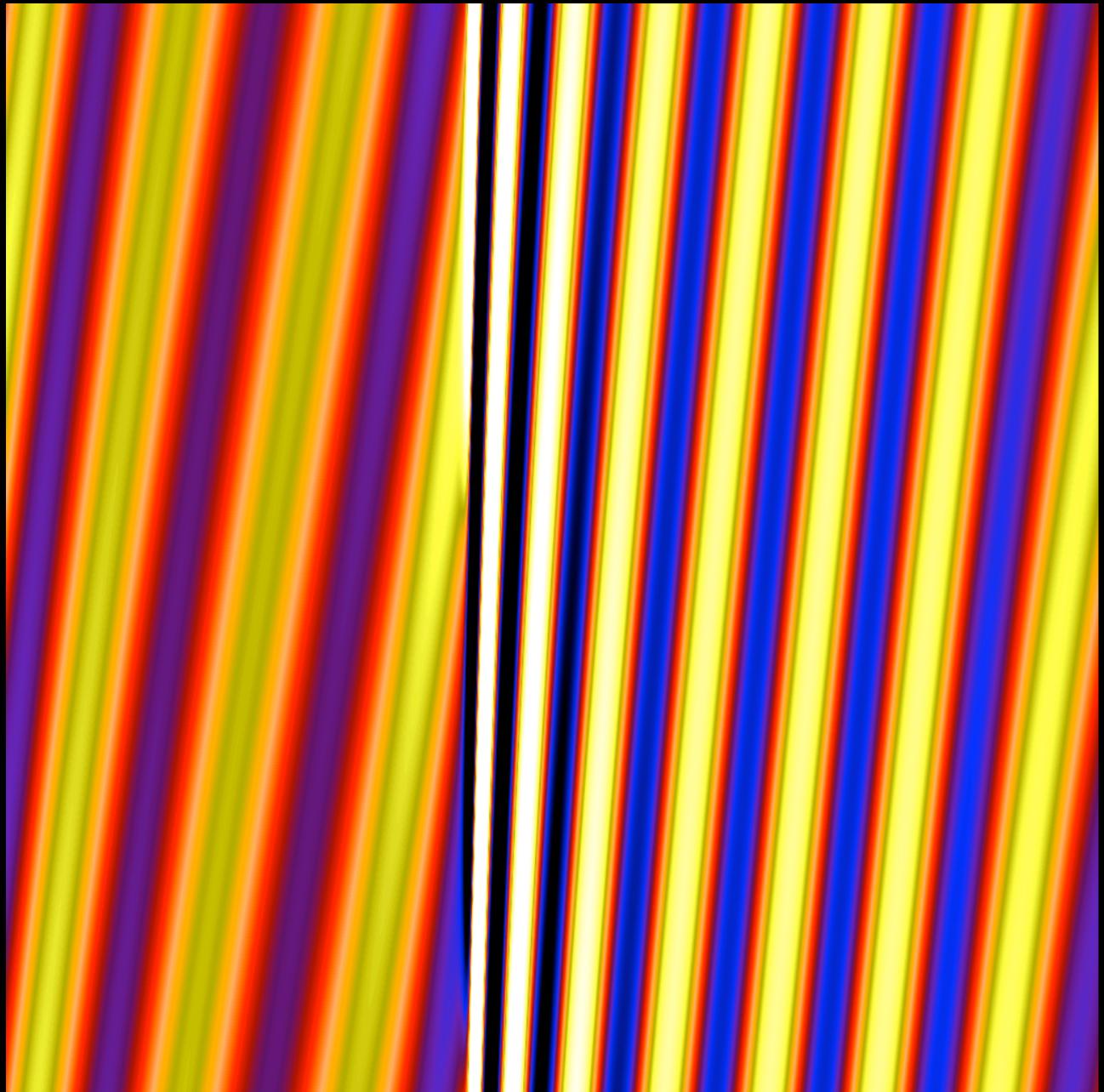
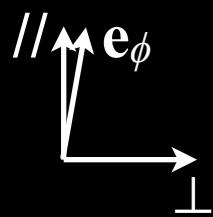
Thermally Unstable

