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# WW Interconnection Effects Well Above Threshold

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 $Z^0 Z^0$  vs.  $W^+ W^-$   
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Summary

# Introduction

(V.A. Khoze & TS, PRL72 (1994) 28, ZPC62 (1994) 281, EPJC6 (1999) 271;  
L. Lönnblad & TS, PLB351 (1995) 293, EPJC2 (1998) 165)

$$\Gamma_W, \Gamma_Z, \Gamma_t \approx 2 \text{ GeV}$$

$$\Gamma_h > 1.5 \text{ GeV for } m_h > 200 \text{ GeV}$$

$$\Gamma_{\text{SUSY}} \sim \text{GeV (often)}$$

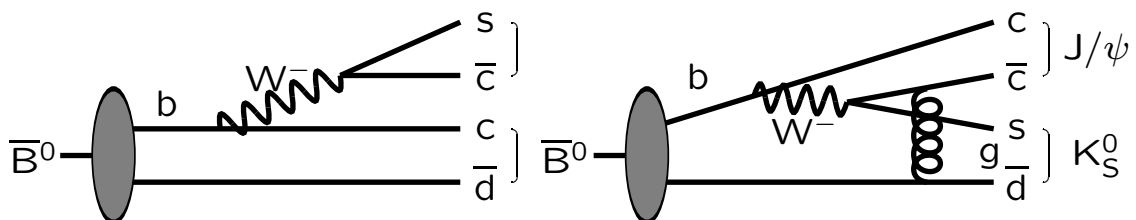
$$\tau = \frac{1}{\Gamma} \approx \frac{0.2 \text{ GeV fm}}{2 \text{ GeV}} = 0.1 \text{ fm} \ll r_{\text{had}} \approx 1 \text{ fm}$$

⇒ hadronic decay systems overlap,  
between pairs of resonances

⇒ cannot be considered separate systems!

Three main eras for interconnection:

1. **Perturbative:** suppressed for  $\omega > \Gamma$  by propagators/timescales ⇒ only soft gluons.
2. **Nonperturbative, hadronization process:** colour rearrangement.



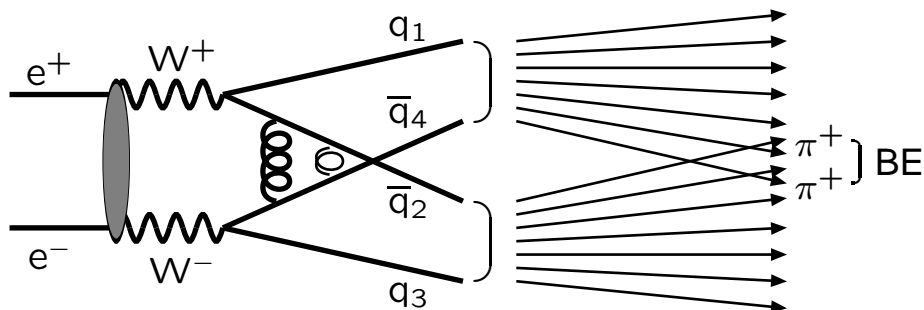
3. **Nonperturbative, hadronic phase:** Bose–Einstein.

Above topics among unsolved problems of strong interactions: confinement dynamics,  $1/N_C^2$  effects, QM interferences, . . . :

- opportunity to study dynamics of unstable particles,
- opportunity to study QCD in new ways, *but*
- risk to limit/spoil precision mass measurements.

So far mainly studied for  $m_W$  at LEP2:

1. **Perturbative:**  $\langle \delta m_W \rangle \lesssim 5 \text{ MeV}$ .
2. **Colour rearrangement:** many models, in general  $\langle \delta m_W \rangle \lesssim 40 \text{ MeV}$ .

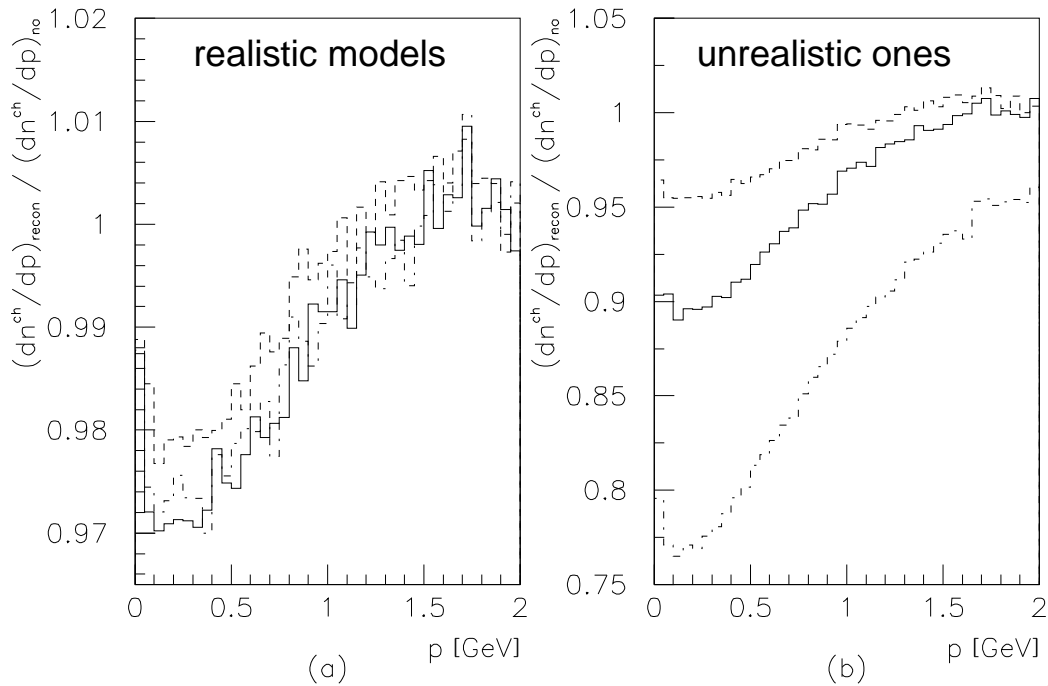


3. **Bose-Einstein:** symmetrization of unknown amplitude, wider spread 0–100 MeV among models, but realistically  $\langle \delta m_W \rangle \lesssim 40 \text{ MeV}$ .

In sum:  $\langle \delta m_W \rangle_{\text{tot}} < m_\pi$ ,  $\langle \delta m_W \rangle_{\text{tot}}/m_W \lesssim 0.1\%$ ; a small number that becomes of interest only because we aim for high accuracy.

