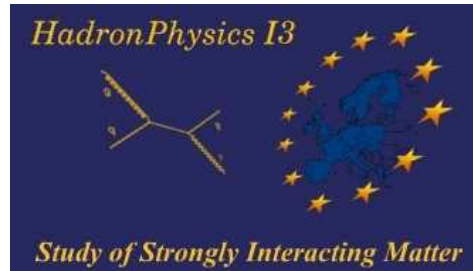




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Hadronic Contributions to the Muon Anomalous Magnetic Moment

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Overview

- Anomalous Magnetic Moment
- Experiment
- Non hadronic contributions: QED and Weak
- Hadronic Contributions
 - Hadronic Vacuum Polarization
 - Light-by-Light
- Conclusions

Recent Papers: [A. Höcker, hep-ph/0410081 \(ICHEP Beijing\)](#); [B. Roberts, hep-ex/0501012](#), [M. Knecht, hep-ph/0307239](#), [M. Passera, hep-ph/0411168](#)

Anomalous magnetic Moment

Classically

$$\mu = \frac{q}{2mc} \vec{L}$$

Quantum Mechanics

$$\vec{\mu} = g \frac{q\hbar}{2m_c} \vec{S}$$

g : gyromagnetic ratio: intrinsic to particle

Relativistic Quantum Mechanics

Dirac Equation

$$g = 2$$

True for e^- , not for $p, n \implies$ composite particles

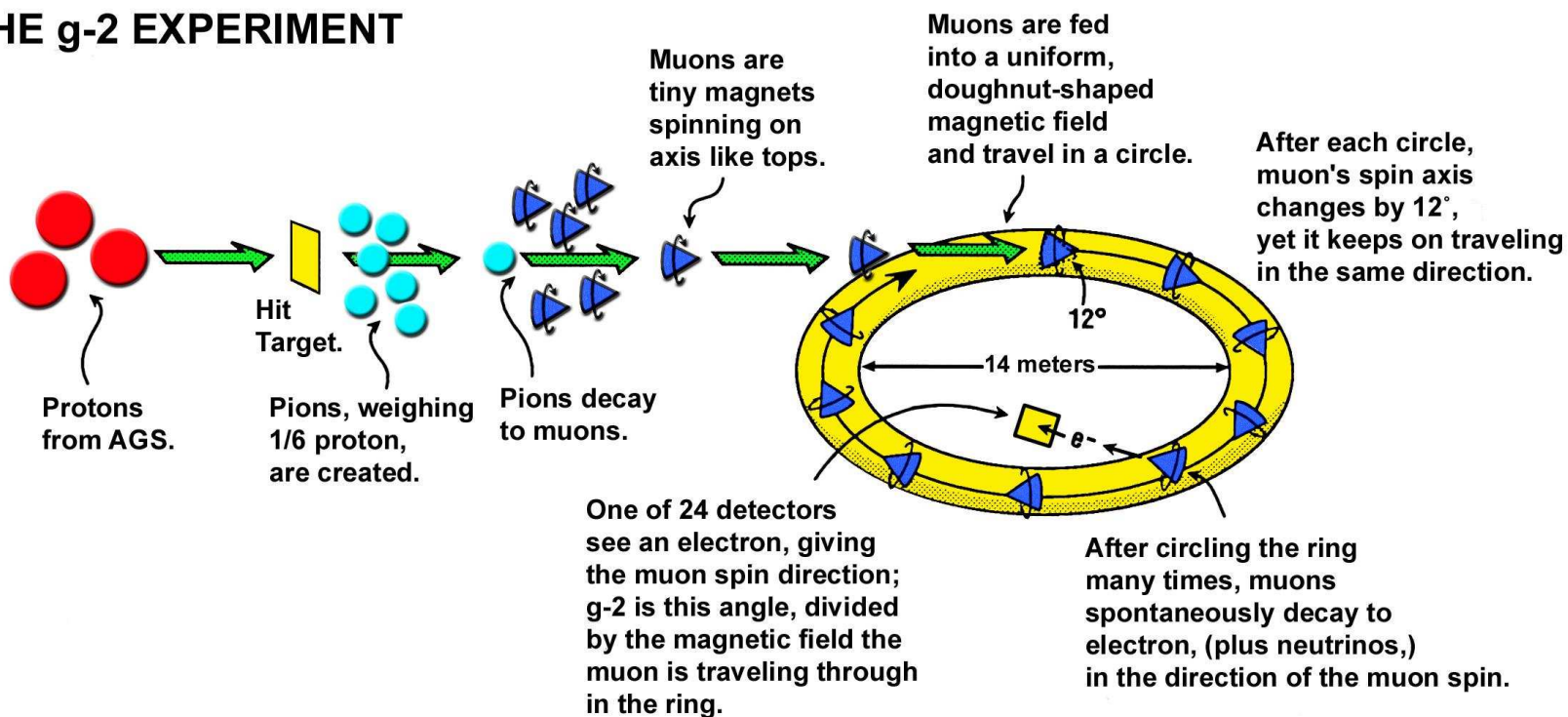
Quantum Field Theory

$$g = 2(1 + a)$$

$a_e = \frac{\alpha}{2\pi}$ Great success for QED (Schwinger)