# Turbulent Steady State

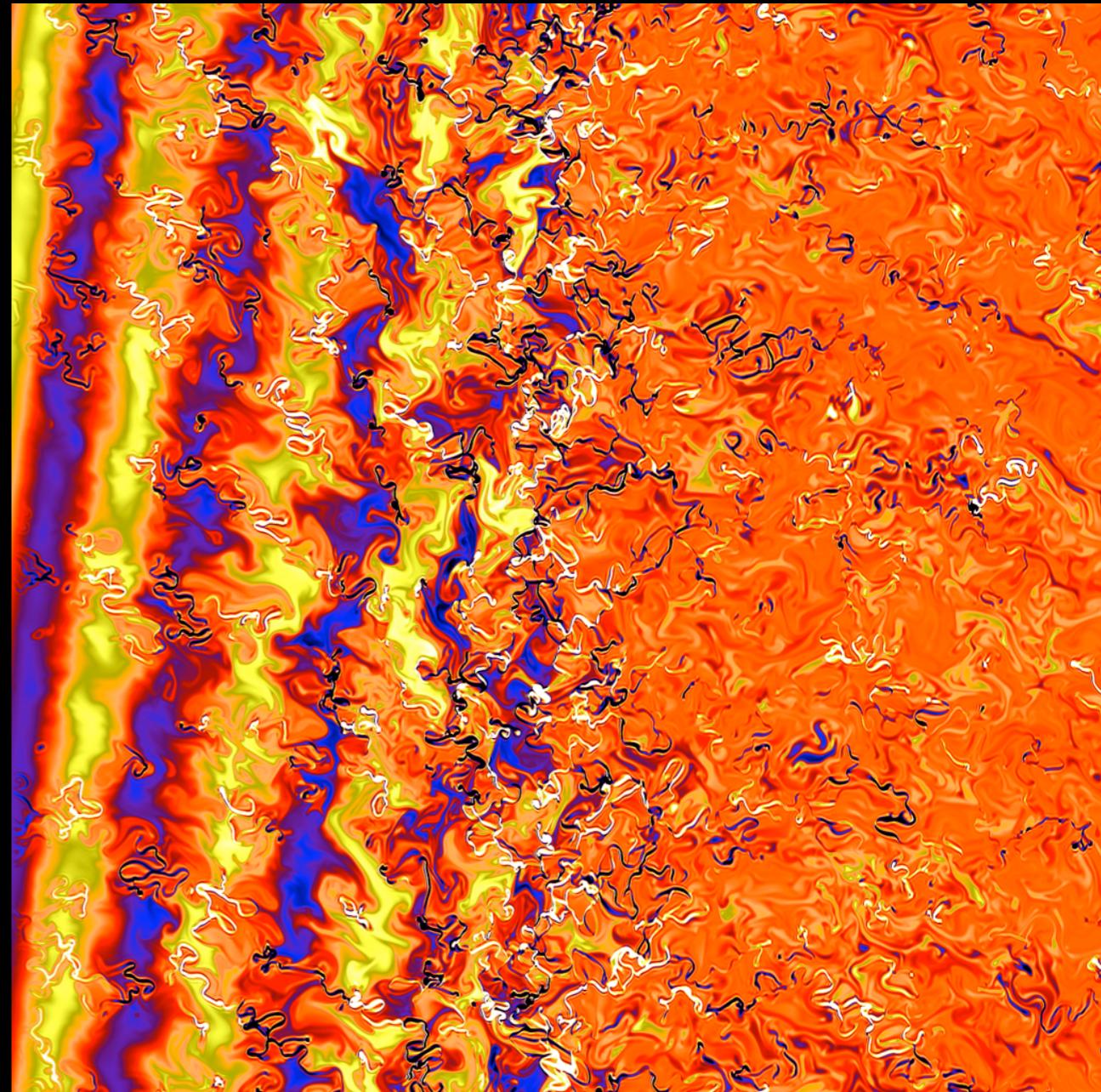
Spiral Forcing

Magnetic Fields

Metal Tracer Field



Isothermal



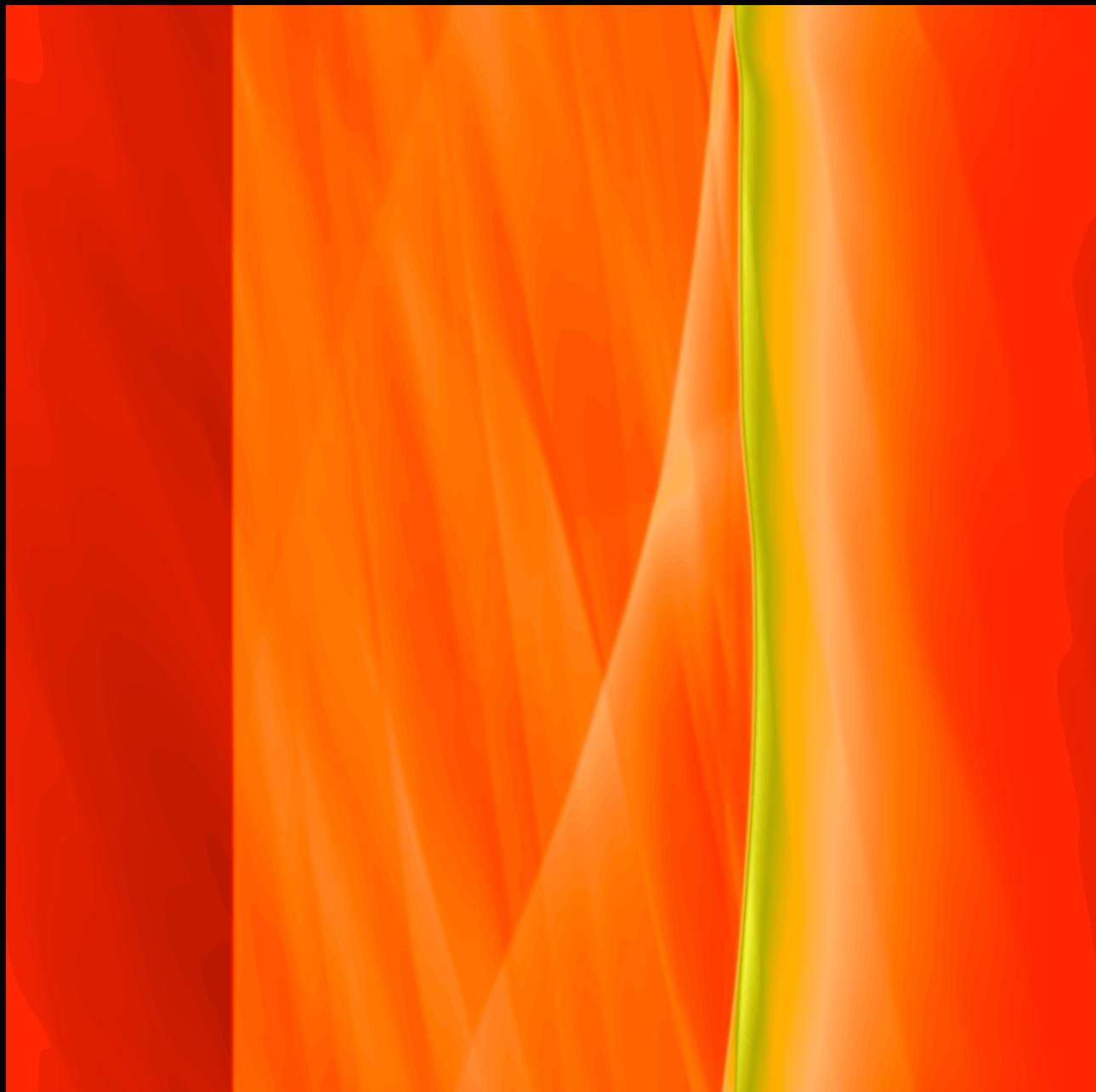
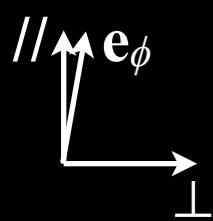
Thermally Unstable