# Connectometry – diagnosing interconnections:

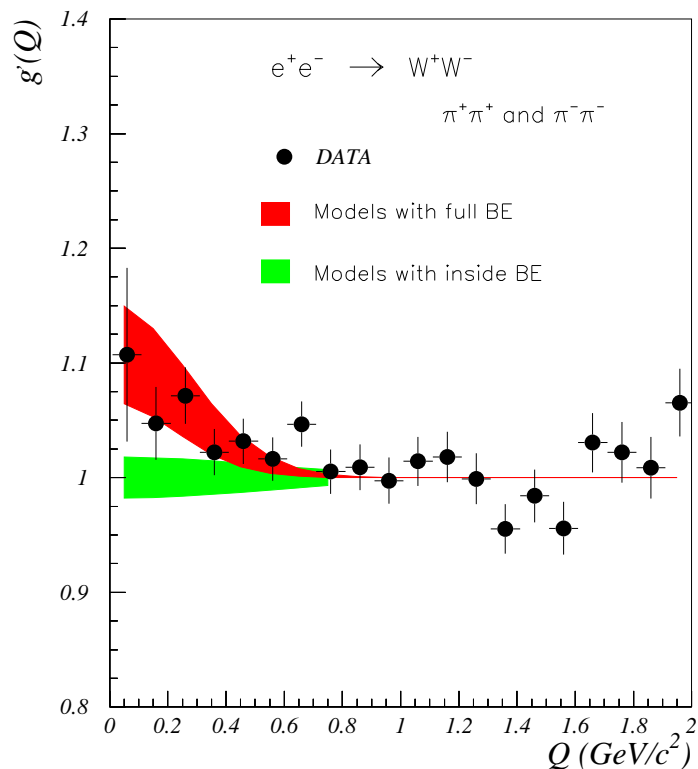
**Threshold: low-momentum particles depleted**



$\sim 4\sigma$  ( $\sim 2\sigma$ ) signal/experiment if  $500 \text{ pb}^{-1}$  at 172 (195) GeV. LEP1  $Z^0$  gives ‘ $Z^0 Z^0$  no-reconnection’ reference. (A) few alternatives.

BE:  
 first strong  
 indication  
 from DELPHI  
 (Moriond 99)

## DELPHI (preliminary)



# Colour rearrangement models

Here we compare

- Scenario I: string  $\approx$  elongated bag; reconnection probability  $\propto$  space–time volume overlap of strings.
- Scenario II: string  $\approx$  thin vortex line; reconnection occurs when cores of strings cross each other.
- Scenario II': as above, but reconnection at a crossing only occurs when the total string length is reduced.
- “GH” (freely based on G. Gustafson & J. Häkkinen): do the reconnection that reduces the total string length most.
- intermediate: reconnect after showers at middle of each string.
- instantaneous: reconnect before showers at middle of each string (unrealistic!).

Only at most one colour reconnection.

Other models/programs not considered here:

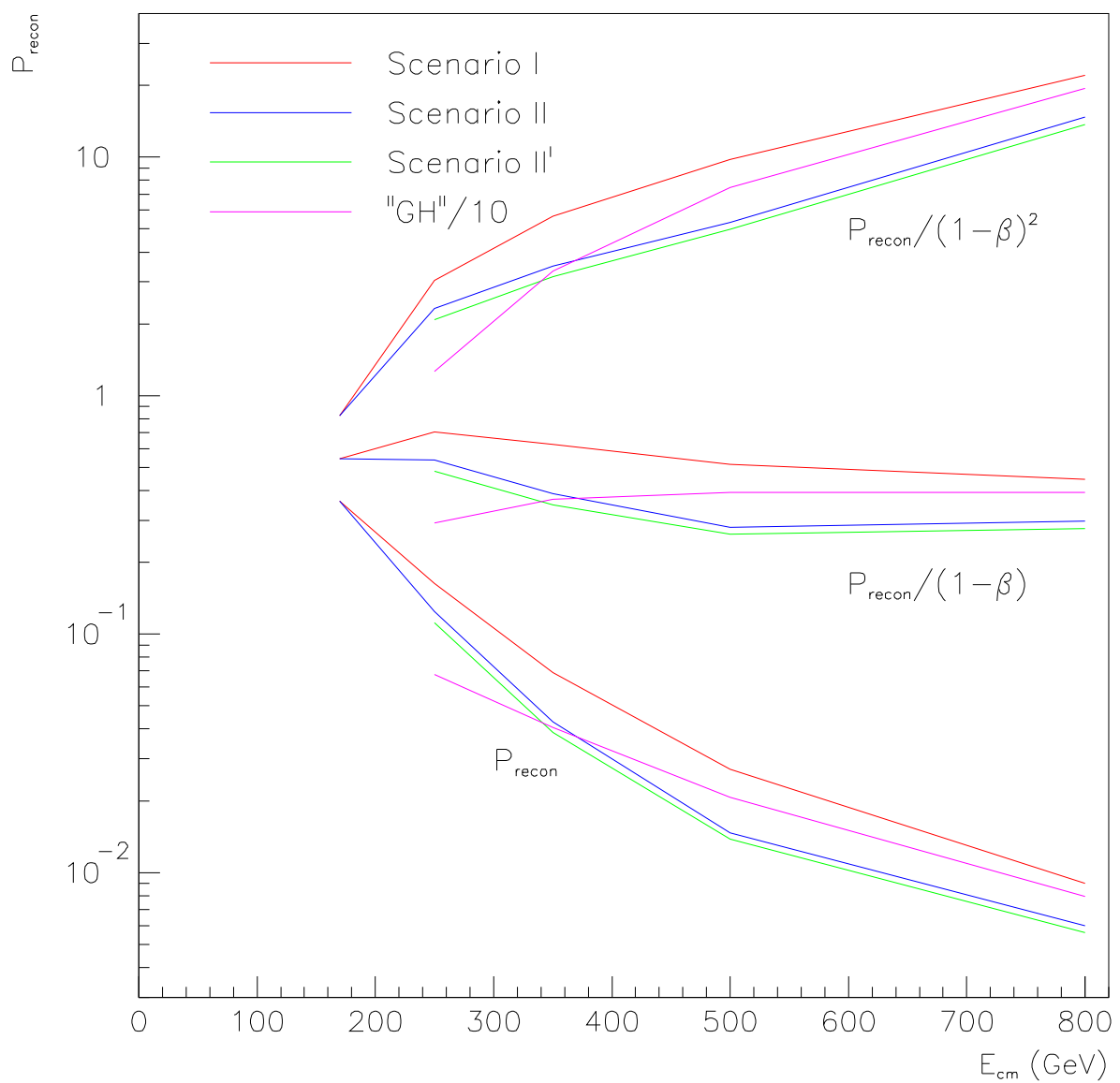
- L. Lönnblad (Ariadne)
- Š. Todorova–Nová
- B.R. Webber (Herwig)
- J. Ellis, K. Kinder-Geiger

# Reconnection probabilities

(A.P. Chapovsky & V.A. Khoze, hep-ph/9902343:)