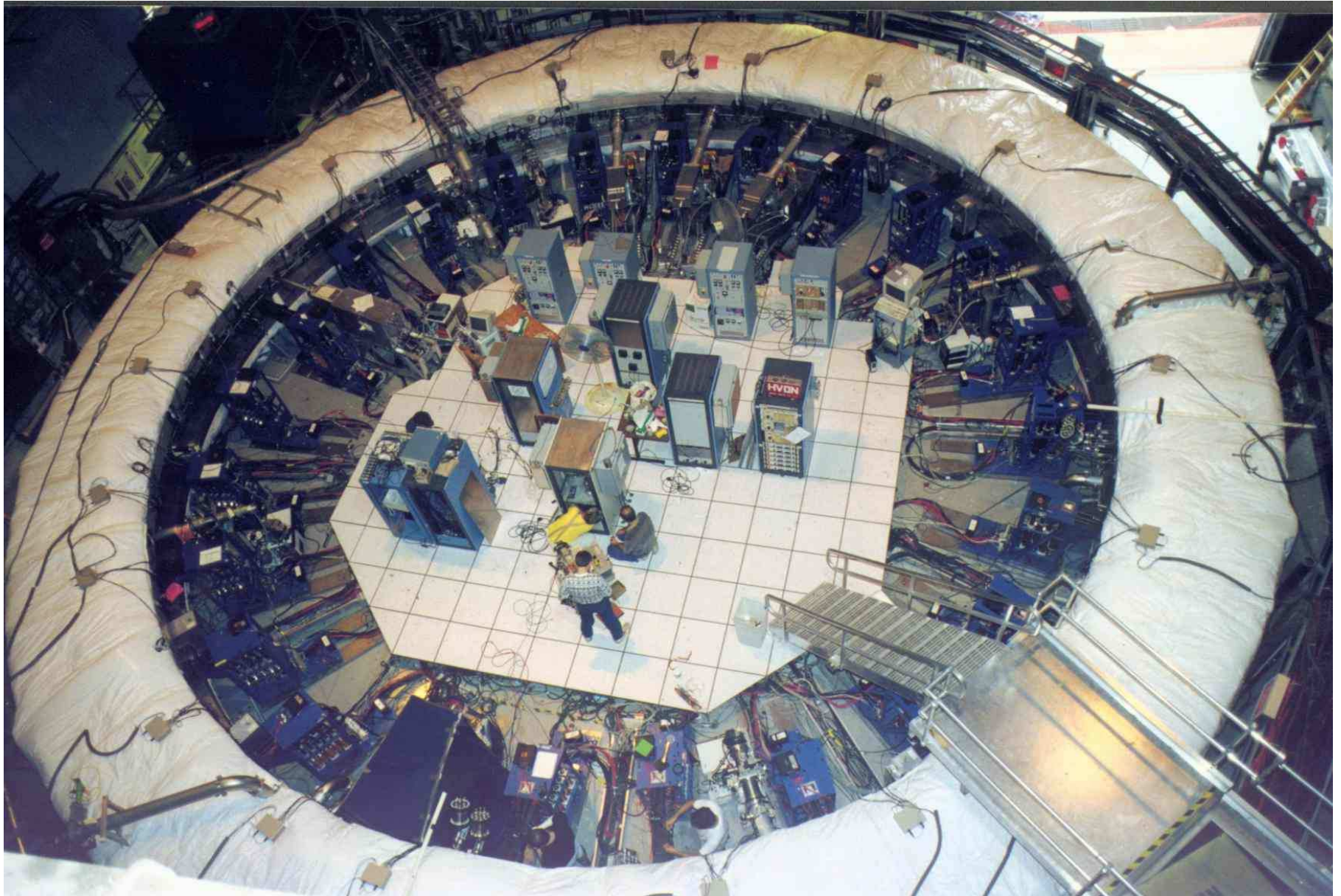
Experiment

LIFE OF A MUON: THE $g-2$ EXPERIMENT



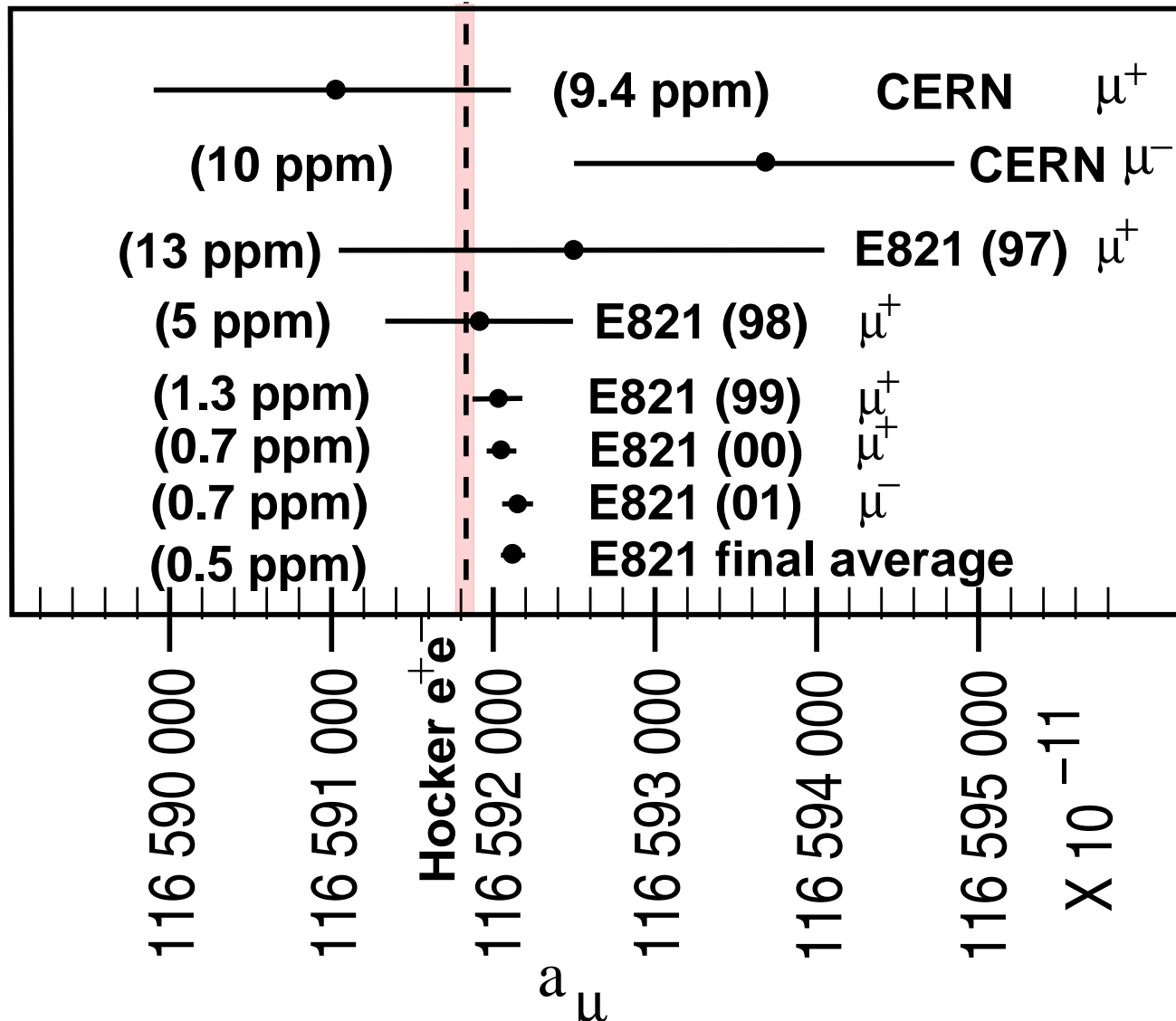
(<http://www.g-2.bnl.gov>)

Experiment



(<http://www.g-2.bnl.gov>)

Experiment



hep-ex/0501012

$$a_\mu(E821) = 11659208.0(5.8) \times 10^{-10}$$

0.5 ppm

Planned:

E969

0.2 ppm

Later

J-PARC

QED and Weak

- $a_\mu = a_\mu(QED) + a_\mu(hadronic) + a_\mu(weak)$
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- $a_\mu(weak) = 15.4(3) \times 10^{-10}$

Czarnecki, Marciano, Vainshtein, Knecht, de Rafael, Peris,...

Notice: $a_\mu(weak \text{ one-loop}) = 19.48 \times 10^{-10}$

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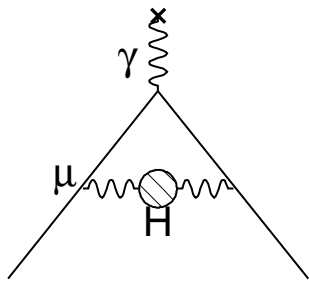
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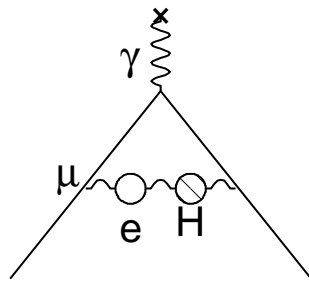
$$\begin{aligned} a_\mu(hadronic) &\equiv a_\mu - a_\mu(QED) - a_\mu(weak) \\ &= 720.6(5.8) \times 10^{-10} \end{aligned}$$

Hadronic Contributions

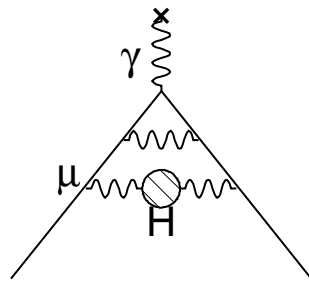
$$a_{\mu}(\text{hadronic-exp}) = 720.6(5.8) \times 10^{-10}$$



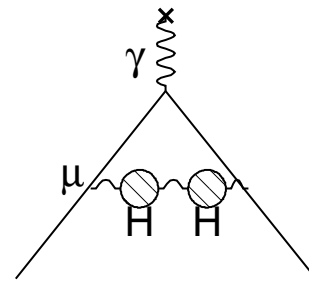
(a)



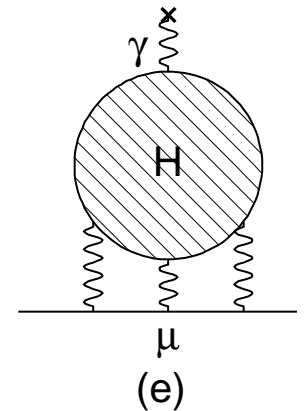
(b)



(c)



(d)



(e)

(hep-ex/0501012)

- (a) Hadronic vacuum polarization: HVP
- (b),(c),(d) higher order HVP: HOV
- (e) Light-by-Light scattering: LBL

Hadronic Contributions

- HVP is the largest contribution
- HOVP is about -10×10^{-10}
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THIS WILL BE DIFFICULT

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THIS WILL BE DIFFICULT

In principle lattice QCD can calculate this

But: difficult observables, large energy ranges, chiral cancellations,...