# Turbulent Steady State

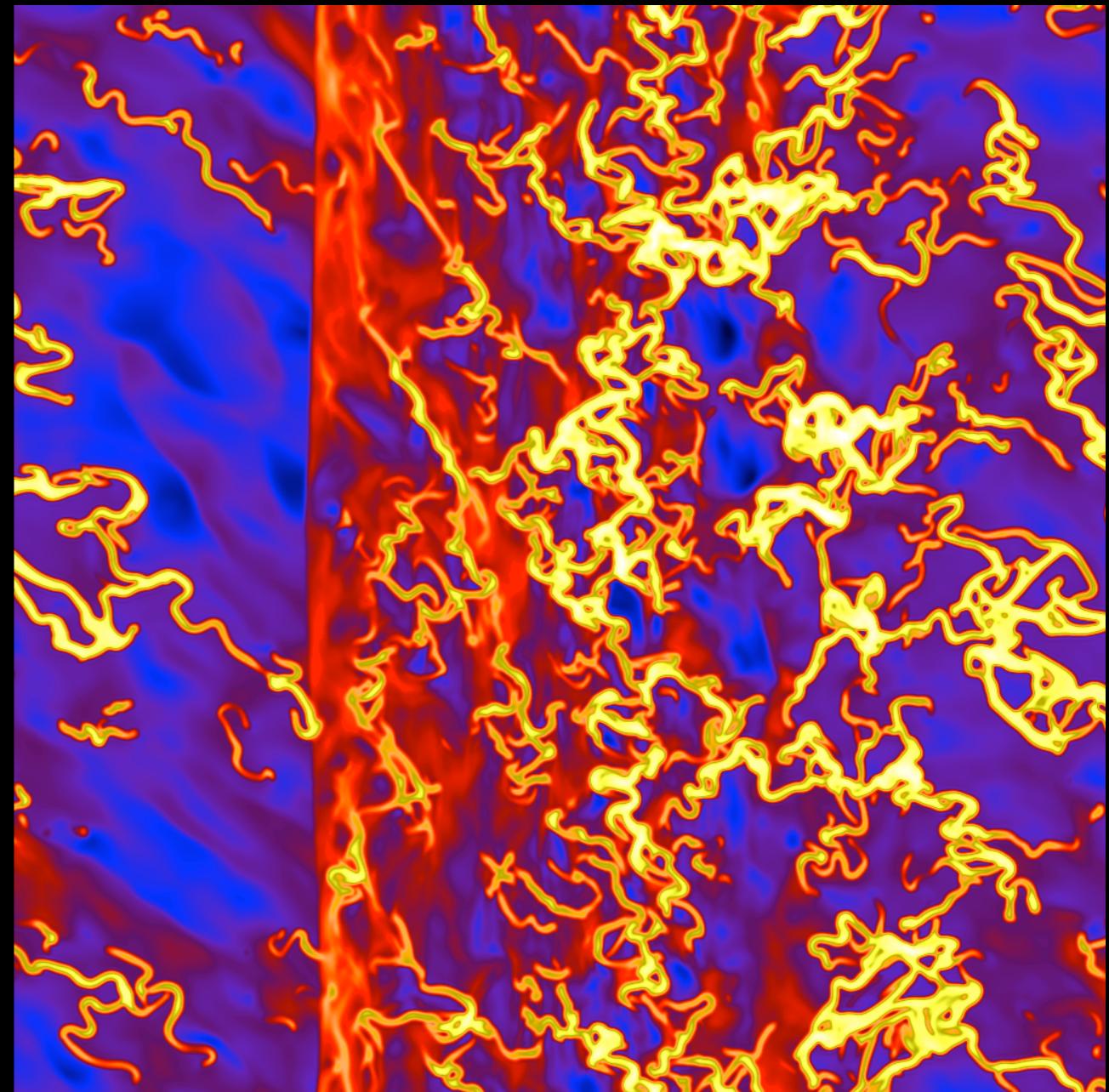
Spiral Forcing

Magnetic Fields

Surface Density



Isothermal



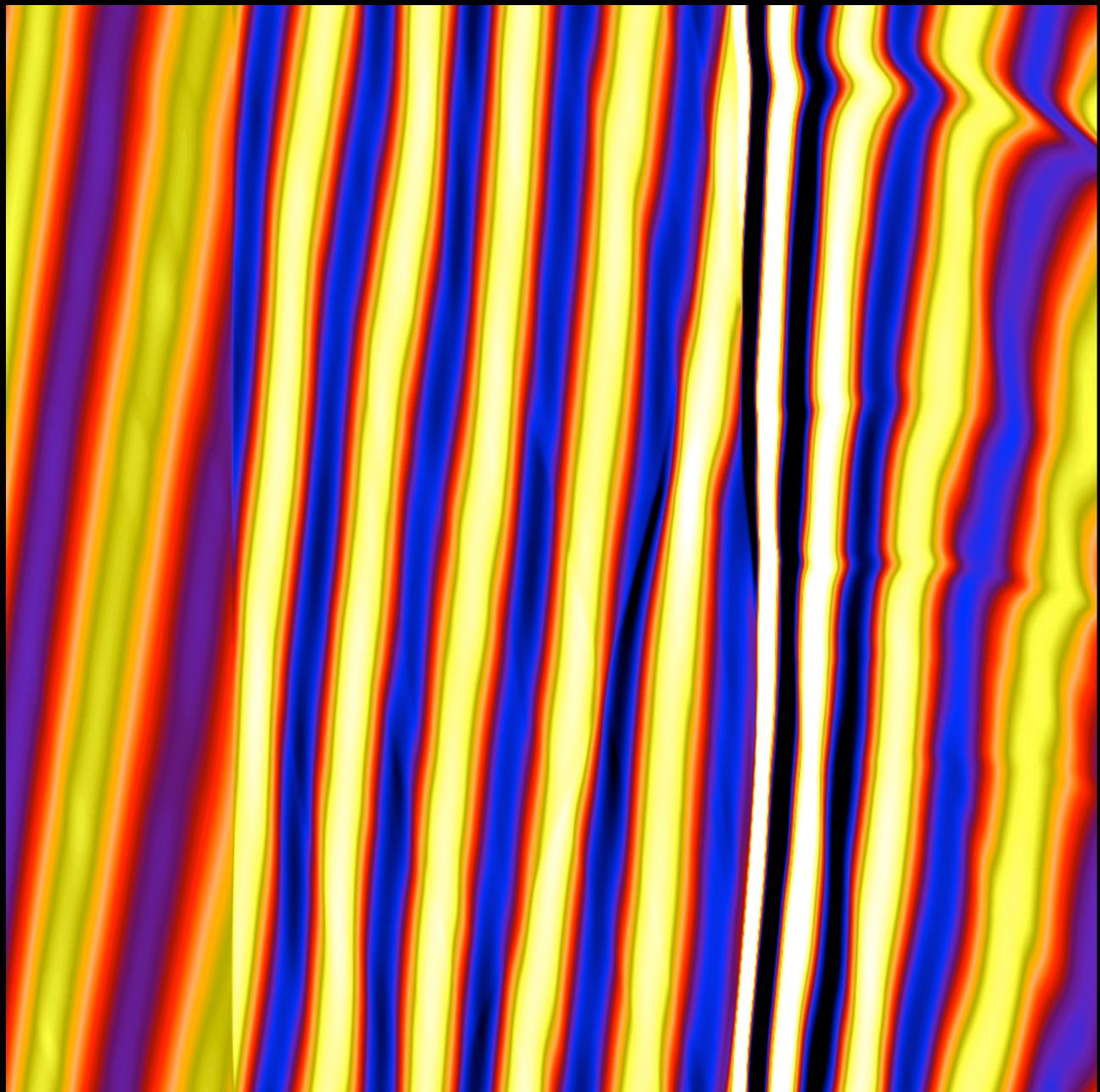
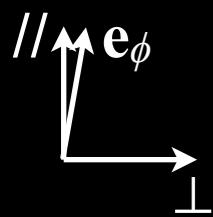
Thermally Unstable