**QED interconnection dampens roughly like  $(1 - \beta)^2$ !**

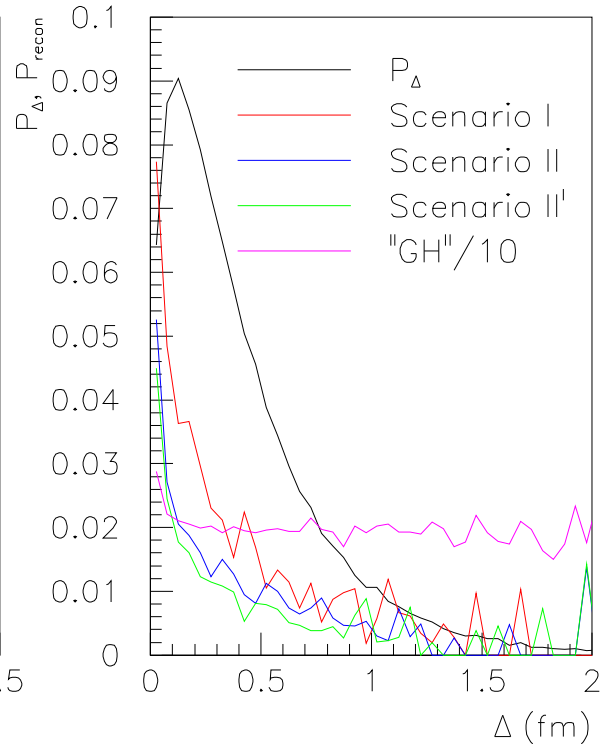
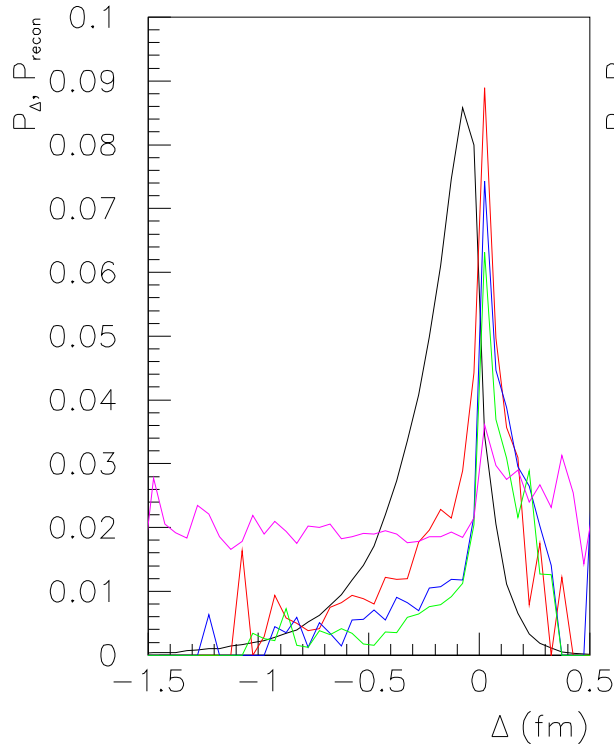
**Nonperturbative models more like  $(1 - \beta)$ :**



## Significant rôle played by ‘early’ W decays:

$$\Delta = \text{sign}(\sqrt{|\Delta\tau^2|}, \Delta\tau^2), \quad \Delta = \sqrt{\Delta t^2 + \Delta x^2}$$

$$\Delta\tau^2 = \Delta t^2 - \Delta x^2$$



Also topology

dependence:

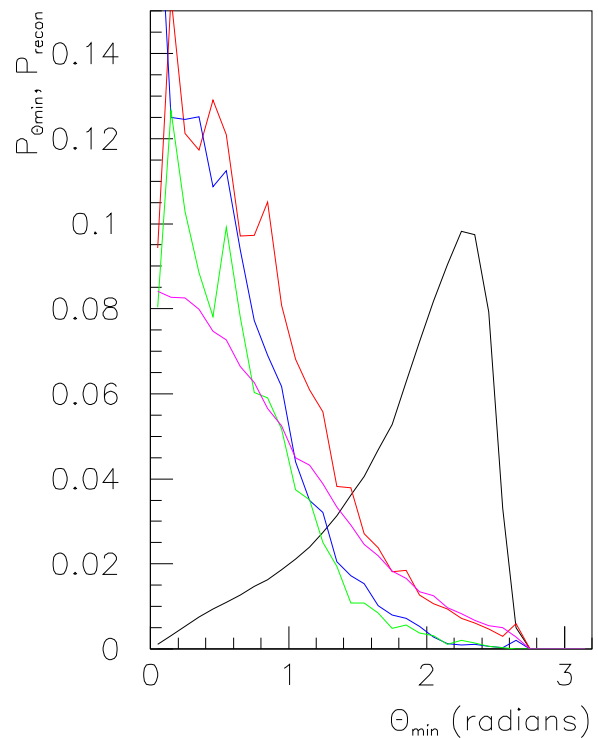
$$\theta_{\min} =$$

$$\min(\theta_{13}, \theta_{14}, \theta_{23}, \theta_{24})$$

$$\text{in } e^+e^- \rightarrow W^+W^-$$

$$\rightarrow q_1\bar{q}_2q_3\bar{q}_4$$

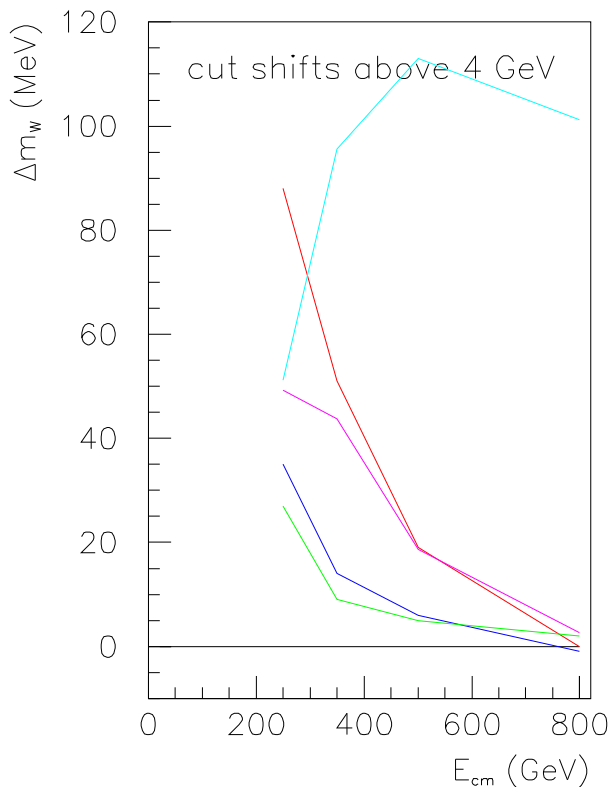
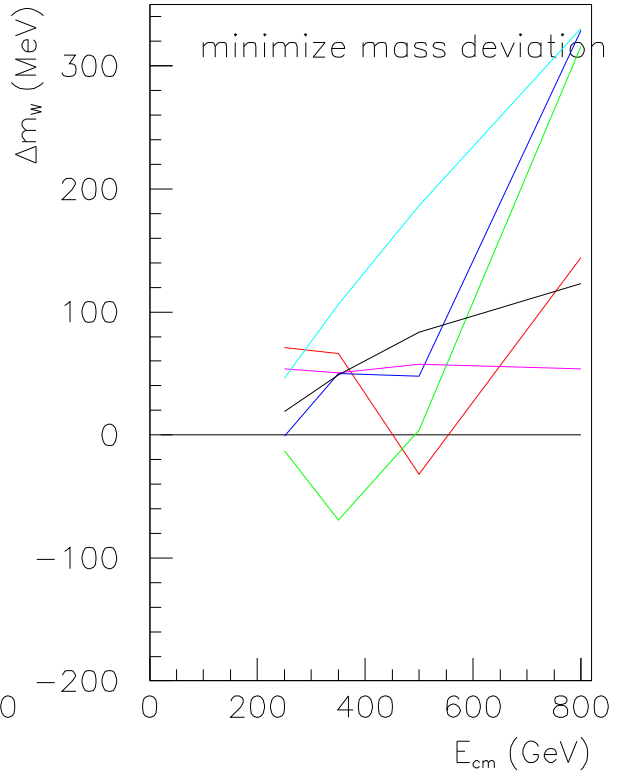
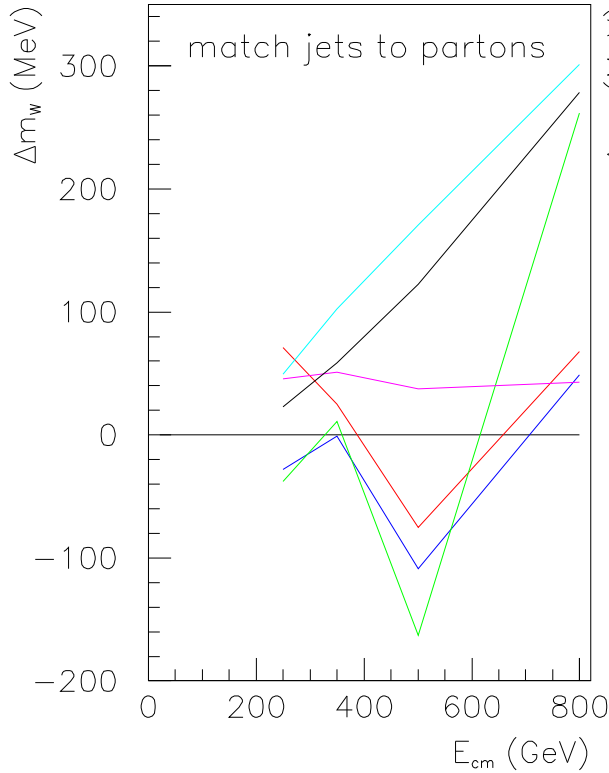
500 GeV, no ISR



# Mass shifts

Search for 4 jets:  $\theta_{\min} = 0.5(E_{\text{cm}}/200 \text{ GeV})$ ,  $E_{\min} = 20 \text{ GeV}$ .

Main criterion: minimize  $|m_{\text{jj}}^{(1)} - 80 \text{ GeV}| + |m_{\text{jj}}^{(2)} - 80 \text{ GeV}|$ .



- Scenario I
- Scenario II
- Scenario II'
- "GH"/10
- Intermediate/25
- Instantaneous/200

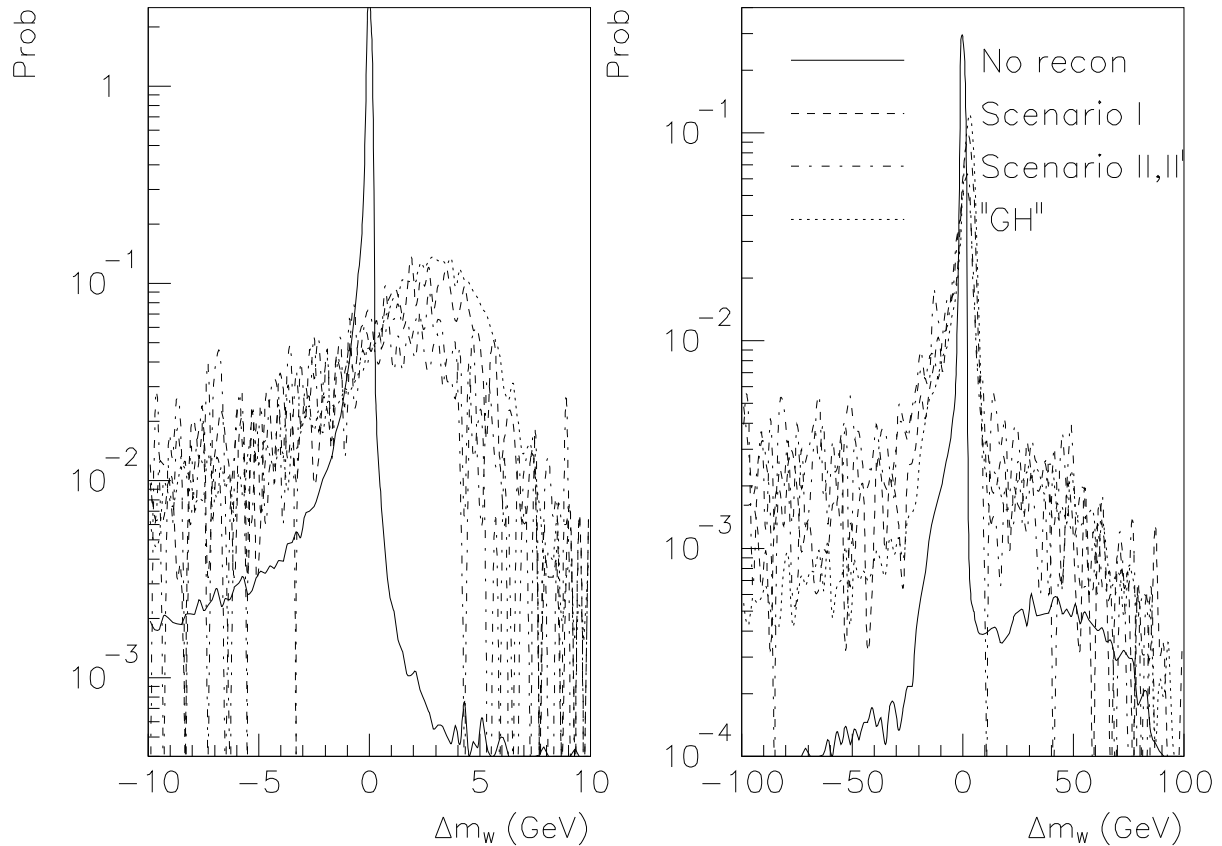
Similar results with other jet matching criteria

No ISR



Note big spread in mass shifts (at 500 GeV):

$$\Delta m_W = \frac{m_{jj}^{(1)} + m_{jj}^{(2)}}{2} - \frac{m_{W^+} + m_{W^-}}{2}$$



Upwards: natural reconnection mass shift!