Hadronic Vacuum Polarization

$$a_{\mu}(HVP) = \left(\frac{\alpha m_{\mu}}{3\pi} \right)^2 \int_{4m_{\pi}^2}^{\infty} \frac{ds}{s^2} K(s) R(s)$$

$$R(s) \equiv \frac{\sigma(e^{+}e^{-} \rightarrow \text{hadrons})}{\sigma(e^{+}e^{-} \rightarrow \mu^{+}\mu^{-})}$$

so we can use experiment to get the precision we want

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$$a_{\mu}(HOVP) = -10.0(6) \times 10^{-10}$$

Krause 1997

$$a_{\mu}(HOVP) = -9.8(1) \times 10^{-10}$$

Hagiwara et al., 2004

Hadronic Vacuum Polarization

- $e^+e^- \rightarrow$ hadrons (the old fashioned way)
- $\tau \rightarrow$ hadrons Davier et al
- Radiative return Kühn et al

Davier, Höcker, Alemany, Eidelmann, Jegerlehner, Yndurain, de Troconiz, Hagiwara, Martin, Nomura, Teubner

$e^+e^- \rightarrow \text{hadrons}$

- Need luminosity normalization at every point
- Correction to the bare process
- exclusive versus inclusive measurements
- final states including extra photons

Main contribution dominated by CMD-2 data
higher energies: combine data from many experiments

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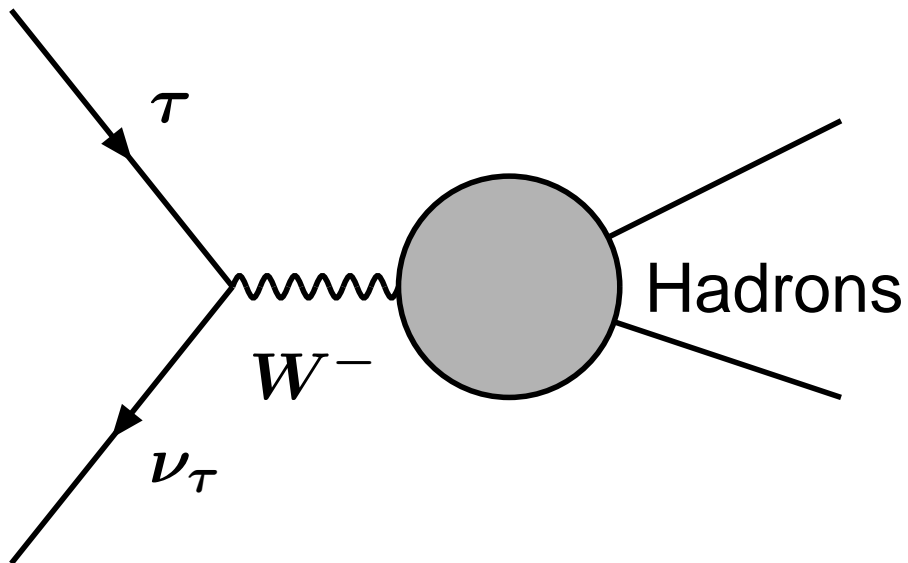
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- Chiral perturbation theory at very low energies
- Dispersion theory in the intermediate regime (under way)
- As much QCD as you can at higher energies

Tau decays

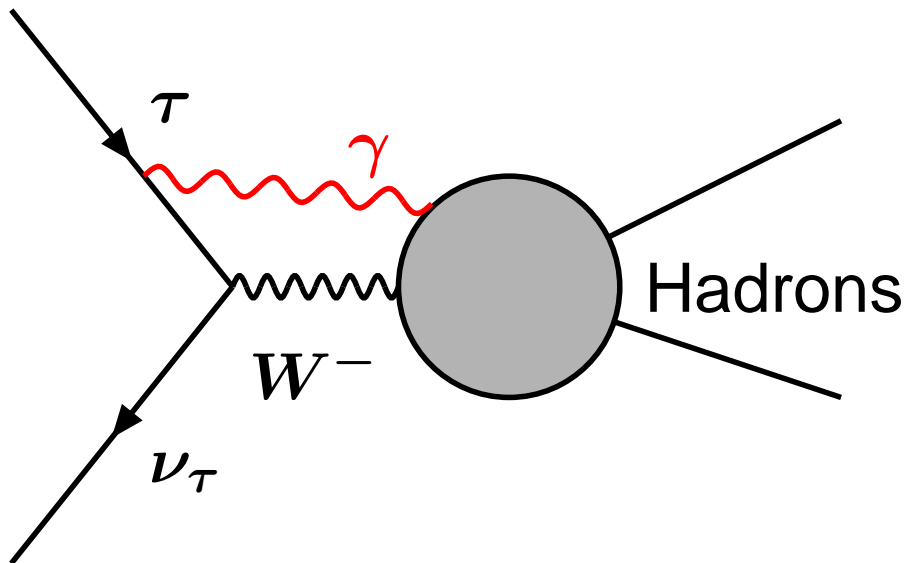
Review: [Davier, Höcker, Zhang, hep-ex/0507078](#) source of many figures



In principle advantage: luminosity is tagging question (and only once), parasitic running

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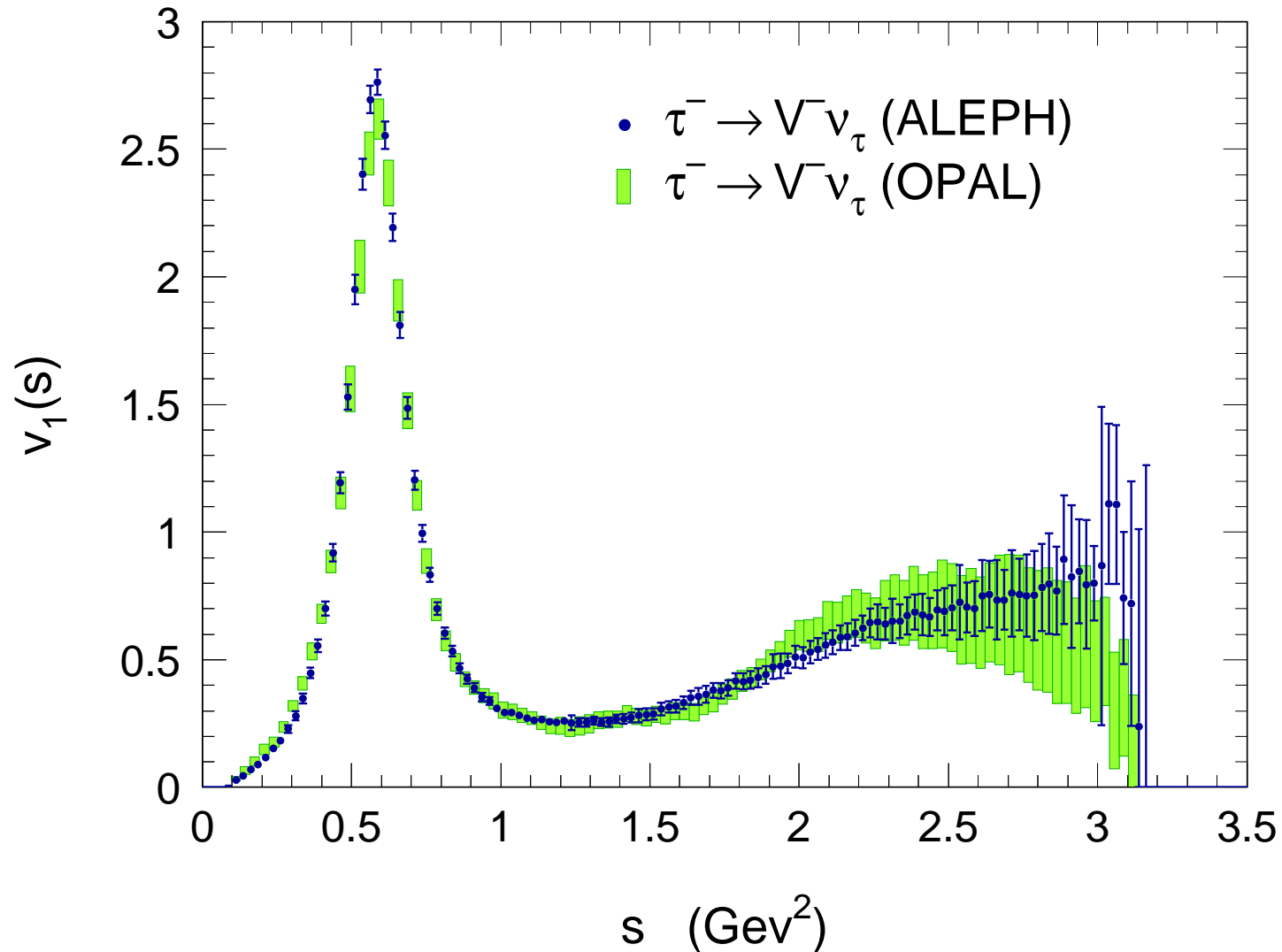