# Turbulent Steady State

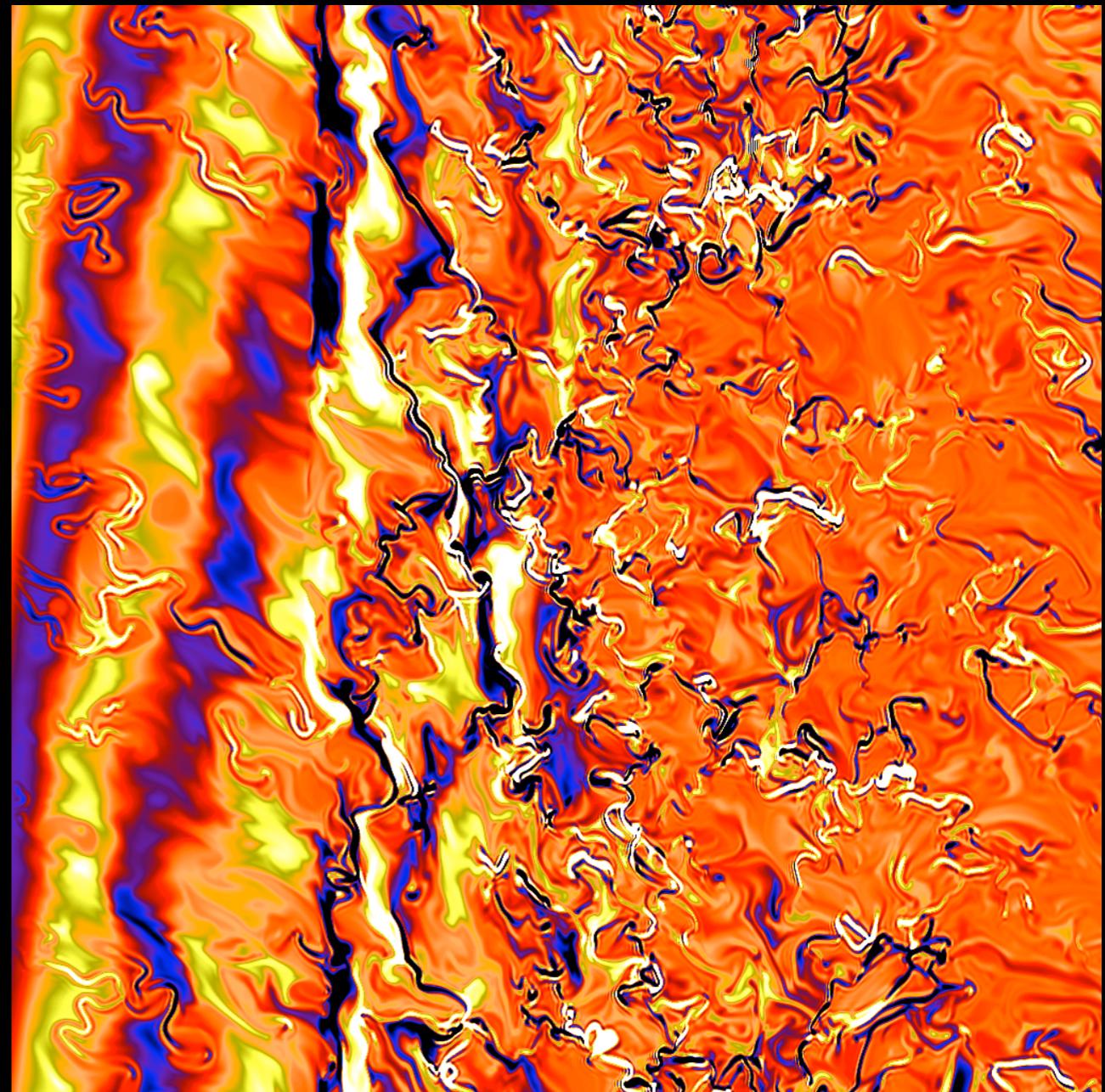
Spiral Forcing

Magnetic Fields

Metal Tracer Field

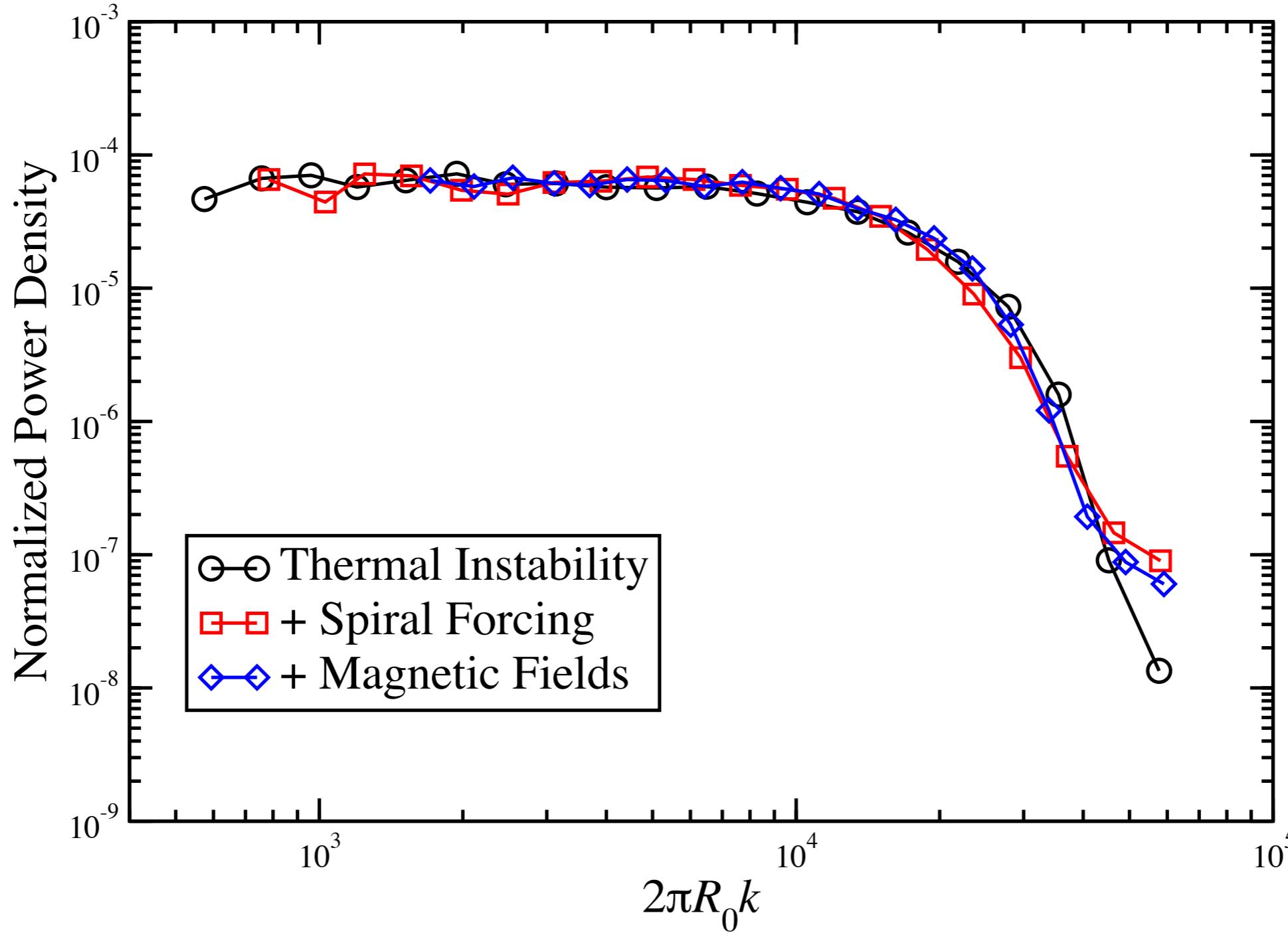


Isothermal



Thermally Unstable

# Power Spectrum of Mixed Metals

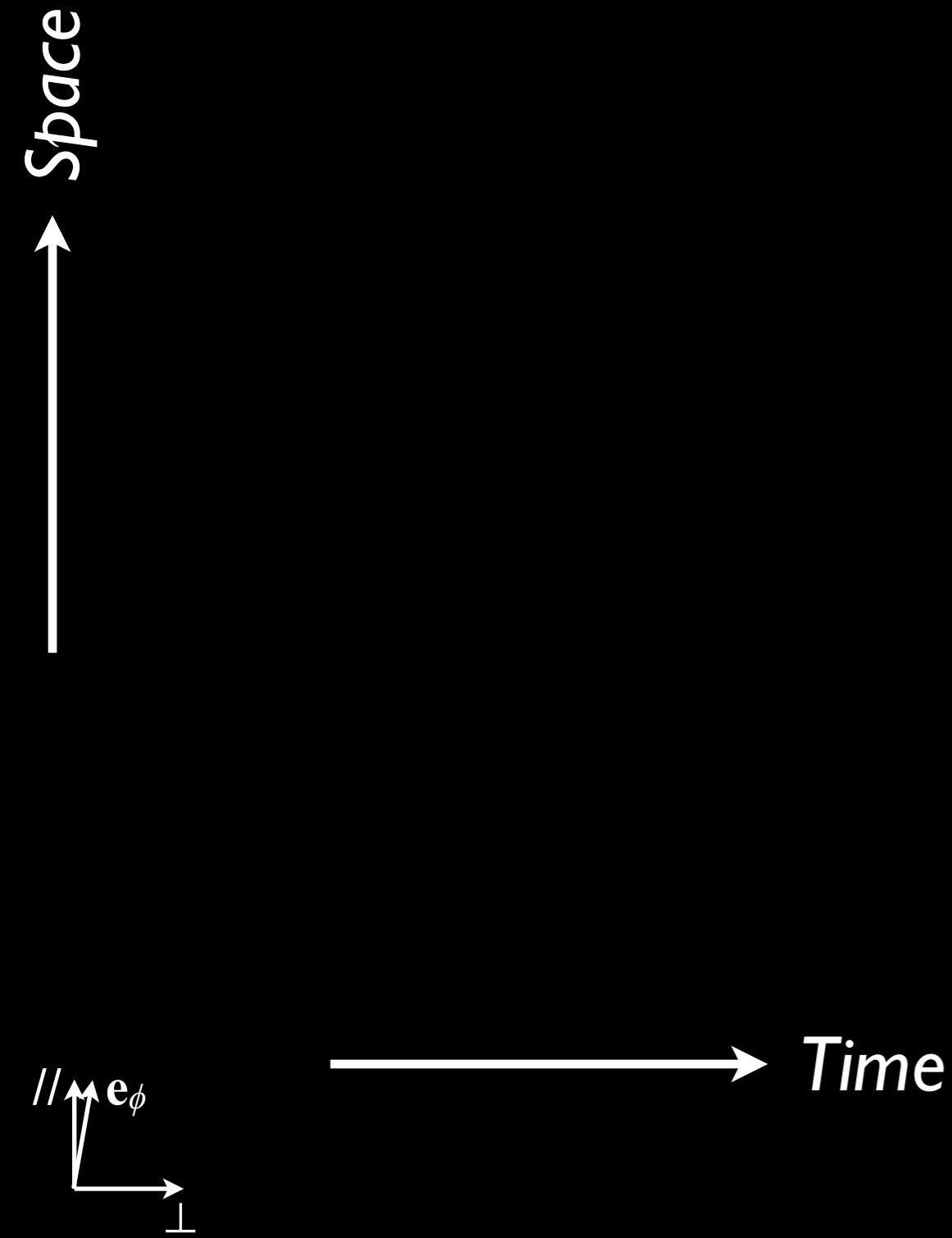


Yang & Krumholz (2012)