Downwards by “trigger bias”: events with overlapping jets more likely to give reconnections *and* big mistakes in mass reconstruction.

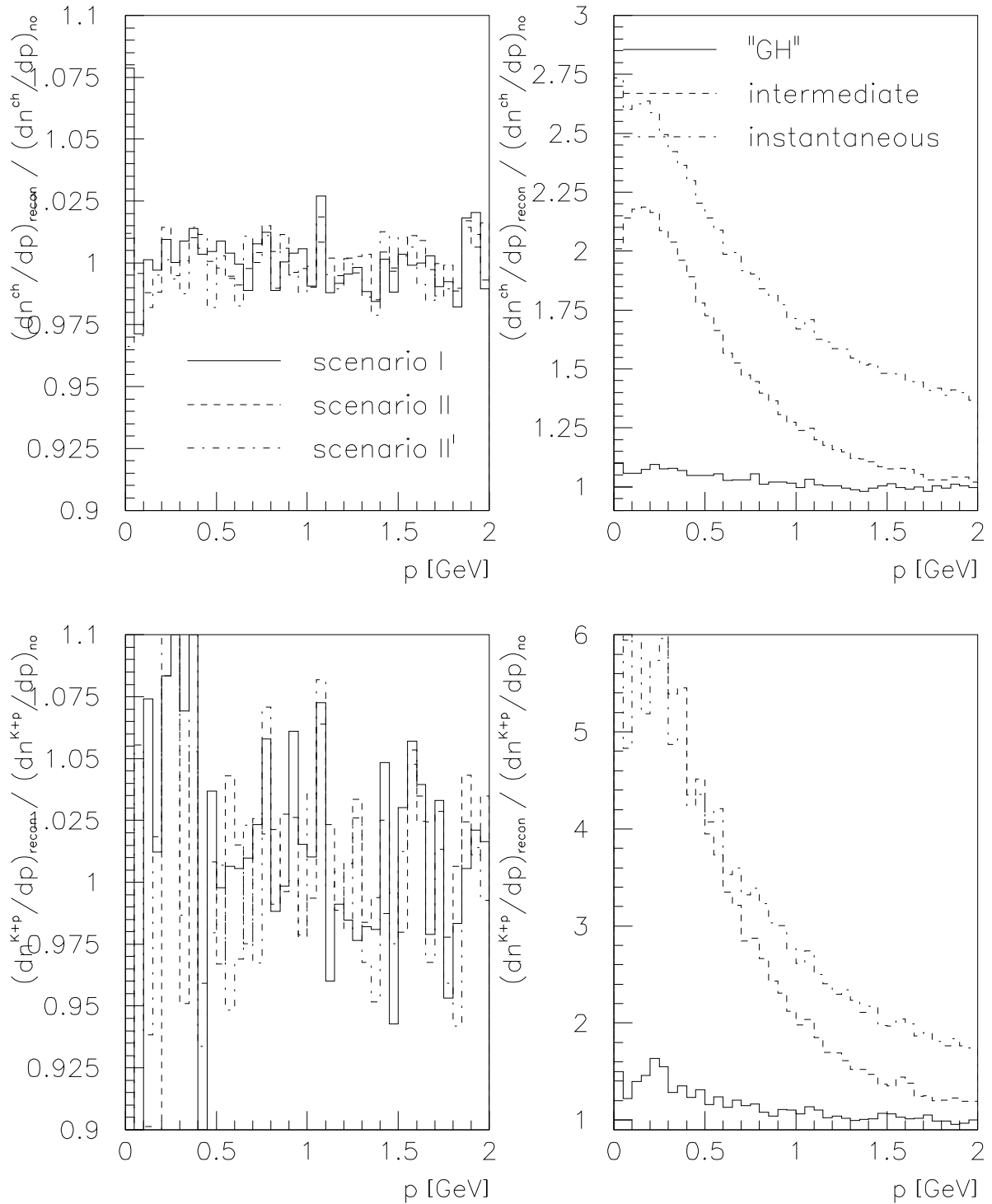
Crude (non-Gaussian tails!) run error estimate:

$$\sigma(m_W) \approx \frac{\sigma(\Delta m_W)}{\sqrt{n_{ev}}} \approx \frac{13 \text{ GeV}}{\sqrt{100000}} \approx 40 \text{ MeV}$$

Multiply by  $\sqrt{2}$  for difference scenarios.

# Inclusive signals

Now expect *enhancement at low p*:



Looks tough!