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Need to correct for isospin and radiative corrections

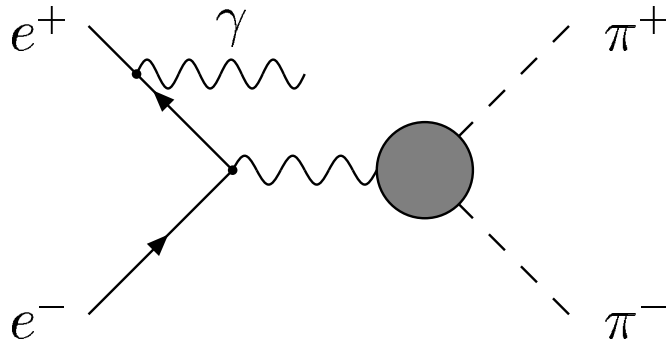
Tau decays

An example of results (ALEPH, OPAL, CLEO in agreement)



Radiative Return

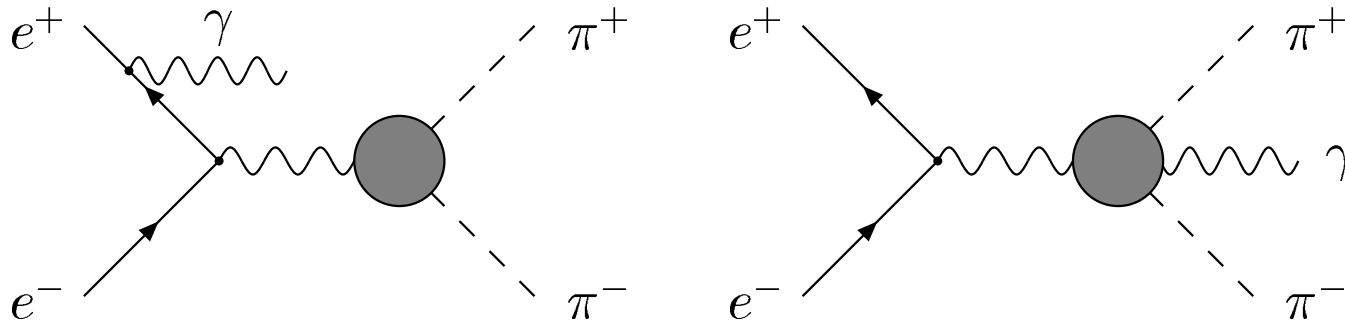
Review: Czyż et al., hep-ph/0312217



So use photon to get to lower E_{cms}

Radiative Return

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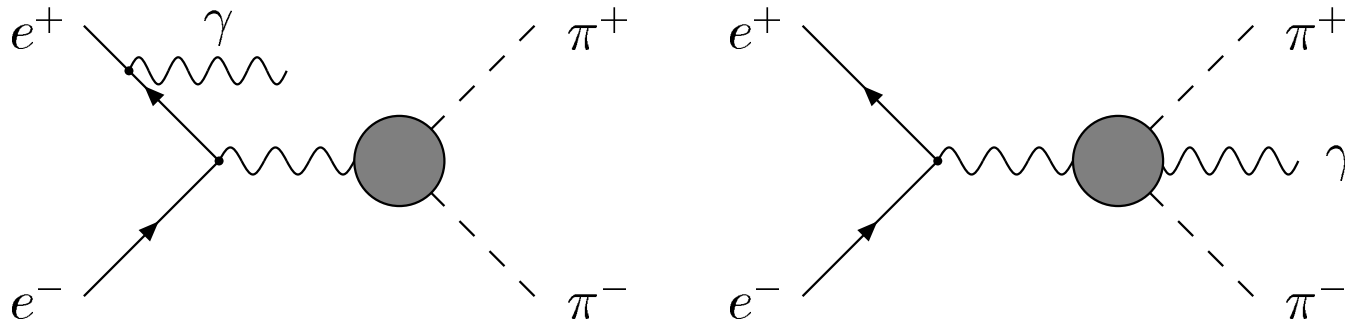
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Need careful separation of initial and final state radiation

Much work done, final uncertainty still under discussion

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So use photon to get to lower $E_{cm s}$