# Following the Flow

Metal Tracer Field

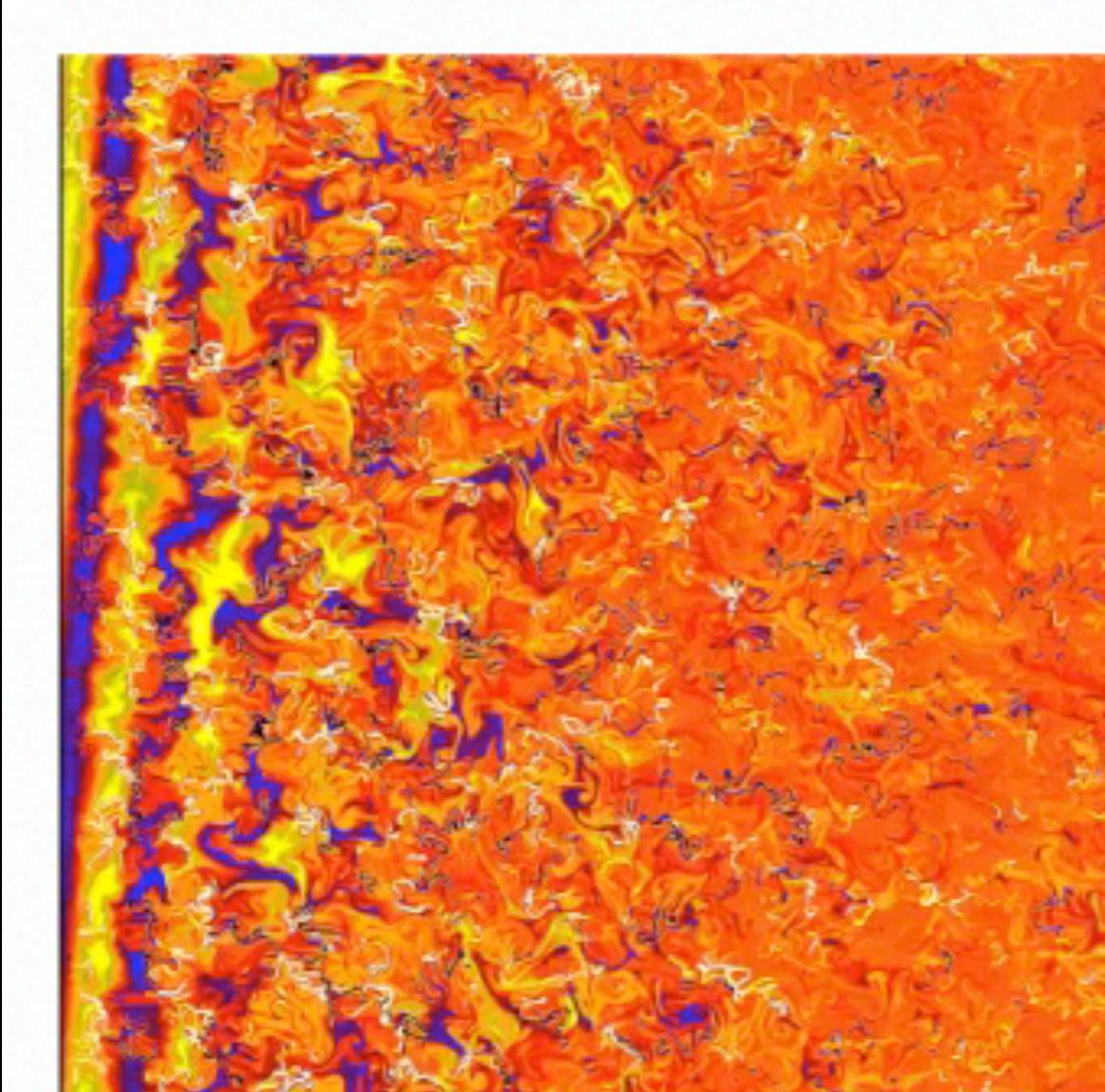
Power in  $k_y$



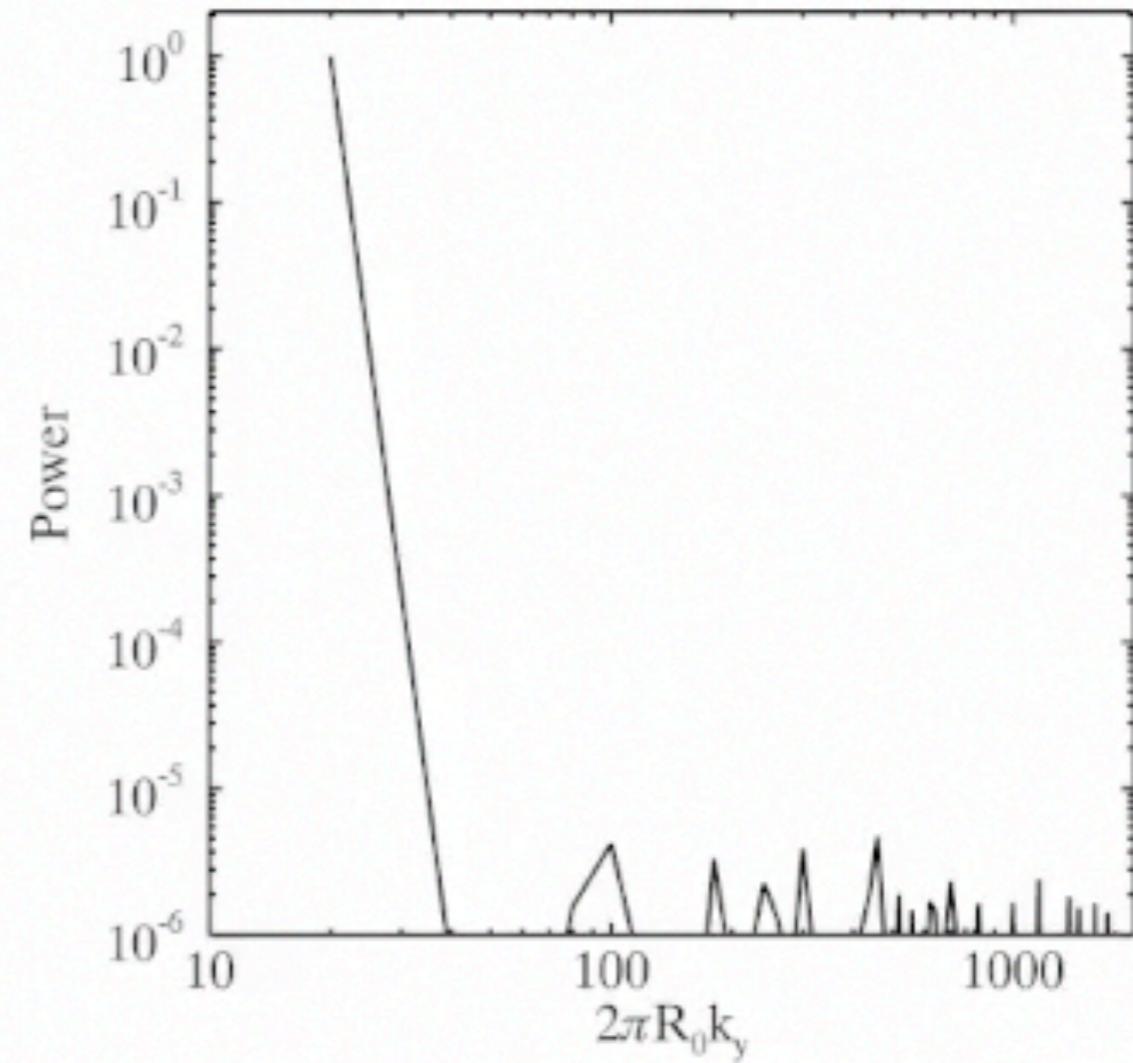
# Following the Flow

Metal Tracer Field

Space  
↑

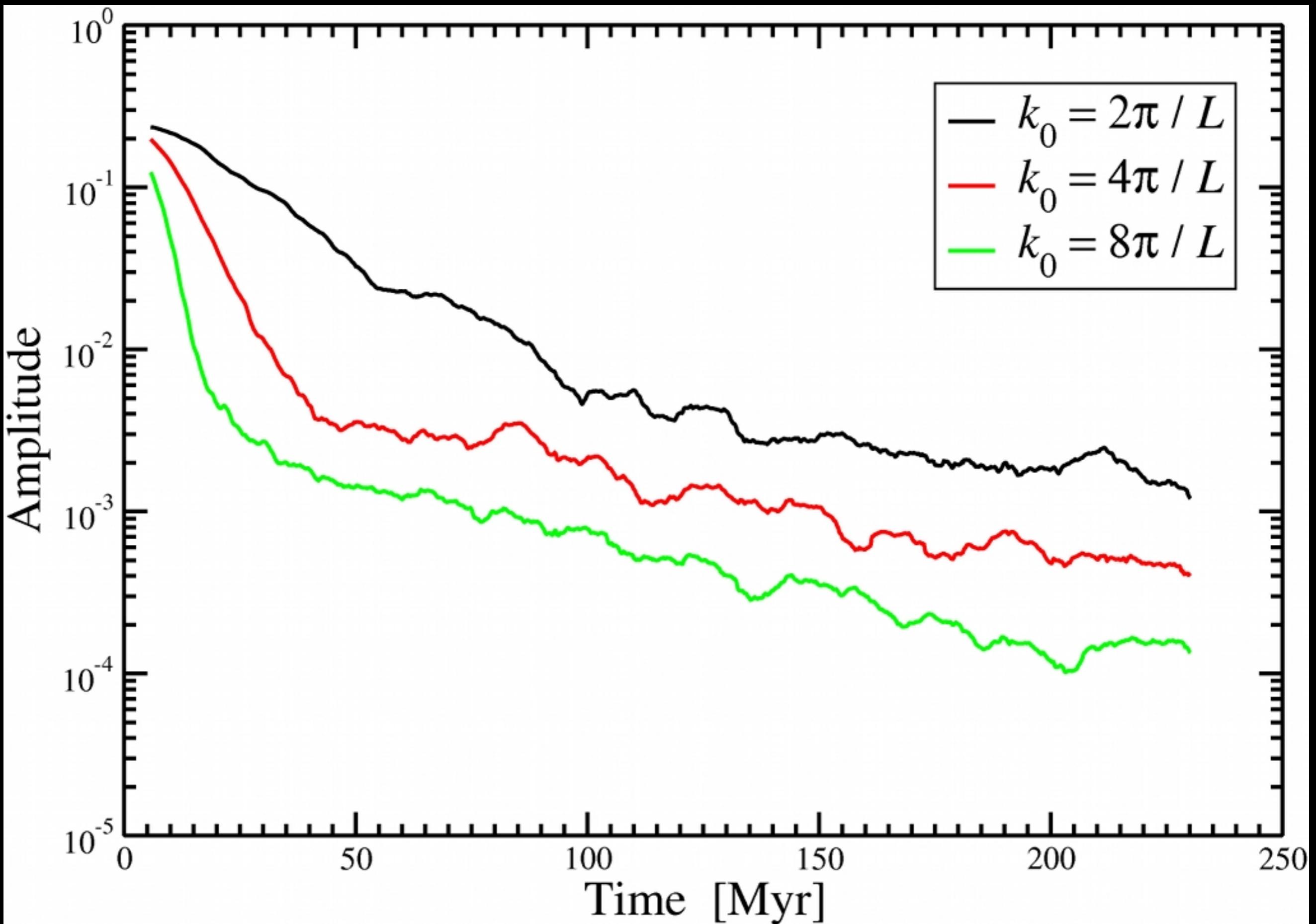


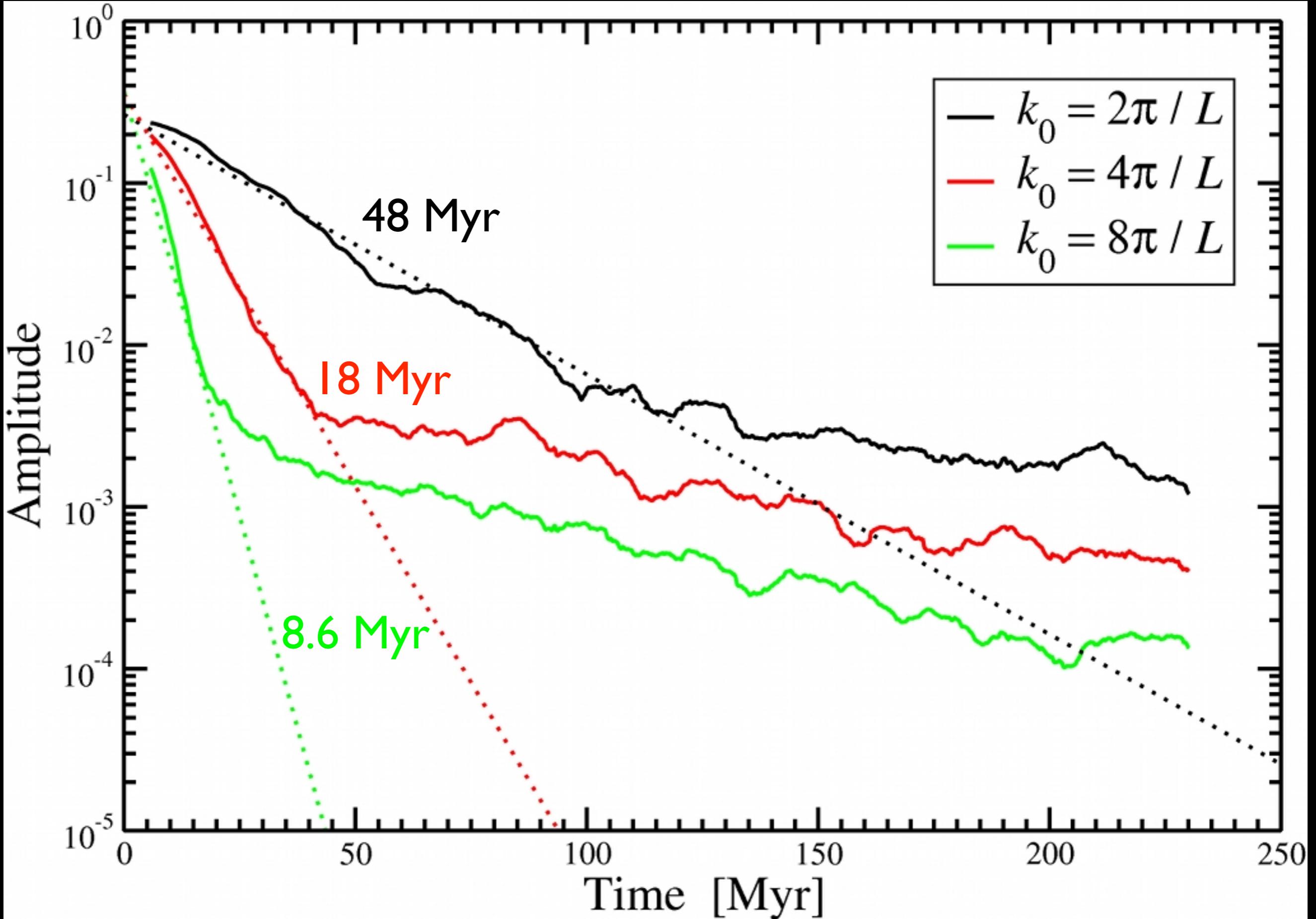
Power in  $k_y$

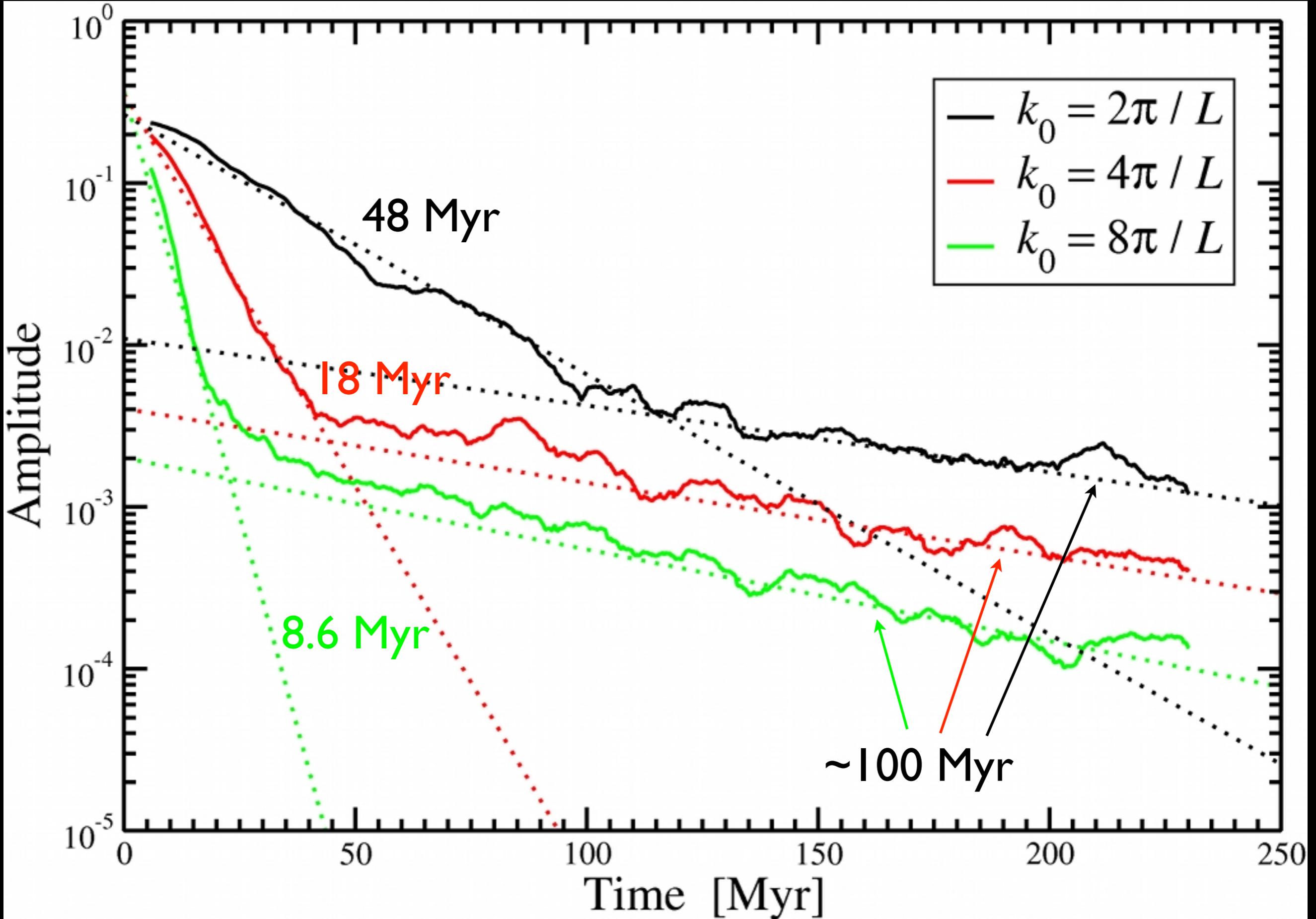


→ Time

//  
↑  
e<sub>φ</sub>  
⊥







**Table 3**  
Properties of the Mixing Process for Different Metal Tracers in Model T

$\lambda_{\text{inj}}$ (kpc)	First Stage			Second Stage		
	$\bar{t}_0$ (Myr)	$\tau_D$ (Myr)	$D$ ( $\text{kpc}^2 \text{ Gyr}^{-1}$ )	$\tau_D$ (Gyr)	$D$ ( $\text{kpc}^2 \text{ Gyr}^{-1}$ )	
3.1	100	48	5.2	0.20		1.2
1.6	41	18	3.5	0.16		0.38
0.78	22	8.6	1.8	0.13		0.12
0.39	12	4.0	0.96	0.11		0.037

**Notes.**  $\lambda_{\text{inj}}$  is the wavelength of the metal distribution injected from the left boundary.  $\bar{t}_0$  denotes the approximate advection time when the mixing process transitions from the first stage to the second.  $\tau_D$  and  $D$  respectively represent the decay time constant of the injected distribution and the corresponding diffusion coefficient at each stage.