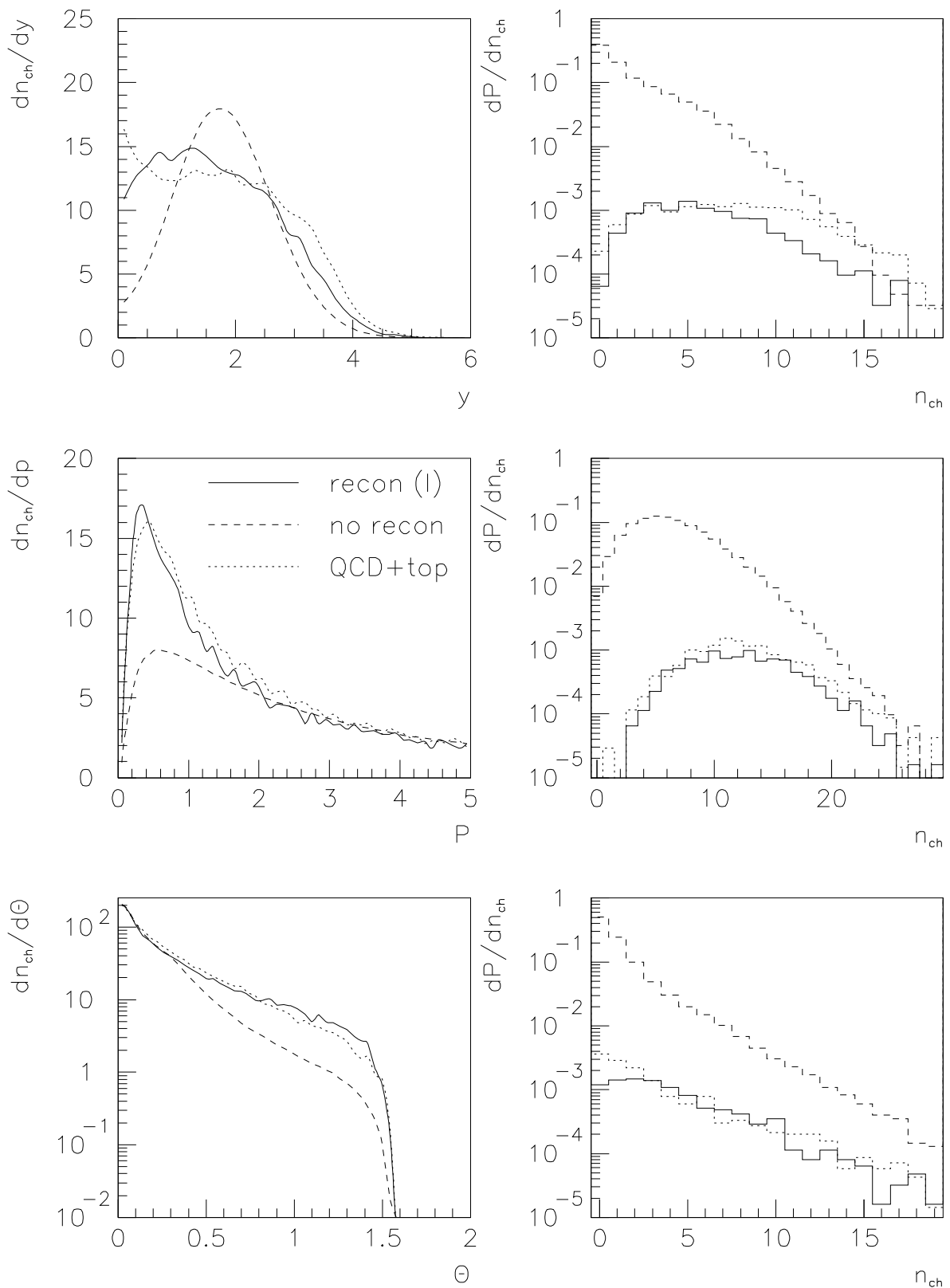
# Exclusive signals

Reconnection  $\Rightarrow$  more particles in the central region (i.e. regions between the two  $W$ 's).

Procedure (at 500 GeV):

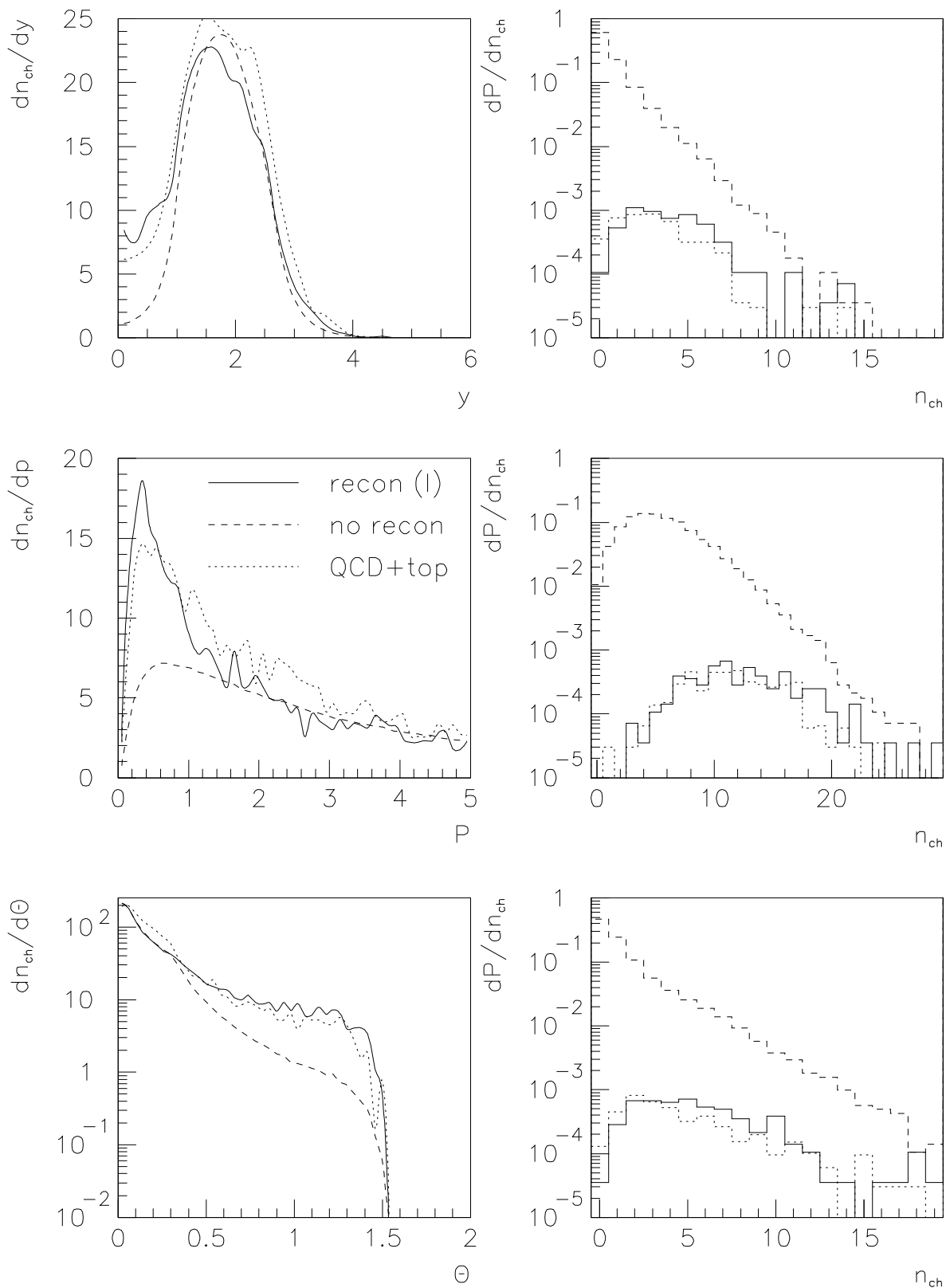
1. Orient event along linearized sphericity axis.
2. Reconstruct  $\geq 4$  jets with PYCLUS,  $d_{\text{join}} = 12.5$  GeV, and reject events with  $\geq 5$  jets.
3. Reconstruct the invariant mass in each hemisphere and require both to be in the range  $70 \text{ GeV} < m_{\text{hem}} < 90 \text{ GeV}$ .  
(Retains  $\sim 63\%$  of  $WW$ ,  
 $\sim 1.0\%$  of QCD+top background)
4. Calculate the total charged multiplicity  $n_{\text{ch}}$  in
  - (a) the region  $|y| < 0.5$  (Gustafson et al.);
  - (b) the region  $|p| < 1$  GeV; and
  - (c) everywhere, excluding cones around each of the four jets, with cone opening angle defined to the other jet in the same hemisphere.
5. Repeat (4) for events where all  $|y_{\text{jet}}| > 1$ .  
(Retains  $\sim 28\%$  of  $WW$ ,  
 $\sim 0.14\%$  of QCD+top background)

## Scenario I results, point (4):



... and slightly worse for scenarios II and II';  
better for "GH", intermediate, instantaneous.