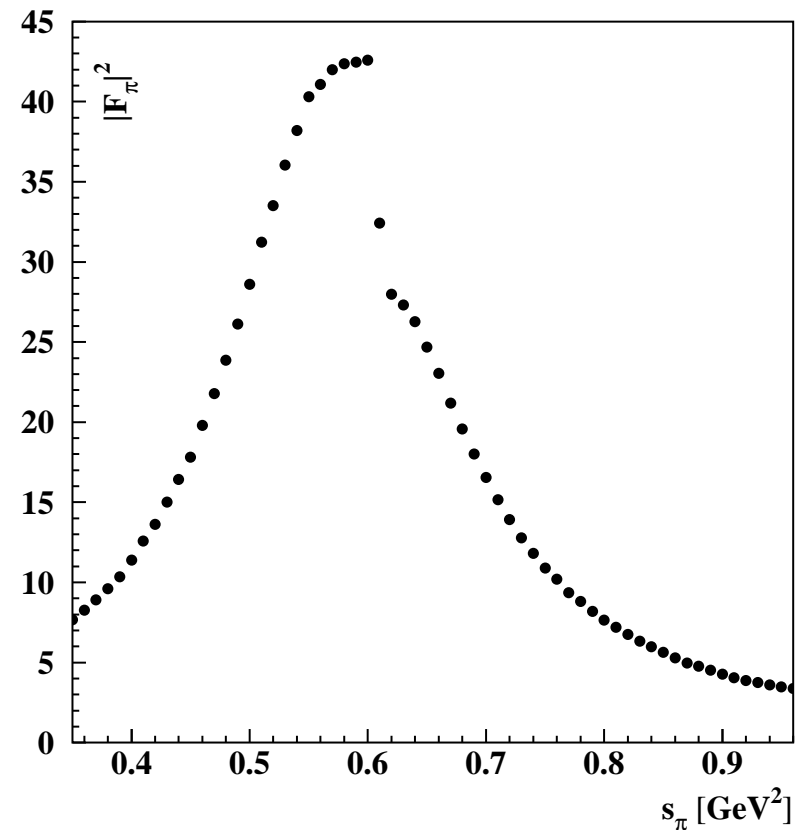
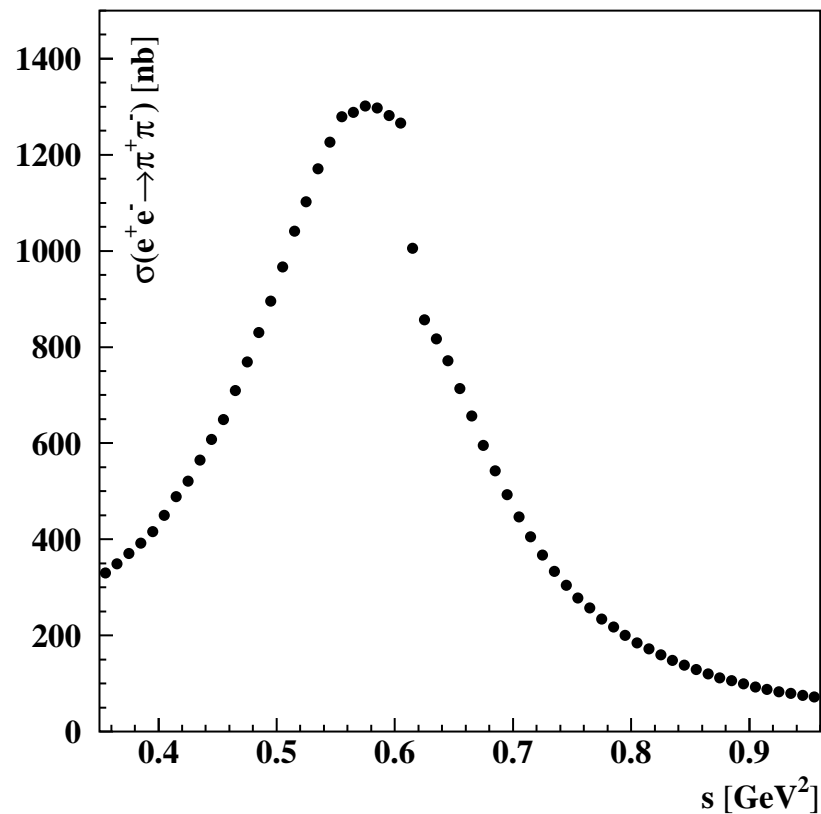
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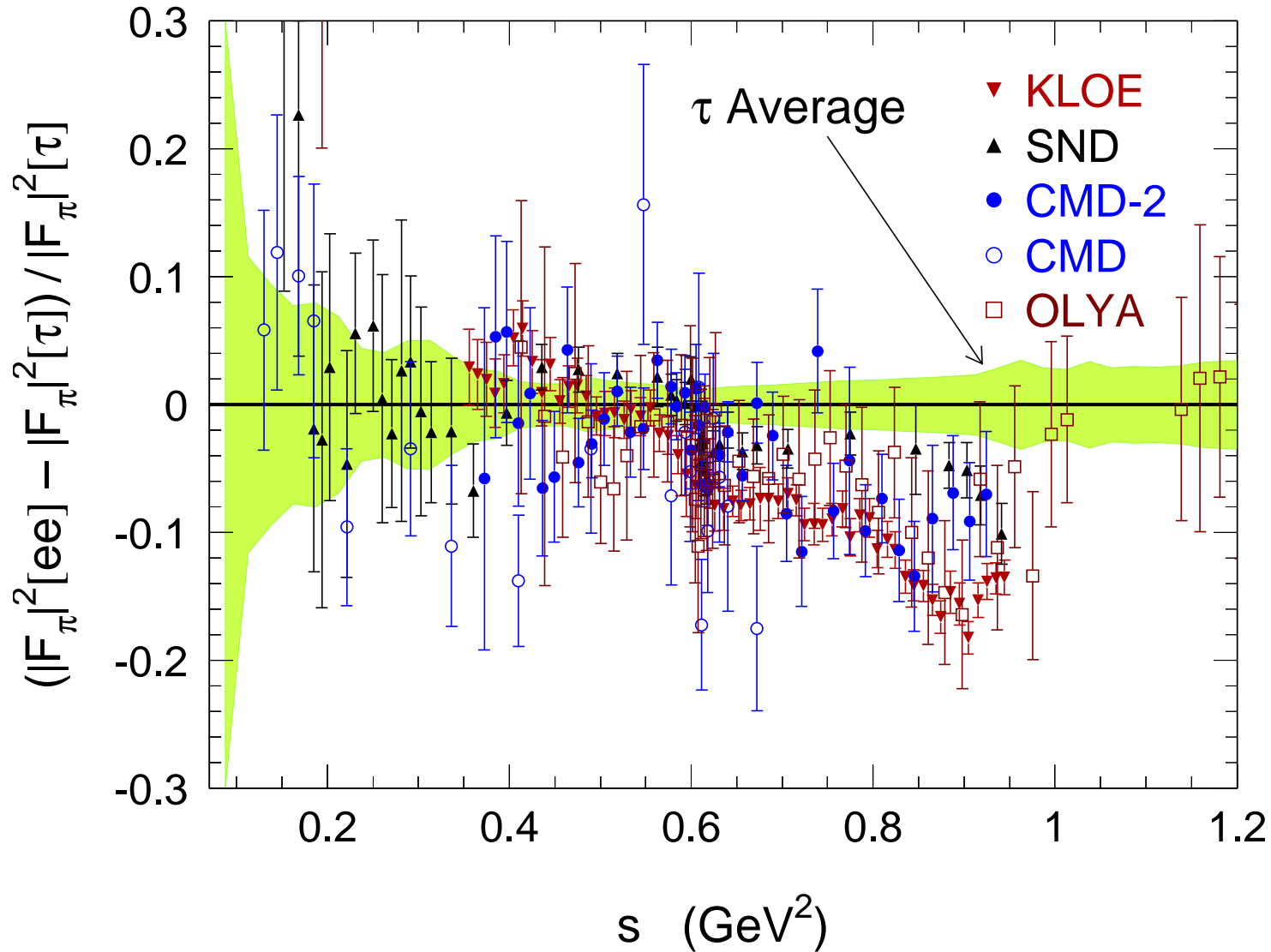
Large experimental advantages: parasitic to factories, luminosity only once

Radiative Return: experiment

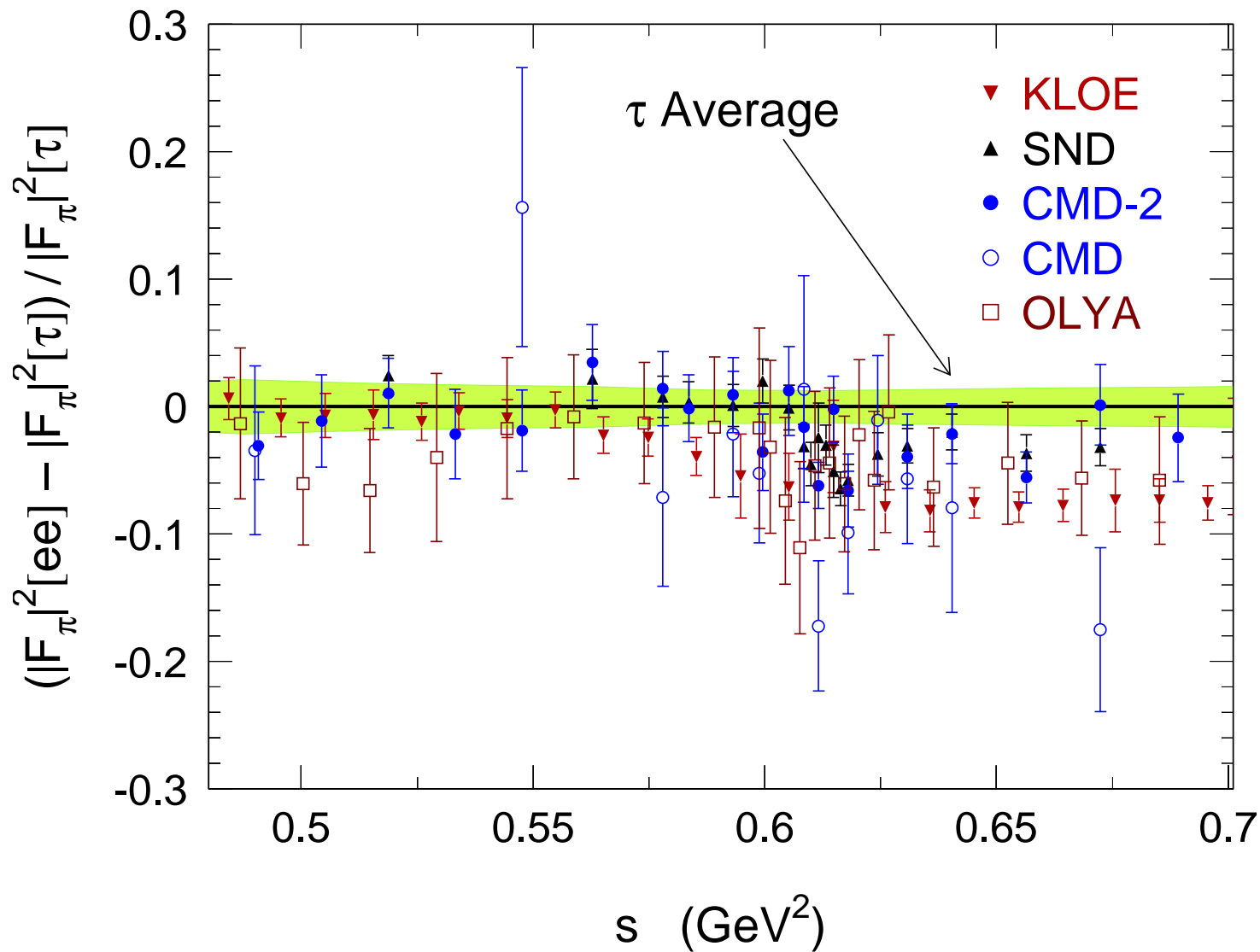
Measurements under way at KLOE ([hep-ex/0407048](https://arxiv.org/abs/hep-ex/0407048)), BaBar and Belle(?)