$$D \sim \alpha c_s H? \quad c_s H \simeq 0.7 \text{ kpc}^2 \text{ Gyr}^{-1}$$

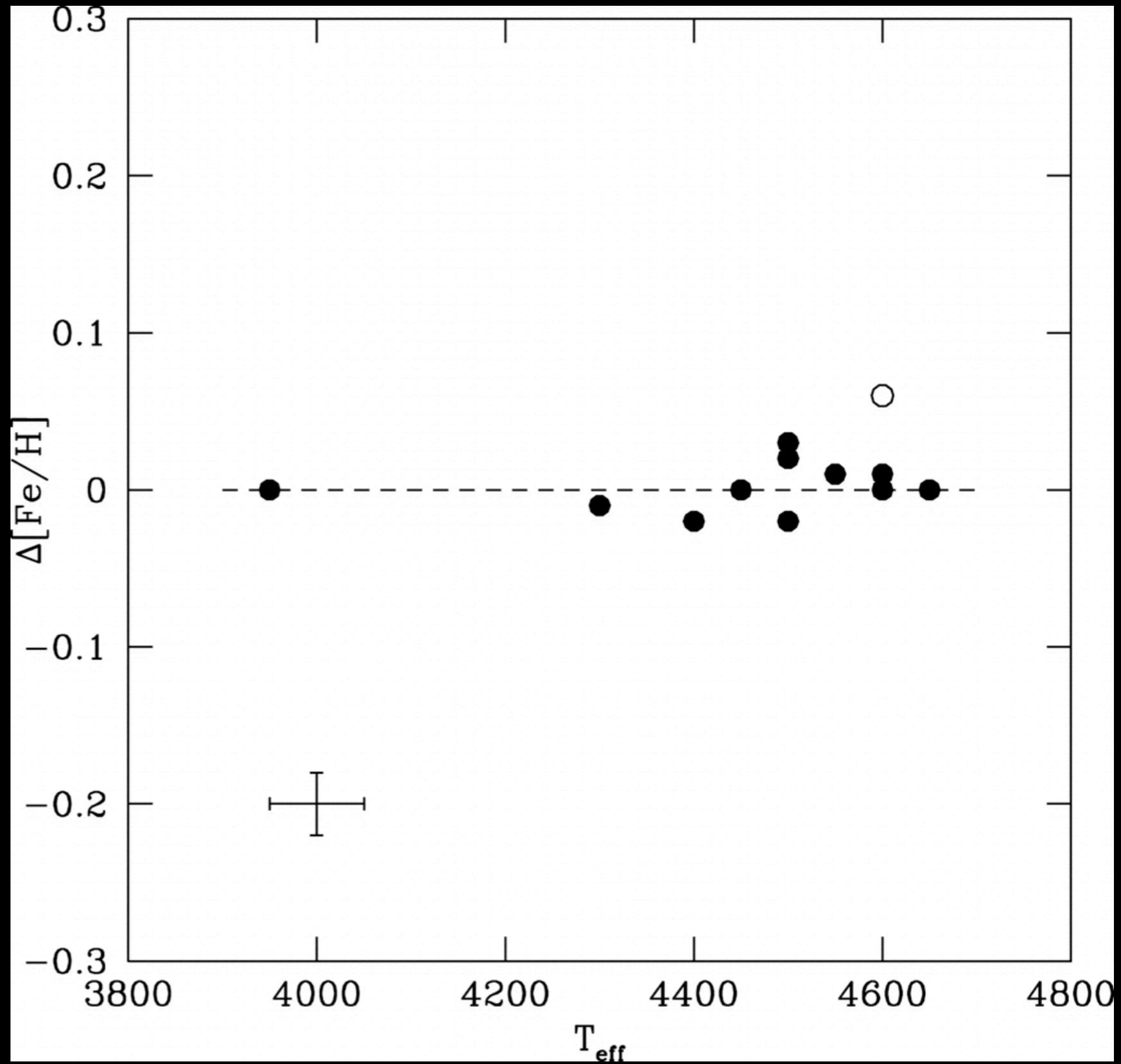
# Conclusions

Turbulent mixing of metals...

- is efficient (timescale < orbital time).
- is not the same as the viscous stress of the gas.
- is important in setting metallicity gradients.

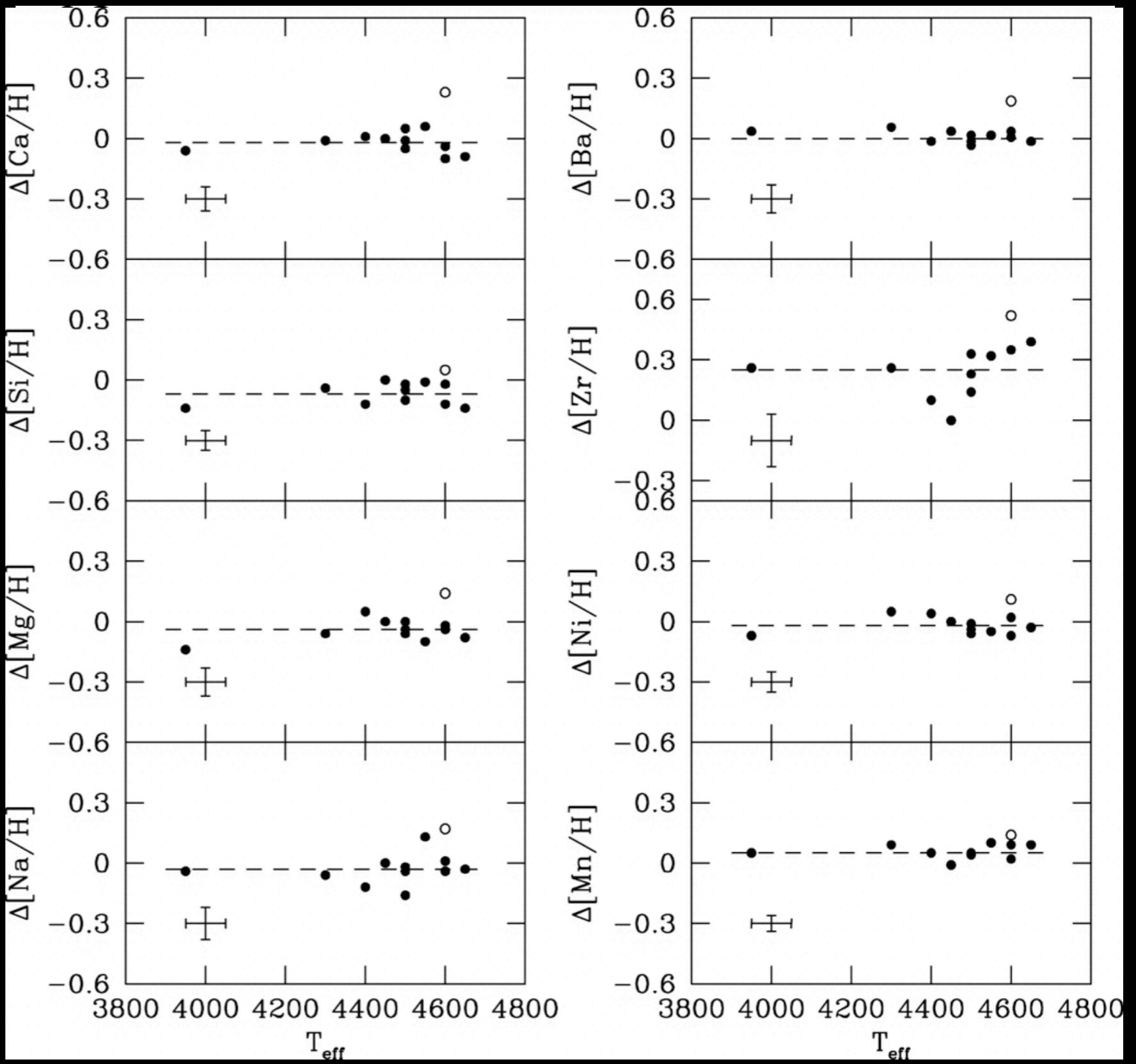
Where do we go  
from here?