## Scenario I results, point (5):

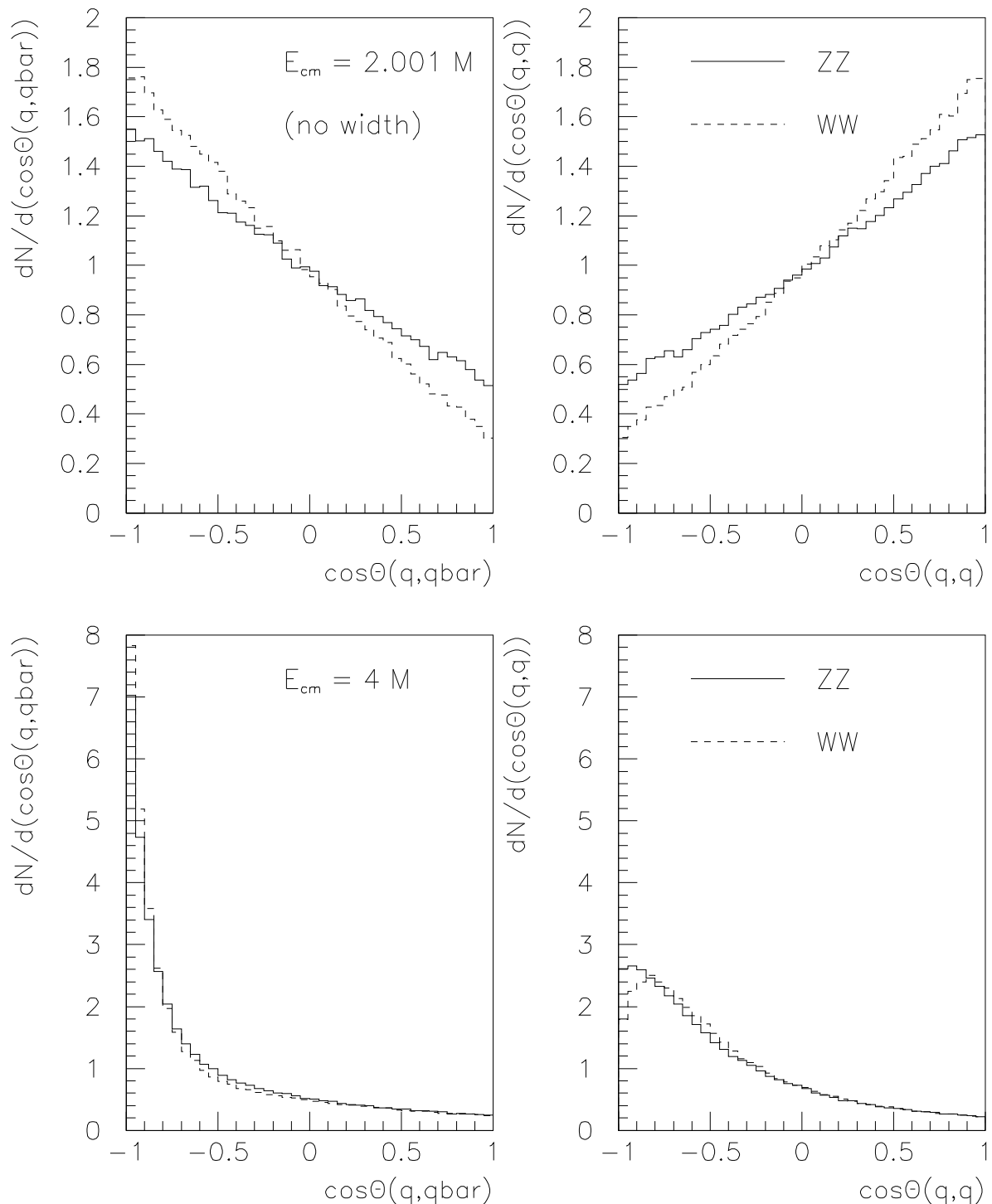


does clear up background for  $m_W$ ;  
but no success for reconnection hunting.

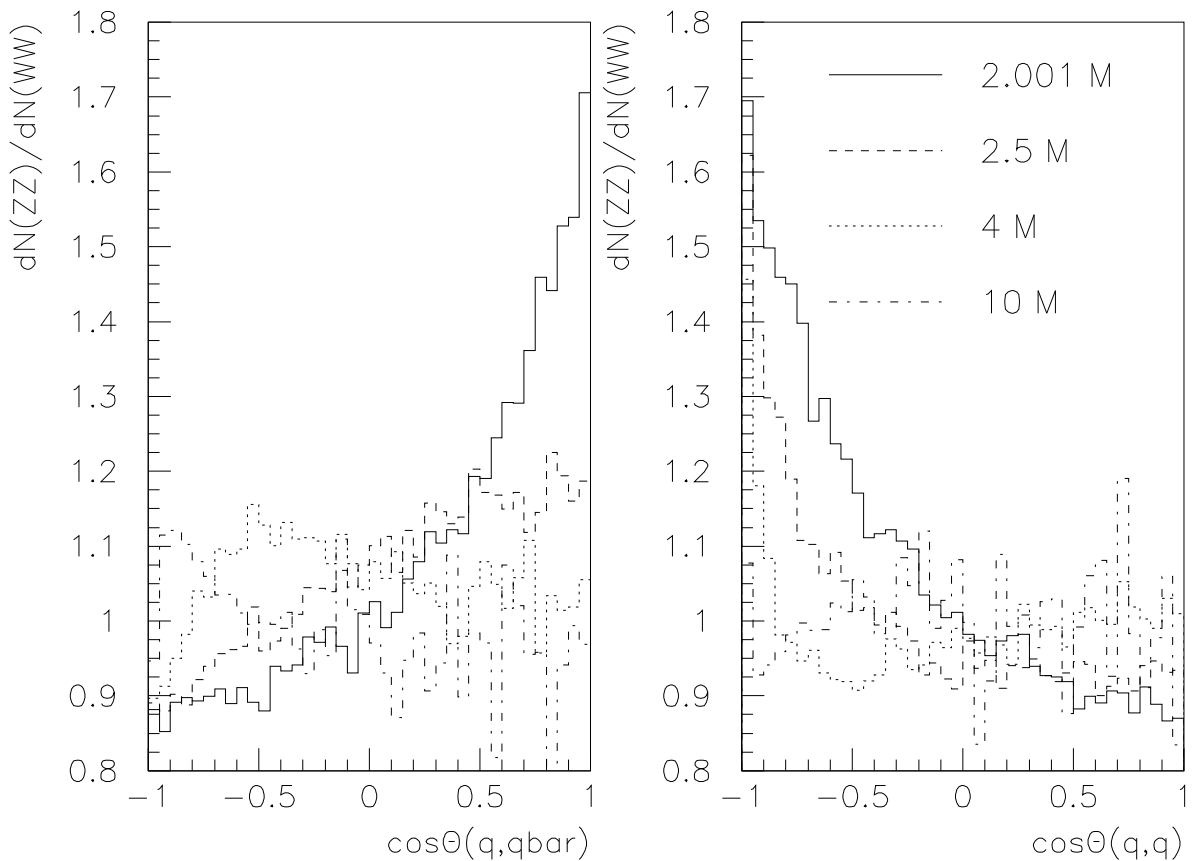
# $Z^0 Z^0$ vs. $W^+ W^-$

$Z^0$  mass and properties known  $\Rightarrow Z^0 Z^0$  excellent hunting ground for interconnection.