Comparison of the three



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$$a_{\mu}(HVP)(e^{+}e^{-}) = (693.4 \pm 5.3 \pm 3.5_{\text{rad}}) \times 10^{-10}$$

$$a_{\mu}(HVP)(e^{+}e^{-}_{\text{no KLOE}}) = (696.3 \pm 6.2 \pm 3.6_{\text{rad}}) \times 10^{-10}$$

$$a_{\mu}(HVP)(\tau) = (711.0 \pm 5.0_{\text{exp}} \pm 0.8_{\text{rad}} \pm 2.8_{\text{iso}}) \times 10^{-10}$$

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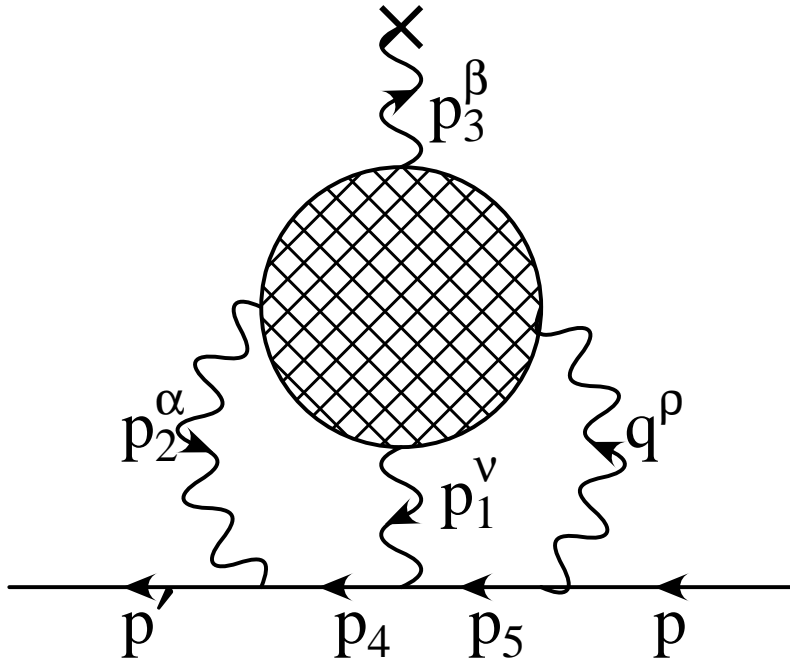
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Hagiwara et al., 2004

$$a_{\mu}(\text{hadronic-exp}) = 720.6(5.8) \times 10^{-10}$$

Light-by-Light Contribution



$$\mathcal{M} = |e|^7 A_\beta \int \frac{d^4 p_1}{(2\pi)^4} \frac{d^4 p_2}{(2\pi)^4} \frac{1}{q^2 p_1^2 p_2^2 (p_4^2 - m^2) (p_5^2 - m^2)}$$

$$\times \Pi^{\rho\nu\alpha\beta}(p_1, p_2, p_3) \bar{u}(p') \gamma_\alpha (\not{p}_4 + m) \gamma_\nu (\not{p}_5 + m) \gamma_\rho u(p)$$

Light-by-Light Contribution

$$\Pi^{\rho\nu\alpha\beta}(p_1, p_2, p_3) \equiv \sum_{(abcd)} i^3 \int d^4x d^4y d^4z e^{i(p_1 \cdot x + p_2 \cdot y + p_3 \cdot z)} \\ \times \langle 0 | T \left(V_a^\rho(0) V_b^\nu(x) V_c^\alpha(y) V_d^\beta(z) \right) | 0 \rangle.$$

$$V_i^\mu(x) \equiv Q_i [\bar{q}_i(x) \gamma^\mu q_i(x)]$$

Green function with four electromagnetic currents

138 Lorentz structures \implies 32 combinations can contribute

8 dimensional integral: 3 can be done

5 remain: 2 moduli, 3 angles

Many scales problem

Light-by-Light: the scale

Muon Loop: 46.5×10^{-10}

Light-by-Light: the scale

Muon Loop: 46.5×10^{-10}

Λ [GeV]	$10^{10} \times a_\mu$
0.5	24
0.7	26
1.0	38(1)
2.0	45(1)

Rather high scales even for muon

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Constituent Quark Loop: 24×10^{-10}

But how good is this number?

Light-by-Light Contribution

Hadronic degrees of freedom versus quark picture

Light-by-Light Contribution

Hadronic degrees of freedom versus quark picture

Separate contributions by chiral powers and large N_c

de Rafael 93

- p^6, N_c : π^0, η, η' exchange
- p^8, N_c : quark loop, “heavy” meson exchanges
- $p^4, 1$: meson loops

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04: More short distance put in Melnikov-Vainstein (MV)

Light-by-Light: old trick

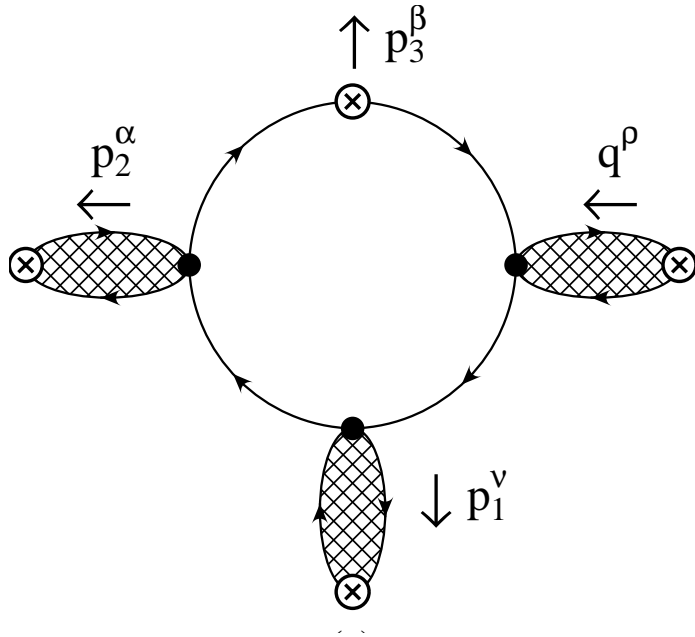
Gauge invariance: $p_{3\beta}\Pi^{\rho\nu\alpha\beta}(p_1, p_2, p_3) = 0$