# Chemical Homogeneites in Old Open Clusters



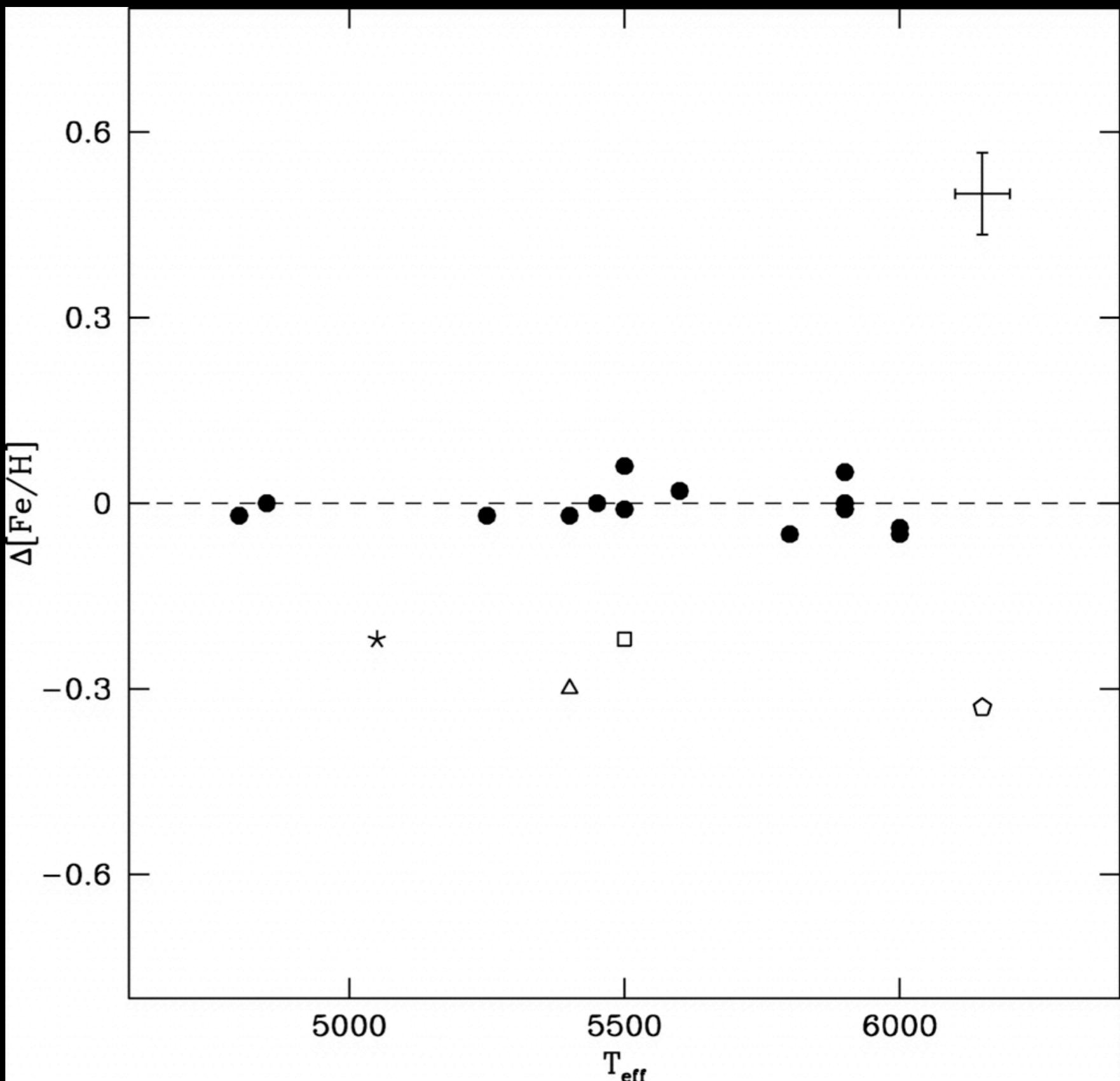
Cr 26 I, de Silva et al. 2007b

# Chemical Homogeneites in Old Open Clusters



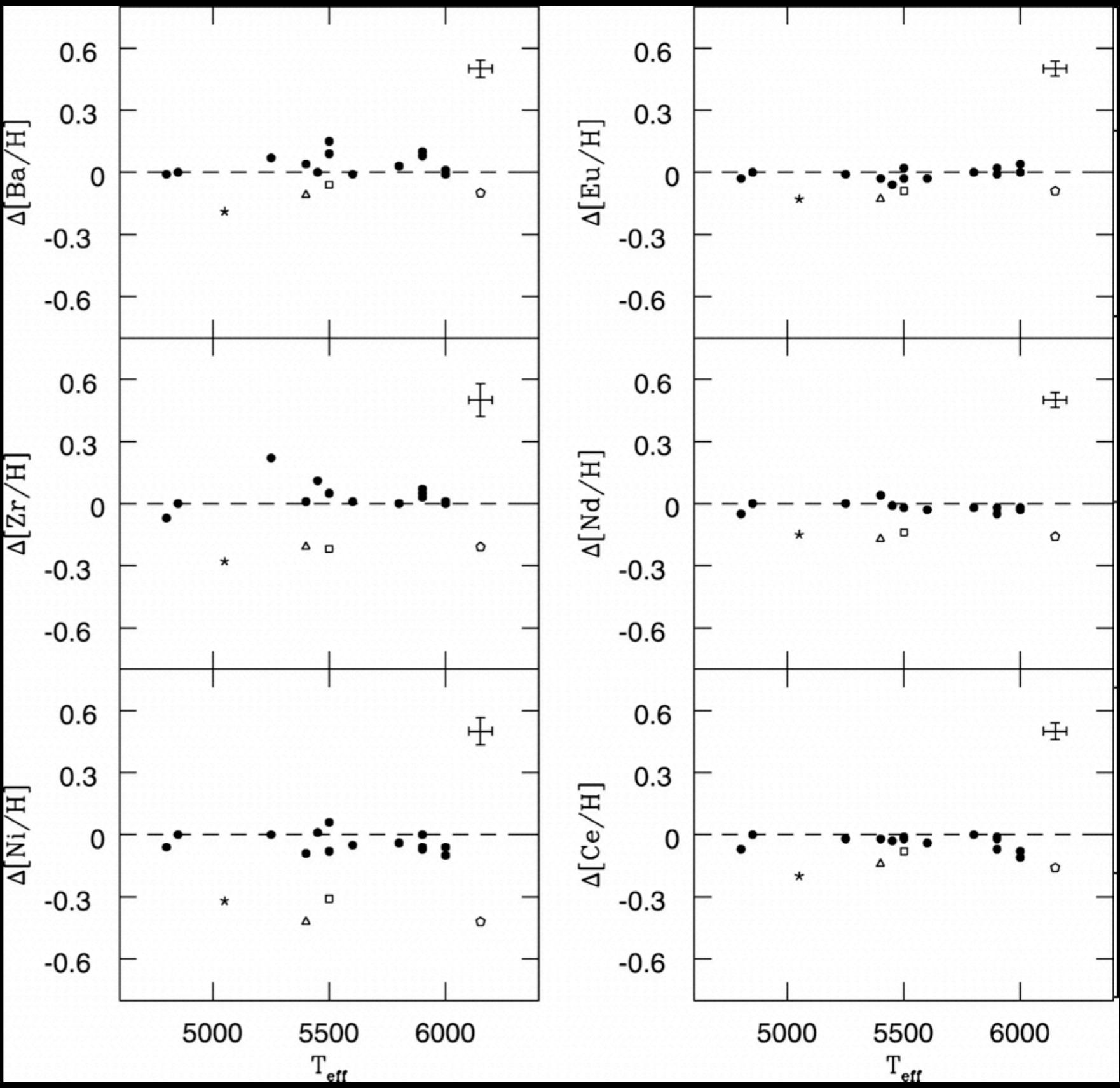
Cr 26 I, de Silva et al. 2007b

# Chemical Homogeneites in Moving Groups



HR 1614, de Silva et al. 2007a

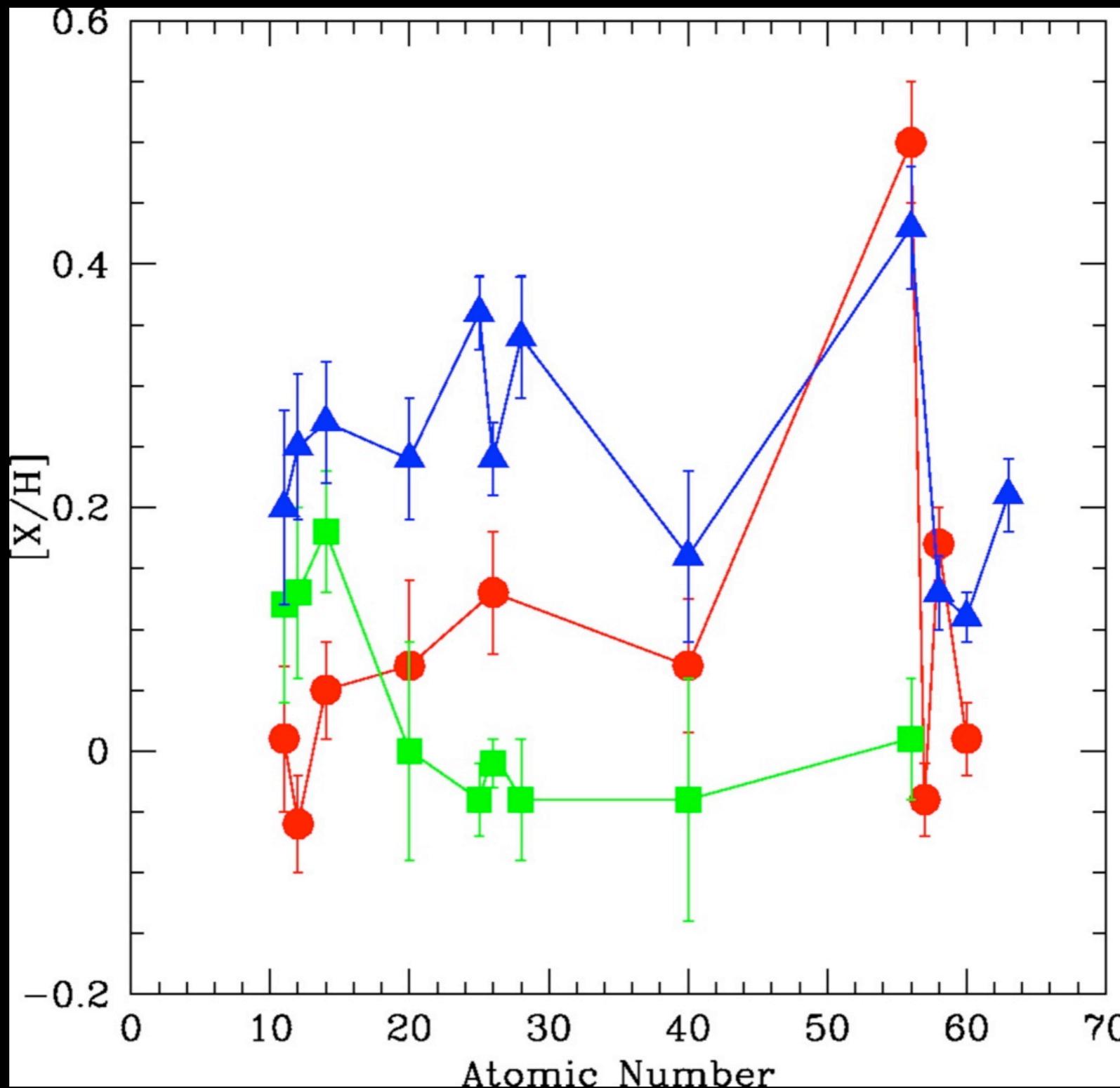
# Chemical Homogeneites in Moving Groups



HR 1614, de Silva et al. 2007a

# Chemical Tagging Technique

(Freeman & Bland-Hawthorn 2002)



*de Silva et al. 2007b*

# Stay tuned...