Compare  $Z^0 Z^0 / W^+ W^-$  angular distribution between  $q/\bar{q}$ 's from *different* bosons:



## Ratio normally close to unity:



## Why are $Z^0Z^0$ and $W^+W^-$ different?

1. Feynman graphs not all same:  
 $e^+e^- \rightarrow \gamma^*/Z^* \rightarrow W^+W^-$  absent for  $Z^0Z^0$ .
2. Another mix vector/axial couplings.
3. Higher mass  $\Rightarrow$  Z slower at fixed  $E_{cm}$ .
4. Larger width  $\Rightarrow$  Z decay vertices closer.

## Thus in general:

- More reconstructions for  $Z^0Z^0$ .  
 Scenario II at 500 GeV:  $P_{recon}$  is 3.2% for ZZ and 1.5% for WW.  $\sigma_{ZZ}/\sigma_{WW} \approx 1/6$ .
- $Z^0Z^0$  moderately good calibration for  $M_W$ .

# Bose–Einstein models

BE  $\approx$  symmetrization of *unknown* amplitude.

Many models. Our approach:

- reject interpretation as *global* weight;
- replace *local* reweighting among almost equivalent global configurations by a shift of momenta within pairs;
- perform shift so as to reproduce given input shape, e.g.  $f_2(Q) = 1 + \lambda \exp(-Q^2 R^2)$ , in limit of starting from a sparse population isotropic in phase space.

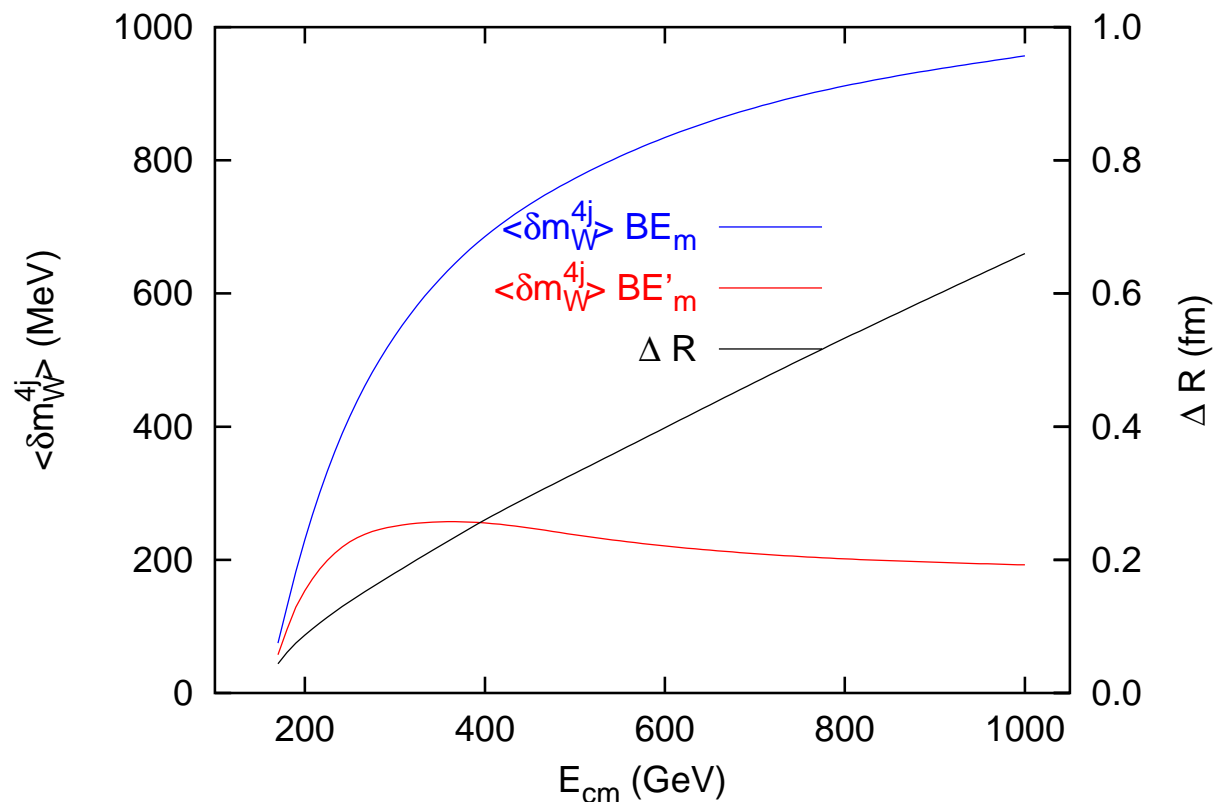
Problem: how conserve both energy and momentum?

- BE<sub>0</sub>: original global rescaling, requiring inconvenient subtraction.
- BE<sub>3</sub>: shift nearby pairs closer and further-away (identical) ones apart,  $f_2(Q) = (1 + \lambda \exp(-Q^2 R^2))(1 + \alpha \lambda \exp(-Q^2 R^2/9))$ , with  $\alpha \approx -0.2$  determined event-by-event by energy conservation.
- BE<sub>32</sub> modified form of above with  $f_2(0) = 1 + \lambda$ .



- $BE_m$ : shift apart a nearby (in mass) pair of non-identical particles for each identical pair pulled closer.
- $BE'_m$ :  $R \rightarrow R + \Delta R$  for pairs from different  $W$ 's,  $\Delta R = |x_{W^+} - x_{W^-}|$ .

Theoretical mass shifts — no reconstruction:



Conclusions of (previous) studies:

- Significant spread of  $\langle \delta m_W \rangle$  between models — signal of  $BE \neq$  known mass correction.
- Size of  $\langle \delta m_W \rangle$  markedly reduced by experimental procedure (even sign shift possible).

Further studies clearly warranted!

# Summary

- LEP2 may clarify Bose–Einstein situation.
- Both colour rearrangement and BE effects (may) remain significant over the full LC energy range.
- The fraction of (significantly) affected events goes down with energy but the effect per event comes up.
- It appears feasible to reduce interconnection “background”, by suitable cuts, to harmless levels for  $m_{VV}$  determinations.
- The possibility to dig out a colour rearrangement signal not yet established, but should be doable with the right cuts.
- $Z^0Z^0$  events should display larger effects than  $W^+W^-$  ones, by about a factor of two.
- How do we distinguish models (for reconnections and for BE)?

The work continues . . .

. . .and so does the excitement!