$$\Pi^{\rho\nu\alpha\lambda}(p_1, p_2, p_3) = -p_{3\beta} \frac{\delta\Pi^{\rho\nu\alpha\beta}(p_1, p_2, p_3)}{\delta p_{3\lambda}}$$

so can calculate at $p_3 = 0$ everywhere

Light-by-Light: Quark Loop

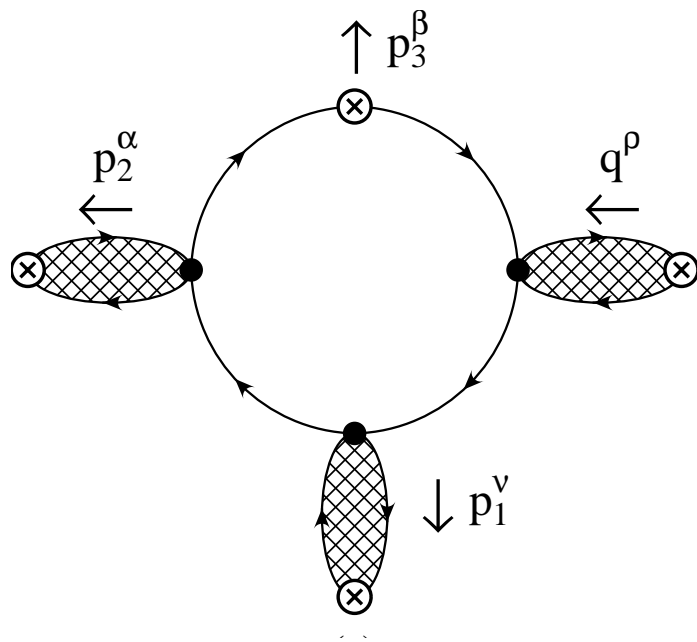
Bijnens, Pallante, Prades



- Low Energy: Extended Nambu-Jona Lasinio model
- High Energy: Bare quark loop with $m_Q = \Lambda$

Light-by-Light: Quark Loop

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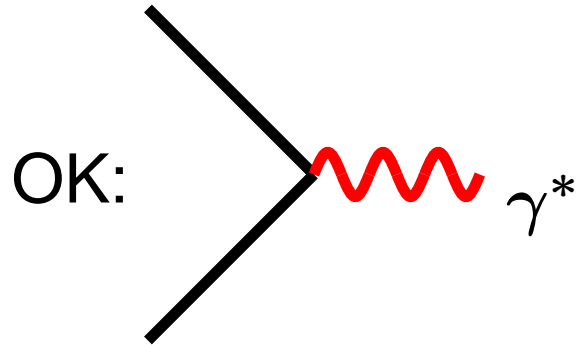


Λ [GeV]	$10^{10} \times a_\mu$
0.7	2.2
1.0	2.0
2.0	1.9
4.0	2.0

- Low Energy: Extended Nambu-Jona Lasinio model
- High Energy: Bare quark loop with $m_Q = \Lambda$
- So OK matching for a first try

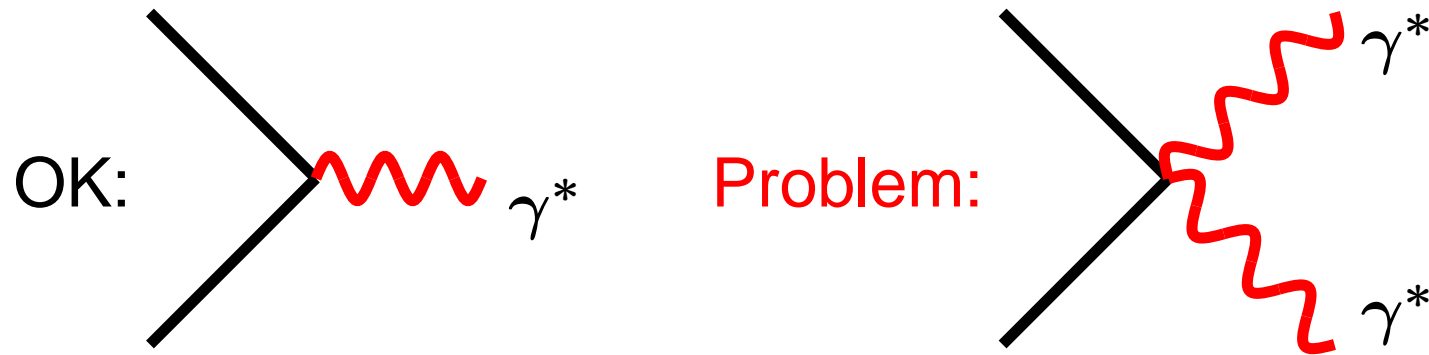
Light-by-Light: Pion-Kaon Loop

Leading contribution in chiral counting, suppressed by $1/N_c$



Light-by-Light: Pion-Kaon Loop

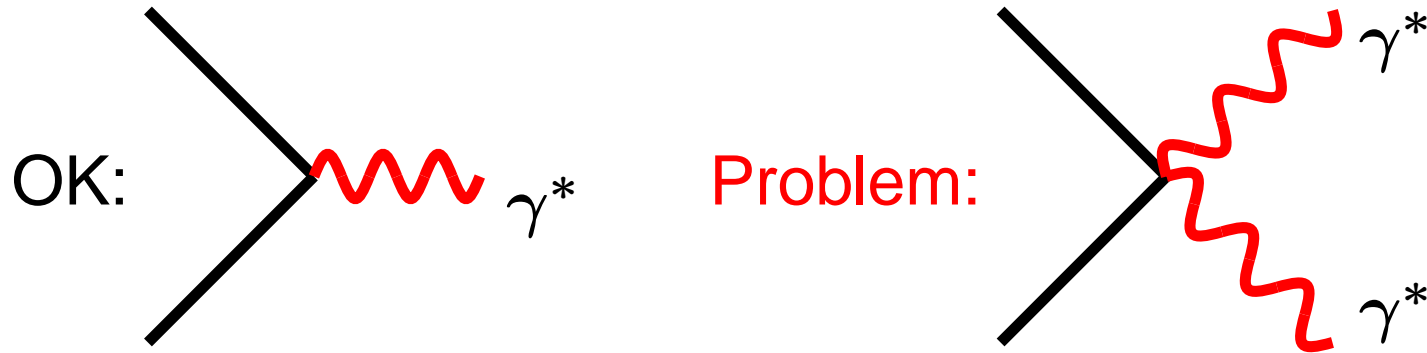
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No data from $\gamma^*\gamma^* \rightarrow \pi\pi$ available: models needed

Light-by-Light: Pion-Kaon Loop

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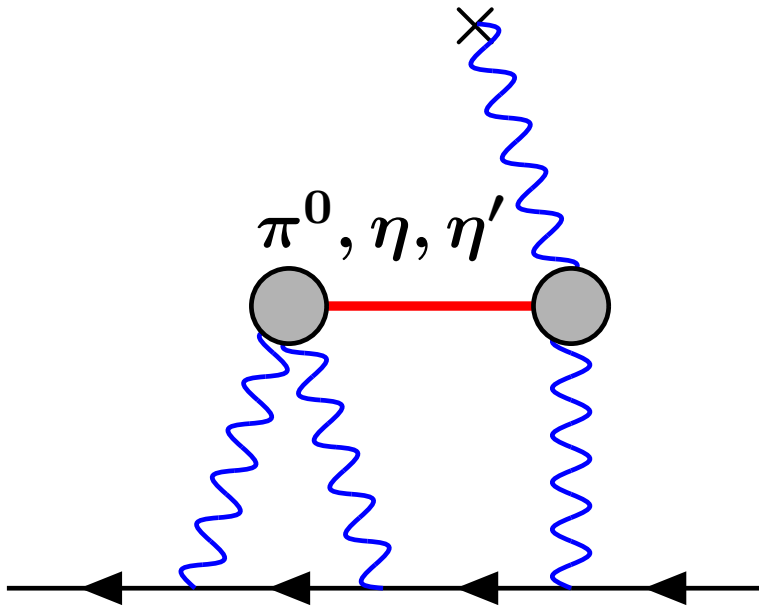


