# Modeling protein aggregation: from sticks to atomic representation

Anders Irbäck Computational Biology and Biological Physics

- Exponentially many possible states
- Unique "native" state
- Native structure by X-ray crystallography or NMR
- Local structure:  $\alpha$ -helices and  $\beta$ -sheets







- Protein with 100 amino acids, 3 states per amino acid  $\rightarrow 3^{100} \sim 10^{47}$  possible structures
- Levinthal's paradox: a random search for the native state would take the protein longer than the age of the universe
- Forces driving folding: H bonding, hydrophobic attraction,...

Do we have

- (i) sufficient knowledge of the driving forces, and
- (ii) sufficiently fast computers
- to be able to simulate the folding of a 100-amino acid protein?

- Computationally designed & experimentally verified protein with >90 amino acids and a novel fold Kuhlman et al. Science 2003;302:1364-1368
- Folding simulations started from random initial conditions. Atomic protein representation, implicit water. General force field, Monte Carlo methods Mohanty et al. Proteins 2013;81:1446-1456

### Simulated structure and crystal structure

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Monday, October 28, 13

Mohanty et al. Proteins 2013;81:1446-1456

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## Folding of Top7



Mohanty et al. Proteins 2013;81:1446-1456

#### **Protein aggregation**



Hartl and Hayer-Hartl NSMB 2009;16:574-581

- Characteristic core of β-sheets
- "Universal": formed by many proteins
- Interesting material properties
- · Linked to many diseases, can be functional



Dobson TBS 1999;24:329-332

### **Amyloid formation**

 Fibril formation occurs with sigmoidal kinetics. Critical nucleus?



• Fibril growth occurs by monomer addition. Aggregation-competent form of the monomer?



- Experimentally difficult, transient species
- Simulations: system size limitations
- Simple nucleation (3D): balance volume, surface terms.
  No critical size in 1D
- Need to study the interplay between fibril length and width
- Sigmoidal kinetics independent of sequence details
- $\longrightarrow$  coarse-grained modeling

Minimalistic model for amyloid formation

- Assume internal dynamics fast and can be averaged out
- Each peptide unit-length stick, **b**, on a cubic lattice
- H bonds in a direction **p** perpendicular to **b**
- Hydrophobic side s = b x p



A Irbäck, S Æ Jónsson, N Linnemann, B Linse, S Wallin Phys Rev Lett 2013

#### **Kinetics**

- Monte Carlo single-peptide moves
- >100,000 peptides, 10 runs from random initial conditions
- Total fibril mass against Monte Carlo time
- Sigmoidal kinetics



• ~40-50 fibrils, average mass ~1400



- Equilibrium Monte Carlo simulation, 256 peptides Cluster moves and generalized-ensemble techniques
- Aggregate length *I* and width *w* from inertia tensor
- Probability for a peptide to be part of an *I* x *w* aggregate



- To reach a given *I*, a minimum *w* is required
- Multistep process



Jeong et al. JMB 2013; 425:1765-1781

- amyloid  $\beta$ ,  $A\beta$  (Alzheimer's disease)
- α-synuclein, αS (Parkinson's disease)
- superoxide dismutase 1 (amyotrophic lateral sclerosis)
- apolipoprotein A-I

Modeling:

- all-atom protein representation, implicit solvent
- one and the same force field (same as in Top7 study)
- Monte Carlo methods

- Major constituent of Alzheimer plaques
- "Intrinsically disordered", 42 amino acids
- Simulated free energy  $F(surface area,\beta-content)$ :



Αβ

• Typical simulations: more disorder, smaller β-content

 <sup>3</sup>J(H<sup>N</sup>,H<sup>α</sup>)-couplings: functions of a single backbone torsion angle (Karplus equation)



Exp.: Sgourakis et al. JMB 2007; 368:1448-1457

• Comparatively good agreement (alanine outlier)

S Mitternacht, I Staneva, T Härd, A Irbäck Proteins 2010, J Mol Biol 2011

## Experimental characterization of unstructured proteins

- Mainly bulk experiments, which must be interpreted with care
- Single-molecule experiments are becoming available



#### AFM single-molecule pulling experiments



Sandal et al. PLoS Biology 2009; 6:e6

- Force versus distance
- Force peaks signal rupture events
- Aβ and αS: unexpected force resistance Hervás et al. PLoS Biology 2012; 10:e1001335

- Sometimes no resistance, sometimes rupture forces as high as those for unusually stable, folded proteins
- Can a small 42-amino acid protein like Aβ be that forceresistant? If so, what do the structures look like?



Hervás et al. PLoS Biology 2012; 10:e1001335

- Initial structures randomly drawn from simulated ensemble
- Two examples of force vs distance trajectories (in total >500)



SÆ Jónsson, SMitternacht & A Irbäck Biophys J 2013

- Plot symbols indicate initial structures
- The color indicates maximum rupture force. Black <20 pN, white 20-150 pN, red >150 pN



- $\beta$ -structure profiles for force-resistant A $\beta$  and  $\alpha$ S structures
- Similarities with β-strand locations in fibrils





Lührs et al. PNAS 2005;102:17342-17347



Vilar et al. PNAS 2008; 105; 8637-8642

Summary — A $\beta$  and  $\alpha$ S studies

- A $\beta$  and  $\alpha$ S pulling simulations reproduce the surprisingly high rupture forces observed in AFM experiments
- The mechanically most resistant structures
  - share a common architecture:
    a β-sheet with three strands in a meander pattern
  - show similarities with the fibril folds
- Fibril-like structures might play a key role in aggregation

To do:

- Study fibril growth (monomer + fibril template)
- Study aggregation-inhibiting small molecules