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Model for $\pi\pi\gamma(\gamma)$	$10^{10} \times a_\mu$
Point-like	-4.5
VMD <small>BPP</small>	-1.6
ENJL <small>BPP</small>	-1.8
HLS <small>HKS</small>	-0.4

Kaon loop much smaller but order 0.05×10^{-10}

Light-by-Light: π^0, η, η'



- double VMD: $\frac{m_V^4}{(q_1^2 - m_V^2)(q_2^2 - m_V^2)}$

- $1/p^2$: $\frac{m_V^4}{(q_1^2 + q_2^2 - m_V^2)}$

- $\frac{4\pi^2 F_\pi^2}{N_c} \frac{q_1^2 q_2^2 (q_1^2 + q_2^2) - h_2 q_1^2 q_2^2 + h_5 (q_1^2 + q_2^2) + (N_c M_1^4 M_2^4 / 4\pi^2 F_\pi^2)}{(q_1^2 + M_1^2)(q_1^2 + M_2^2)(q_2^2 + M_2^2)(q_1^2 + M_2^2)}$

KN, MV, h_2 different

Light-by-Light: π^0, η, η'

BP: Bijnens-Persson, hep-ph/0106130

Model $\pi^0 \gamma^* \gamma^*$	$10^{10} a_\mu (\pi^0)$	$10^{10} a_\mu (\pi^0, \eta, \eta')$
Point	33	
ENJL _{BPP}	5.9	8.5(1.3)
HLS _{HKS}	5.7	8.3(6)
double VMD _{BP}	5.6	7.9
$1/p^2$ _{BP}	4.1	7.9
KN	5.8	8.3(1.2)
MV1	6.3	

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KN	5.8	8.3(1.2)
MV1	6.3	
MV2	7.7	11.4(1.0)

MV2: a new short-distance constraint on $\Pi^{\mu\nu\alpha\beta}(p_1, p_2)$

Light-by-Light: π^0, η, η'

MV Look at: $\langle 0 | T(A_\mu(q_1) A_\nu(q_2) A_\nu(q_3)) | \gamma(q_4 \rightarrow 0) \rangle$

for $q_3^2 \ll q_2^2 \sim q_1^2$ thus $\hat{q} = q_1 \approx -q_2$

Light-by-Light: π^0, η, η'

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for $q_3^2 \ll q_2^2 \sim q_1^2$ thus $\hat{q} = q_1 \approx -q_2$

Use OPE: $T(A_\mu(q_1) A_\nu(q_2)) \sim \frac{1}{\hat{q}^2} \epsilon_{\mu\nu\alpha\beta} \hat{q}^\alpha j_5^\beta$

and the remainder estimated by π^0 saturation (q_3^2 small)

Light-by-Light: π^0, η, η'

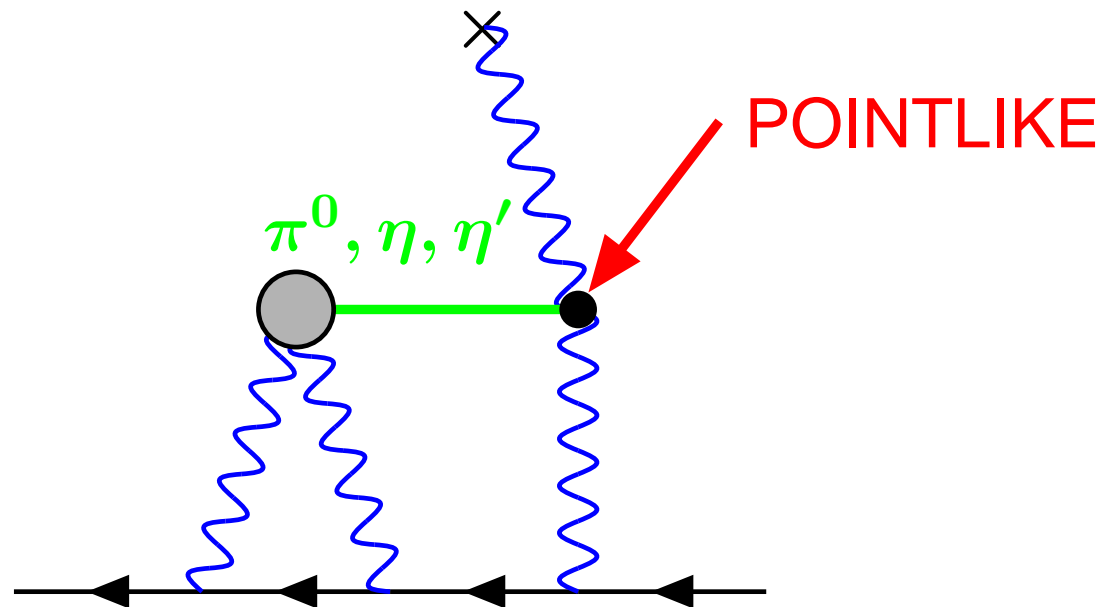
MV Look at: $\langle 0 | T(A_\mu(q_1) A_\nu(q_2) A_\nu(q_3)) | \gamma(q_4 \rightarrow 0) \rangle$

for $q_3^2 \ll q_2^2 \sim q_1^2$ thus $\hat{q} = q_1 \approx -q_2$

Use OPE: $T(A_\mu(q_1) A_\nu(q_2)) \sim \frac{1}{\hat{q}^2} \epsilon_{\mu\nu\alpha\beta} \hat{q}^\alpha j_5^\beta$

and the remainder estimated by π^0 saturation (q_3^2 small)

Implemented by:



Light-by-Light: axial vector, scalar

BPP: 0.25×10^{-10}

HKS: 0.174×10^{-10}

MV: axial vector: different model, get 0.7×10^{-10} , pointlike at one end, becomes 2.2×10^{-10}

Light-by-Light: Conclusions

$10^{10} a_\mu$	BPP	HKS	MV
quark loop	2.1 ± 0.3	0.97 ± 1.11	-
π, K loop	-1.9 ± 1.3	-0.45 ± 0.81	0 ± 1.0
π^0, η, η'	8.5 ± 1.3	8.27 ± 0.64	11.4 ± 1.0
axial vector	0.25 ± 0.1	0.174	2.2 ± 0.5
scalar	-0.68 ± 0.2	-	-
total			

Note: in BPP scalar and quark loop belong together

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Feeling: pointlike only way to SD?; π, K loop; axial vector

Central value: 9-12

Error: 3-4

Conclusions

$$\begin{aligned}
 a_\mu(\text{hadronic}) &\equiv a_\mu - a_\mu(\text{QED}) - a_\mu(\text{weak}) \\
 &= 720.6(5.8) \times 10^{-10}
 \end{aligned}$$

	$10^{10} a_\mu$	$10^{10} \delta a_\mu$
HVP (e^+e^-)	693.4 ± 6.4	
HVP (e^+e^- no KLOE)	696.3 ± 7.2	
HVL (τ)	711.0 ± 5.8	
HOVP	-9.8 ± 0.1	
LBL <small>BPP</small>	8.3 ± 3.2	$28.7 \pm 9.2 (3.1\sigma)$
LBL <small>HKS</small>	9.0 ± 1.5	$28.0 \pm 8.8 (3.2\sigma)$
LBL <small>MV</small>	13.6 ± 2.5	$23.4 \pm 9.0 (2.6\sigma)$
LBL <small>feeling</small>	11 ± 4	$26.0 \pm 9.5 (2.7\sigma)$

Systematic and statistical errors summed quadratically

Conclusions: some remarks

By adding linearly and taking last number:

$$(5.8)_{exp} + (5.3 + 3.5)_{HVP} + (4)_{LBL} + (0.3)_{weak} = 18.9 \\ \implies (1.4\sigma)$$

Note: $\mu^+ / \mu^- - 1 = -2.6 \pm 1.6$ for many years after CERN experiment

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2-3 σ discrepancy still best estimate